

P.E. Civil Exam Review:
Foundation

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FOUNDATION



National Council of Examiners for Engineering and Surveying

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STUDY REFERENCES

- Foundation Engineering; Peck Hanson & Thornburn
- Introductory Soil Mechanics and Foundations; Sowers
- NAVFAC Design Manuals DM-7.1 & 7.2
- Foundation Analysis and Design; Bowles
- Practical Foundation Engineering Handbook; Brown

Foundation Type Selection

Shallow Bearing Footings: Adequate Bearing Capacity
Acceptable Settlement_

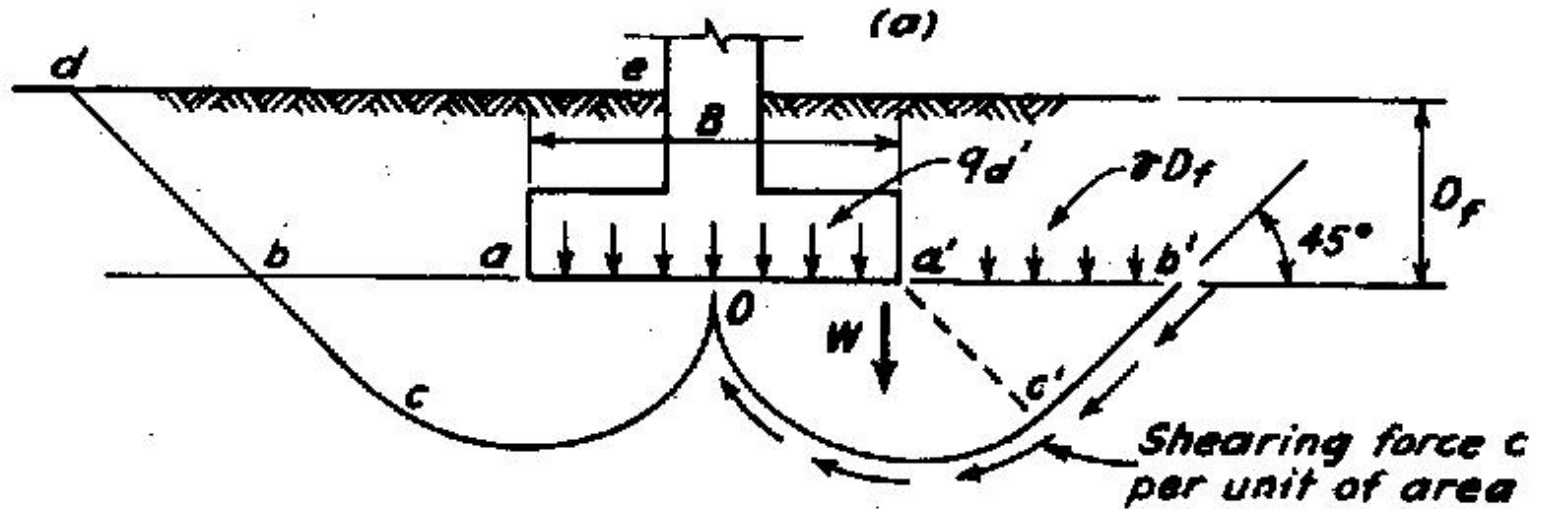
Mat or Raft: Low Bearing Pressure & Usually Minimum Settlement

Deep Foundations: Higher Load Capacity & Minimal Settlement

Drilled Piers: (Caissons) Large Load Capacity; Good Quality Control
Generally Limited to < 100'

Driven/Auger or Injected Piles: Moderate Load Capacity
Can Extend >> 100'

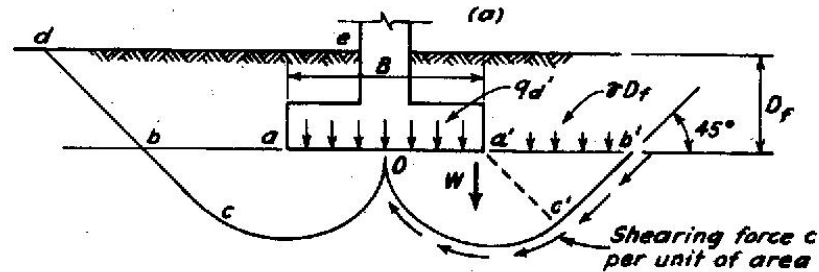
General Bearing Capacity: Terzaghi-Meyerhof



$$\frac{1}{2} \gamma B N_\gamma + C N_c + q N_q - \gamma D_f$$

Note: $q = \gamma D_f$

General Bearing Capacity



$$Q_a = \frac{Q_{net}}{F} = \frac{Q_{ult} - \gamma D_f}{F} = \frac{(\frac{1}{2} \gamma B N_\gamma + C N_c + q N_q - \gamma D_f)}{F}$$

Where:

Q_a = maximum net allowable bearing pressure

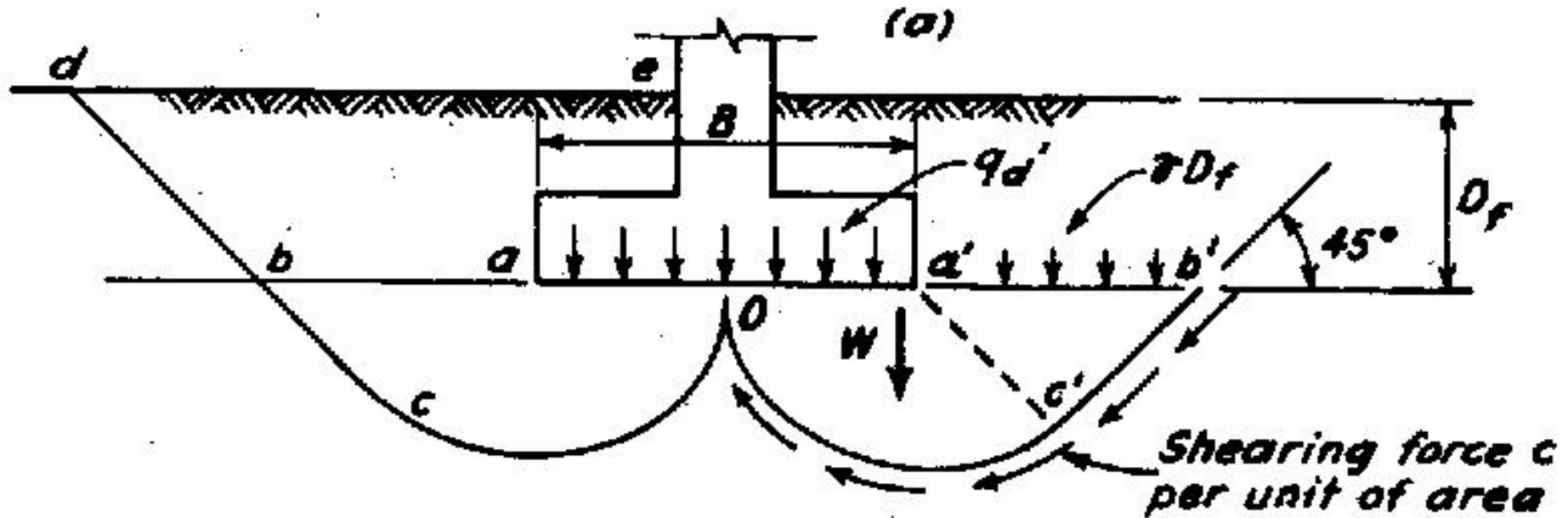
F = factor
of safety

Q_{net} = maximum net bearing pressure

(typ. 2-3)

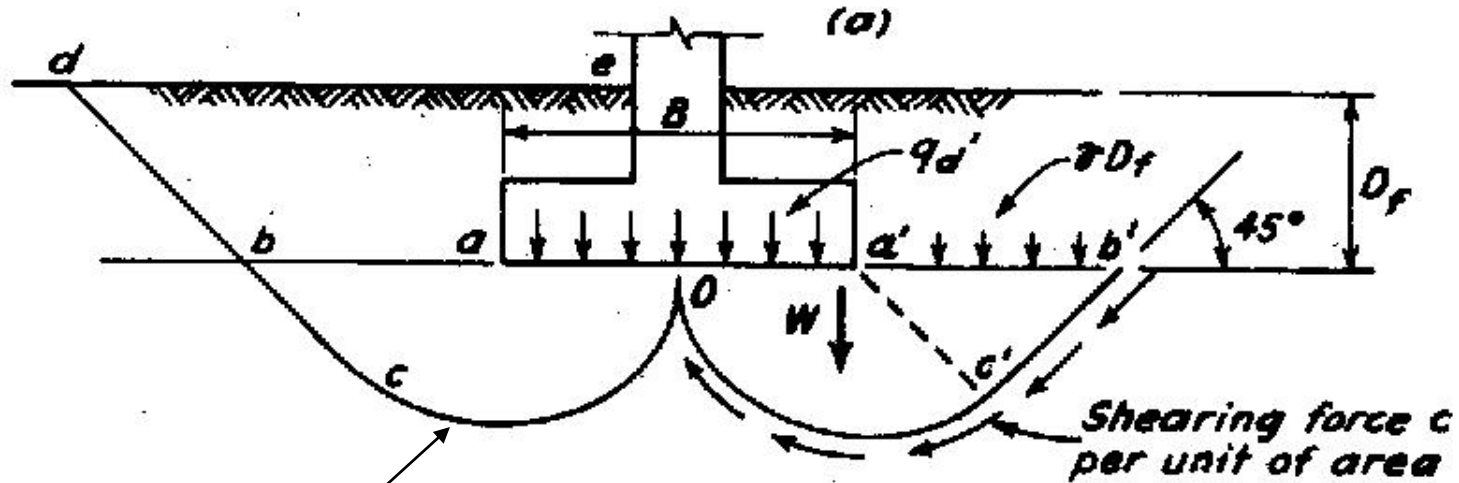
Q_{ult} = ultimate general bearing capacity

General Bearing Capacity



$$Q_{\text{net}} (\text{at } D_f) = Q_{d'} = \left(\frac{1}{2} \gamma B N_\gamma + C N_c + q N_q - \gamma D_f \right)$$

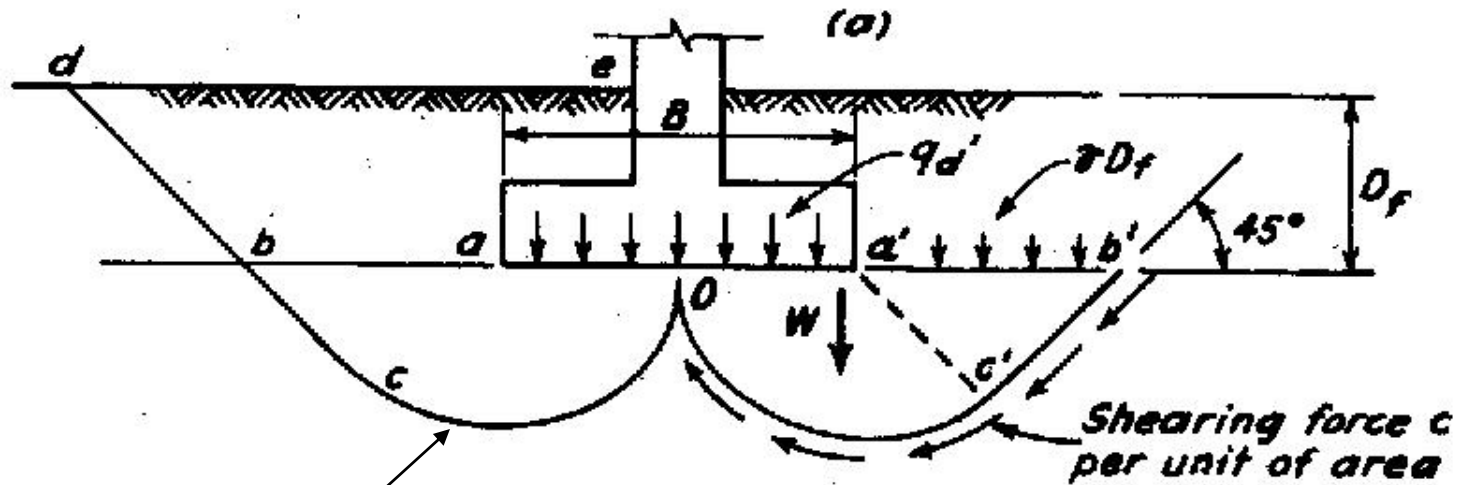
General Bearing Capacity



$$Q_{\text{net}}(\text{at } D_f) = Q_{d'} = \left(\frac{1}{2} \gamma B N_\gamma + C N_c + q N_q - \gamma D_f \right)$$

N_γ = footing width & soil weight factor, accounts for friction along bearing failure line ($\Rightarrow 1$ if $\phi=0$)

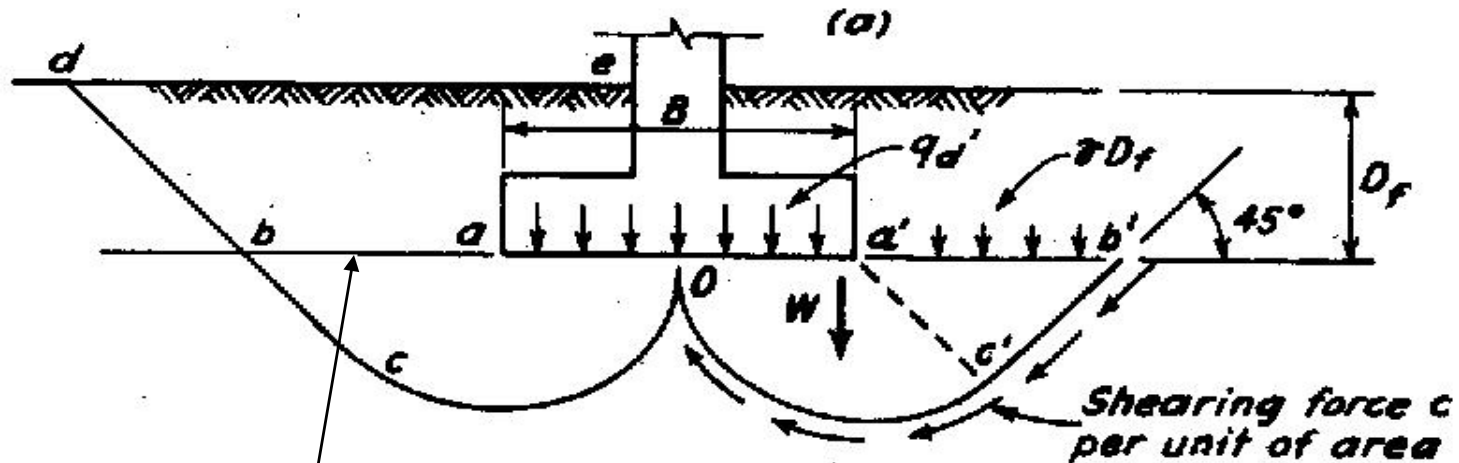
General Bearing Capacity



$$Q_{\text{net}}(\text{at } D_f) = Q_{d'} = \left(\frac{1}{2} \gamma B N_\gamma + C N_c + q N_q - \gamma D_f \right)$$

N_c = soil cohesion factor, accounts for cohesion along bearing failure line ($\Rightarrow 5.3 \pm$ if $\phi=0$)

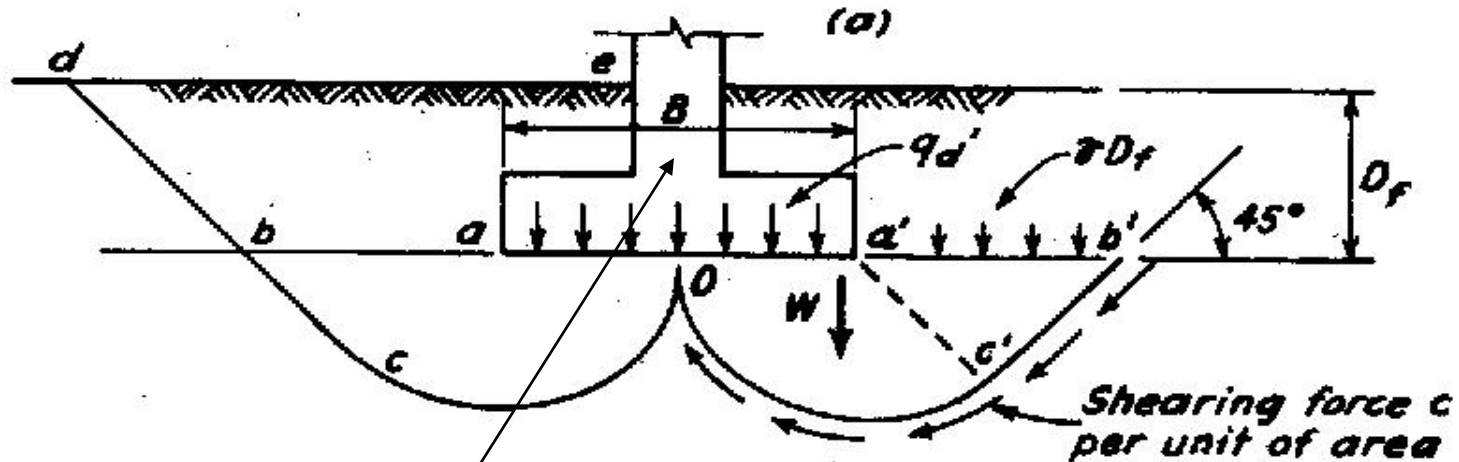
General Bearing Capacity



$$Q_{\text{net}} (\text{at } D_f) = q_{d'} = \left(\frac{1}{2} \gamma B N_\gamma + C N_c + q N_q - \gamma D_f \right)$$

N_q = surcharge factor, accounts for weight above the bearing failure line ($\Rightarrow 1$ if $\phi=0$)

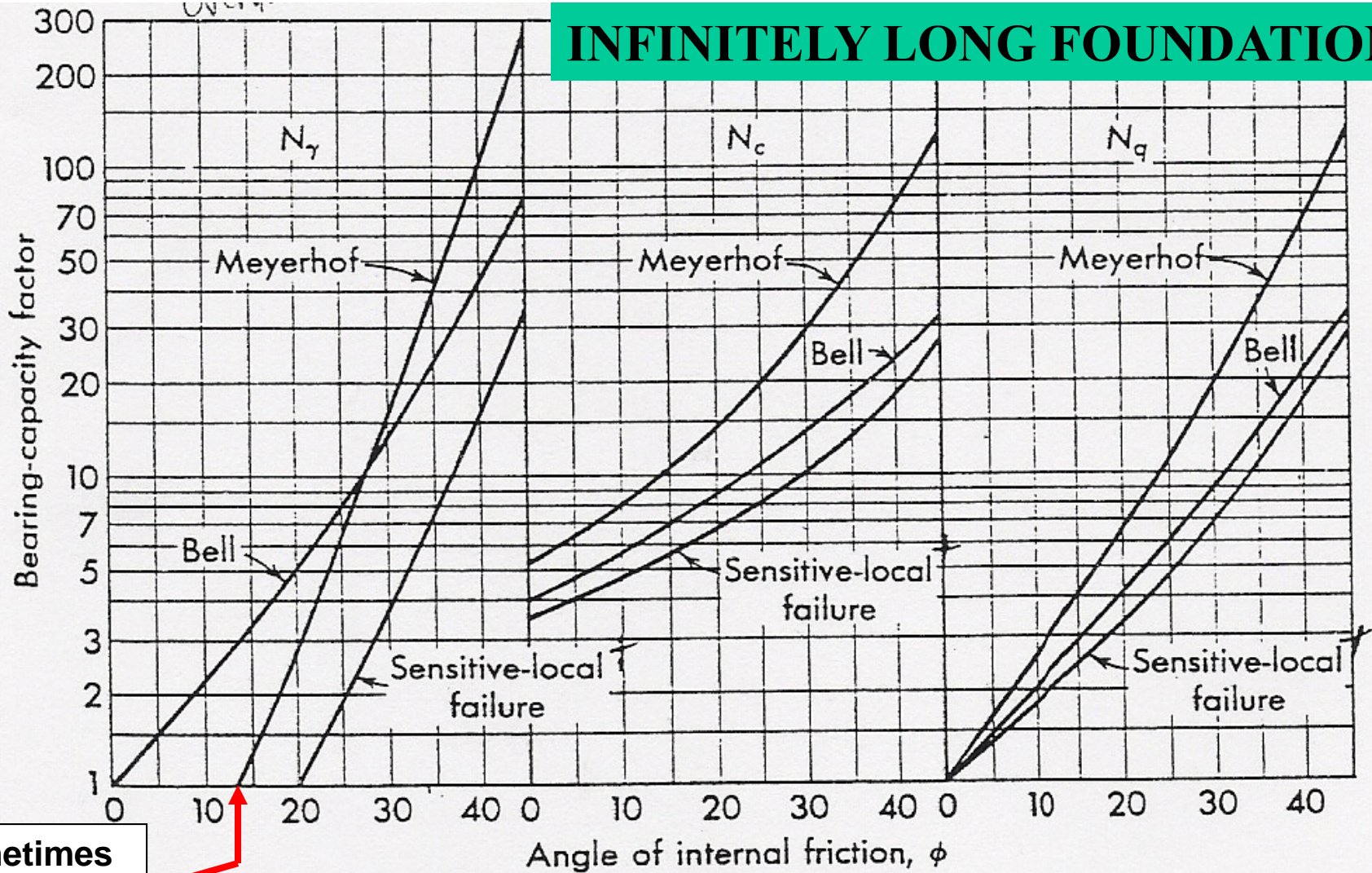
General Bearing Capacity



$$Q_{\text{net}} (\text{at } D_f) = Q_{d'} = \left(\frac{1}{2} \gamma B N_\gamma + C N_c + q N_q - \gamma D_f \right)$$

D_f = net bearing correction, reduces the ultimate bearing capacity by the weight of the soil and foundation above the bearing surface

INFINITELY LONG FOUNDATION



Sometimes shown as ZERO

$$Q_{net} = \left(\frac{1}{2} \gamma B N_\gamma + C N_c + q N_q - \gamma D_f \right)$$

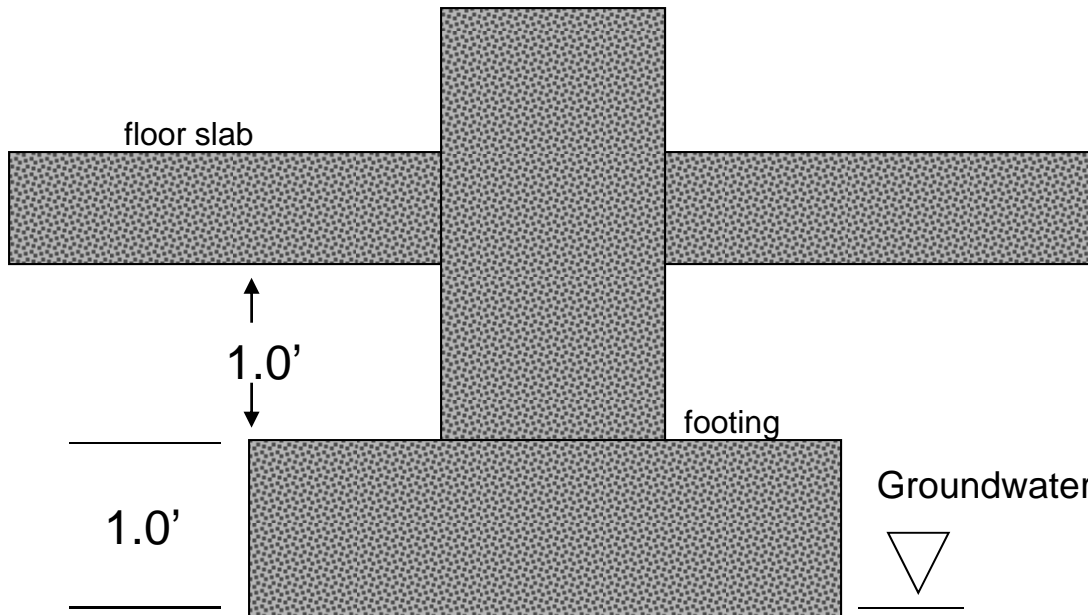
Note: multiply "N" factors by shape corrections for other shape footings

Bearing Factor Corrections for Rectangular and Circular Foundations

<u>Shape</u>	<u>N_c Correction</u>	<u>N_γ Correction</u>
Square	1.25	0.85
Rectangular L/B=2	1.12	0.90
L/B=5	1.05	0.95
Circular (dia. = B)	1.2	0.70

Calculate the Bearing Capacity

Use factor of safety = 3



Interior Square Footing
DL=75 kips LL=50 kips

0.5'

Soil moist unit weight=120 pcf

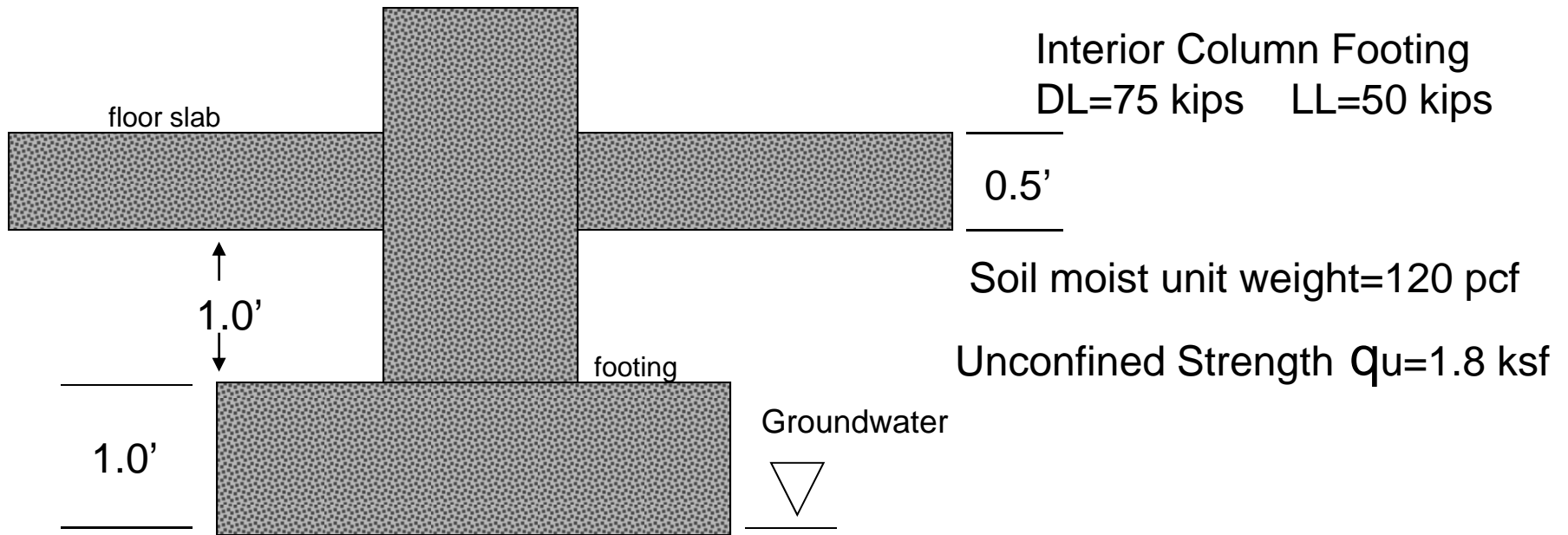
Unconfined Strength $q_u=1.8$ ksf

A) 2000 psf

B) 2500 psf

C) 3000 psf

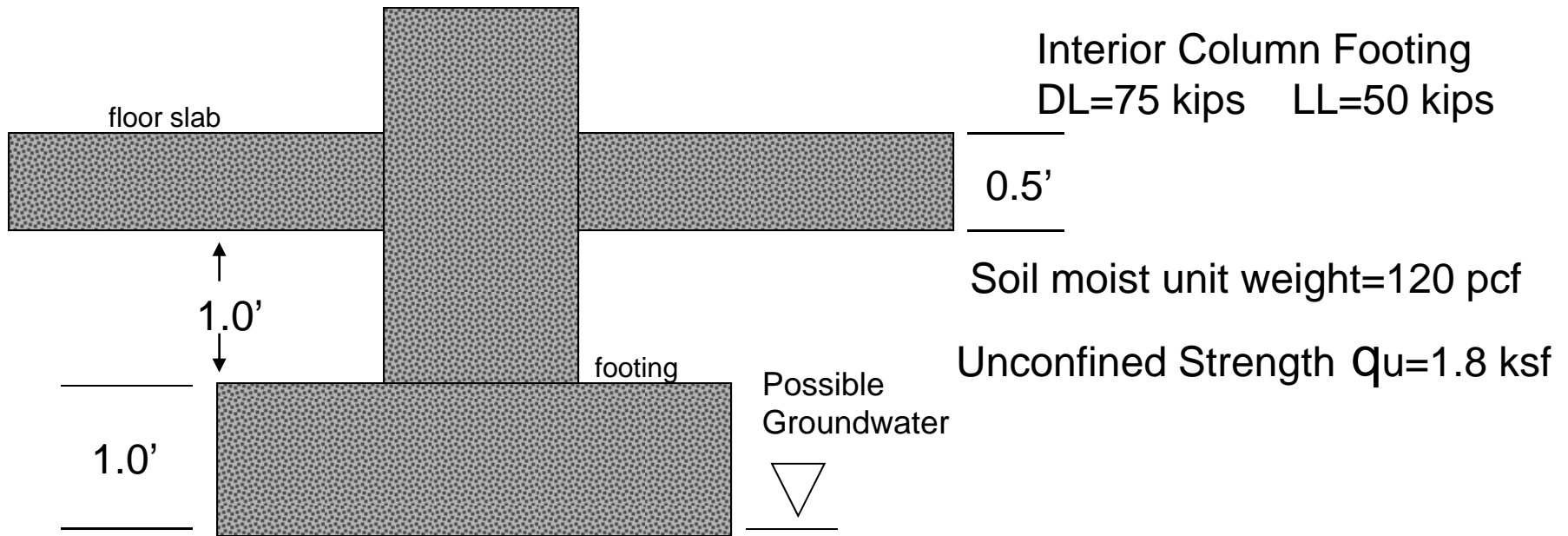
Bearing Capacity – Shallow Footing



$$Q_a = \frac{Q_{ult} - \gamma D_f}{F} = \frac{(1/2 \gamma B N_\gamma + C N_c + q N_q - \gamma D_f)}{F}$$

$$\text{since } \phi = 0 \quad N_\gamma = 1 \quad N_q = 1$$

Bearing Capacity – Shallow Footing



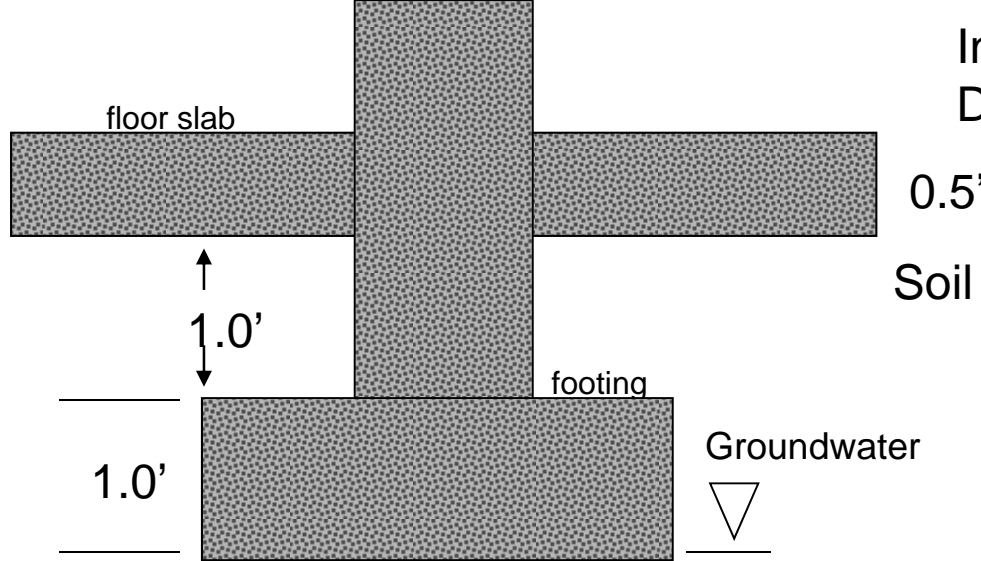
$$Q_a = \frac{Q_{ult} - \gamma D_f}{F} = \frac{(\frac{1}{2} \gamma B N_\gamma + C N_c + q N_q - \gamma D_f)}{F}$$

Assume a reasonable footing width $B = 7.9$ feet

From Tables $N_c = 5.3$; for square footing shape factor = 1.25

$N_\gamma = 1$; shape factor = 0.85

$N_q = 1$; no surcharge shape factor



Interior Column Footing
DL=75 kips LL=50 kips

0.5'

Soil moist unit weight=120 pcf

$q_u=1.8$ ksf

$C=1/2 q_u = 1.8 / 2$

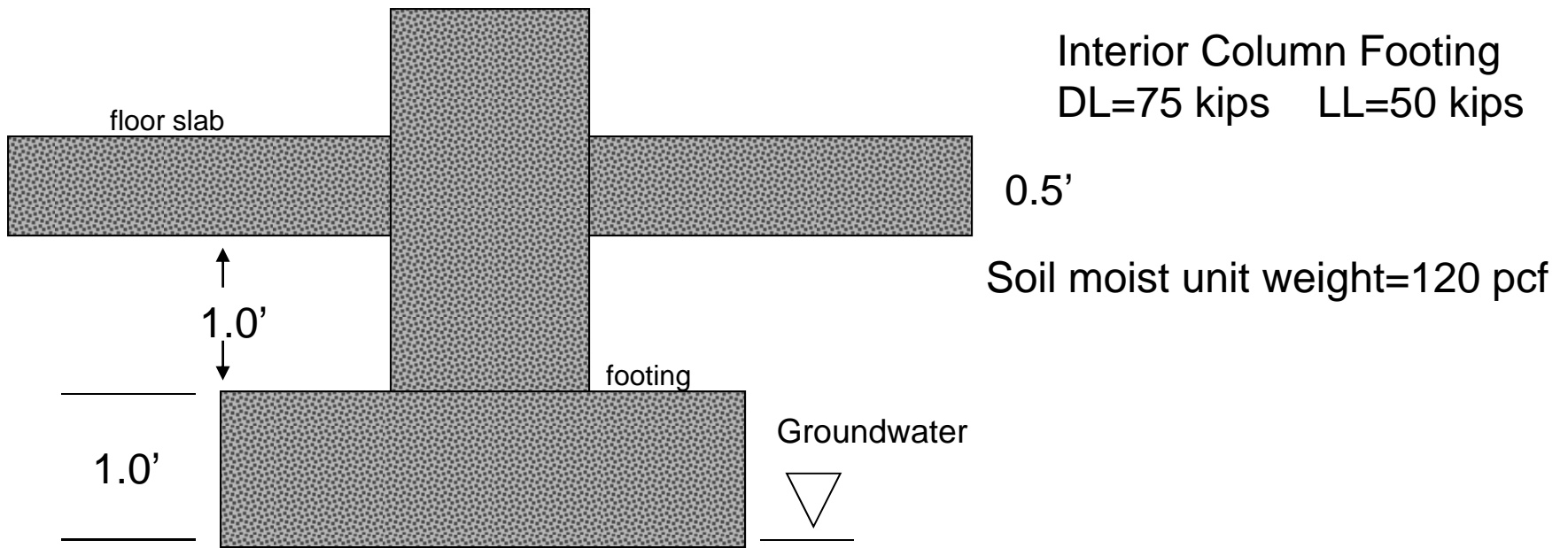
= 0.9 ksf or 900 psf

$$Q_a = \frac{(0.85)1/2(120-62.4)7.9(1)+1.25(900(5.3)+[(2.5)120(1)-(2.5)120]}{3}$$

$$Q_a = \frac{193+5963}{3} = 2052 \text{ psf net allowable}$$

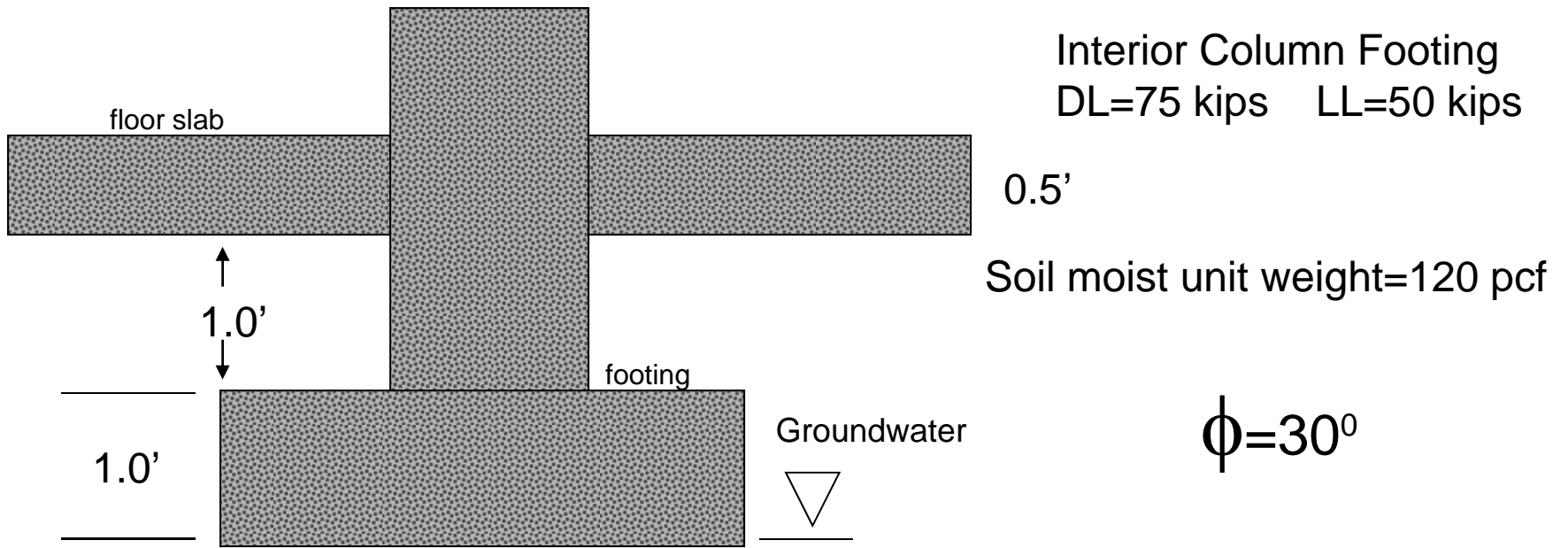
Answer is "A"

Footing Size= $(75,000+50,000)/2000 = 62.5 \text{ ft}^2$ $\sqrt{\quad} = 7.9'$
say 7' – 11" \square



Recalculate for sand with water at bearing level:

$$\phi=30^{\circ}$$



Interior Column Footing
DL=75 kips LL=50 kips

0.5'

Soil moist unit weight=120 pcf

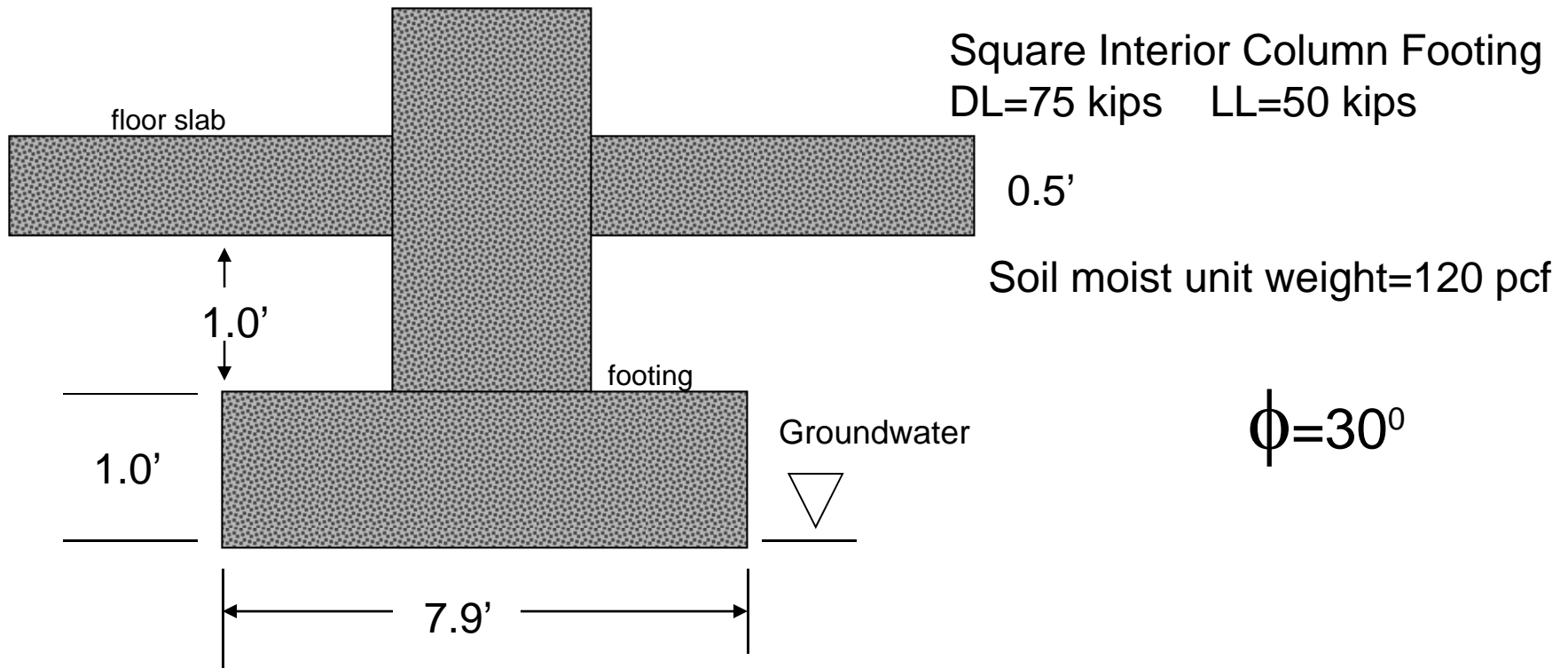
$\phi = 30^\circ$

Groundwater
▽

$$Q_{ult} = \frac{1}{2} \gamma_b B N_\gamma + \gamma D_f N_q$$

↑
↓
↖
↗

Base failure submerged unit weight Overburden above water- moist unit weight



$$Q_{ult} = \frac{1}{2} \gamma_b B N_\gamma + \gamma D_f N_q$$

$$= \frac{1}{2} (120 - 62.4) 7.9 (17) 0.85 + 120 (2.5) 20 = 9,288 \text{ psf}$$

shape factor

$$\text{net} = 9,288 - 2.5(120) = 8,988$$

$$\text{for FS} = 3; 8,988 / 3 = 2,996 \text{ psf}$$

say = 3000 psf net allowable

Lateral Earth Pressure

$$\sigma_h = \sigma_v k = d \gamma k$$

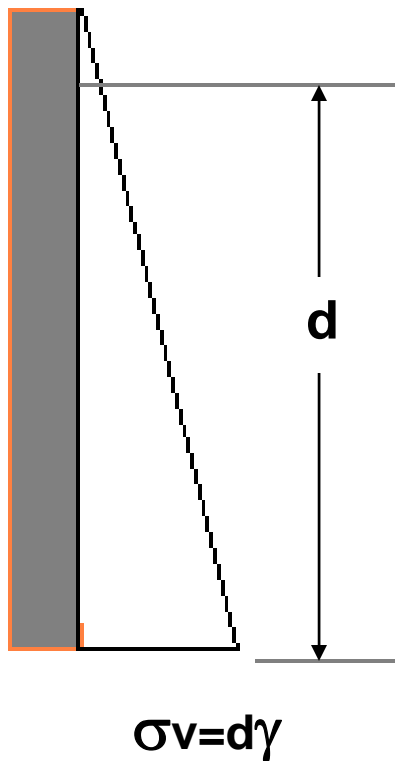
“k” depends on
loading condition

Active

At Rest

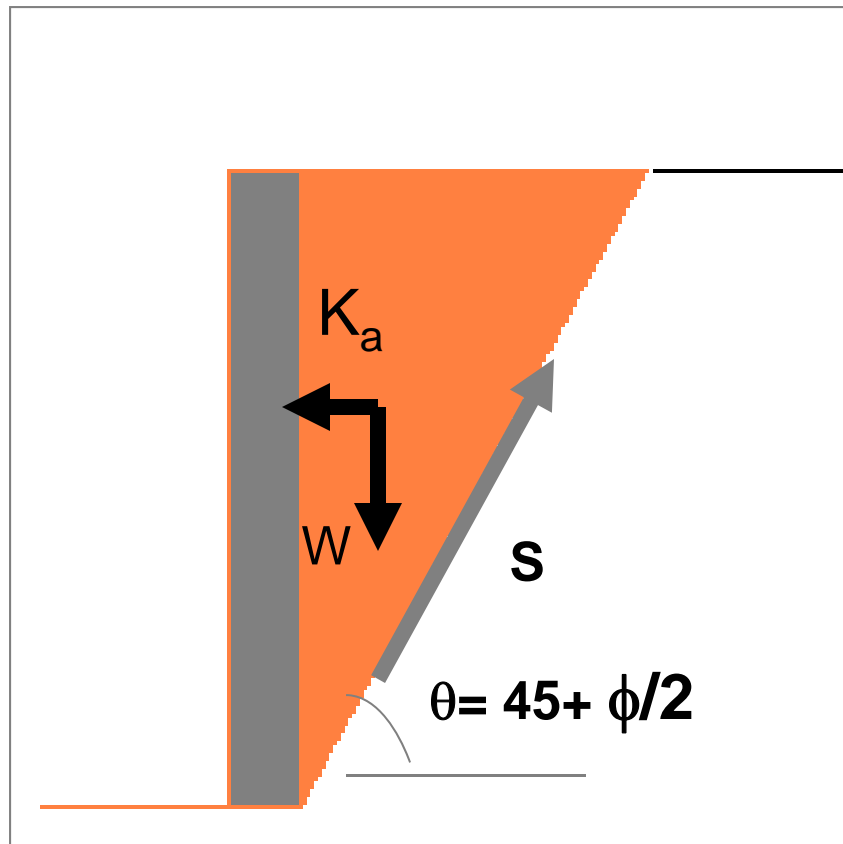
Passive

equivalent fluid
pressure = γk



Active Lateral Earth Pressure

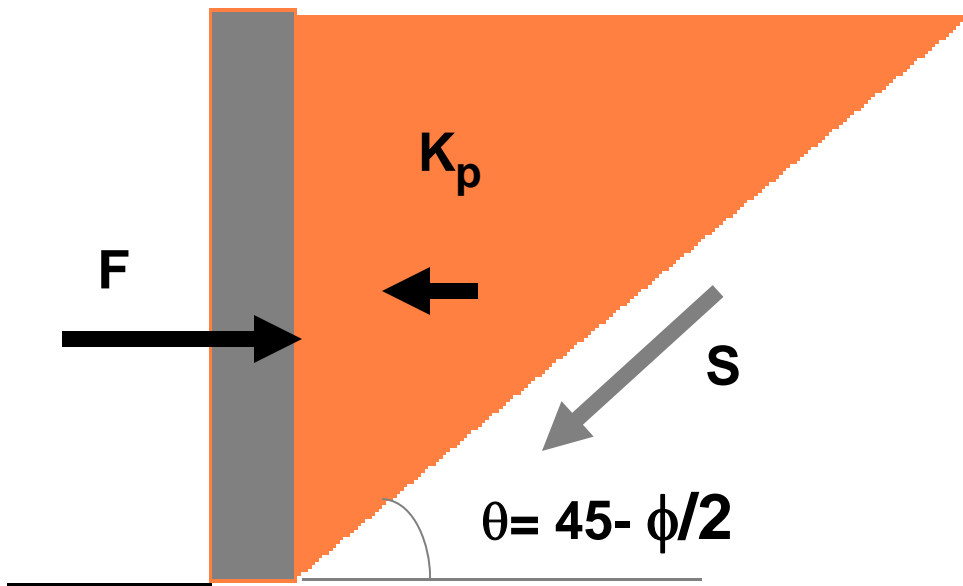
(load primarily gravity or surcharge - vertical)



Minimum pressure
achieved when soil
strains toward wall
& mobilizes shear
resistance

$$k_a = \tan^2(45 - \phi/2)$$

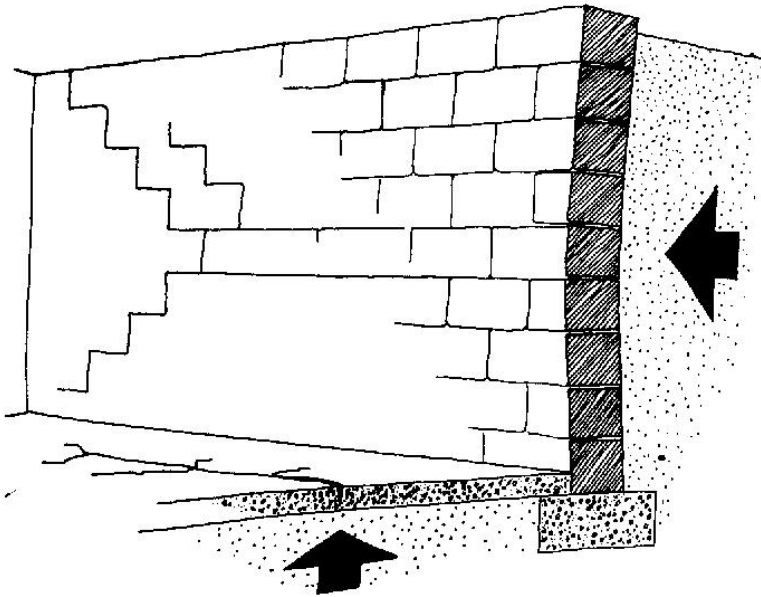
Passive Lateral Earth Pressure



The maximum pressure achieved when structure is pushed toward soil - lateral bearing failure at limit

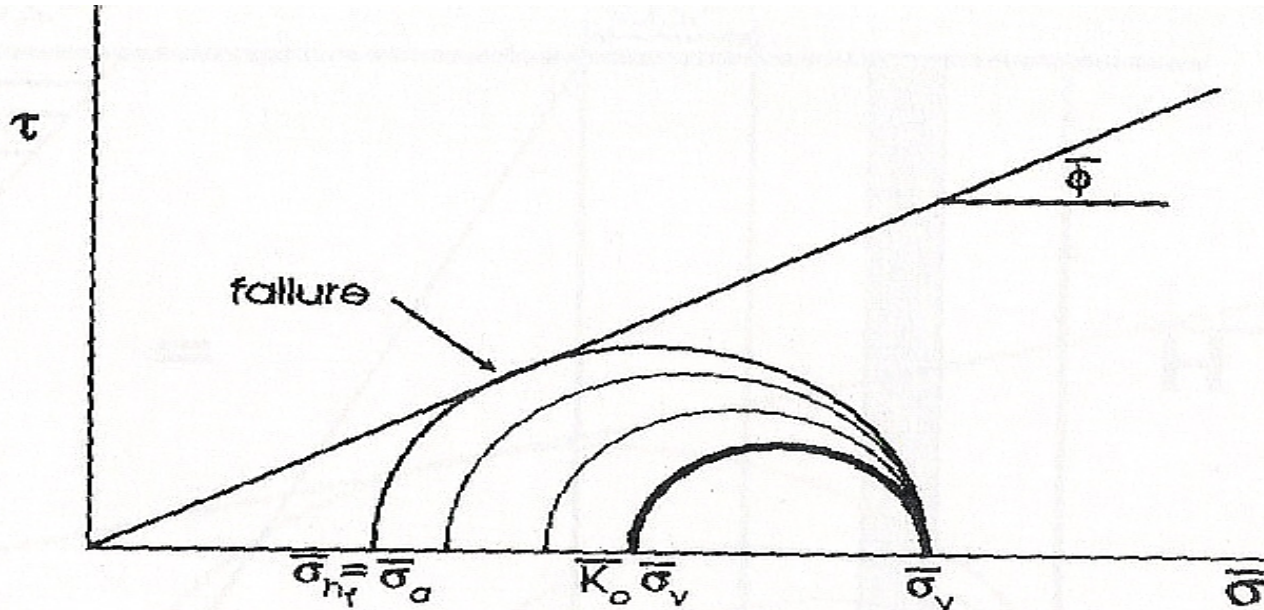
$$k_p = \tan^2(45 + \phi/2) = 1/k_a$$

At Rest Lateral Earth Pressures



The pressure maintained when no movement or relief occurs

At Rest Earth Pressure



$$\sigma_h = \sigma_v k_0 = \gamma z k_0$$

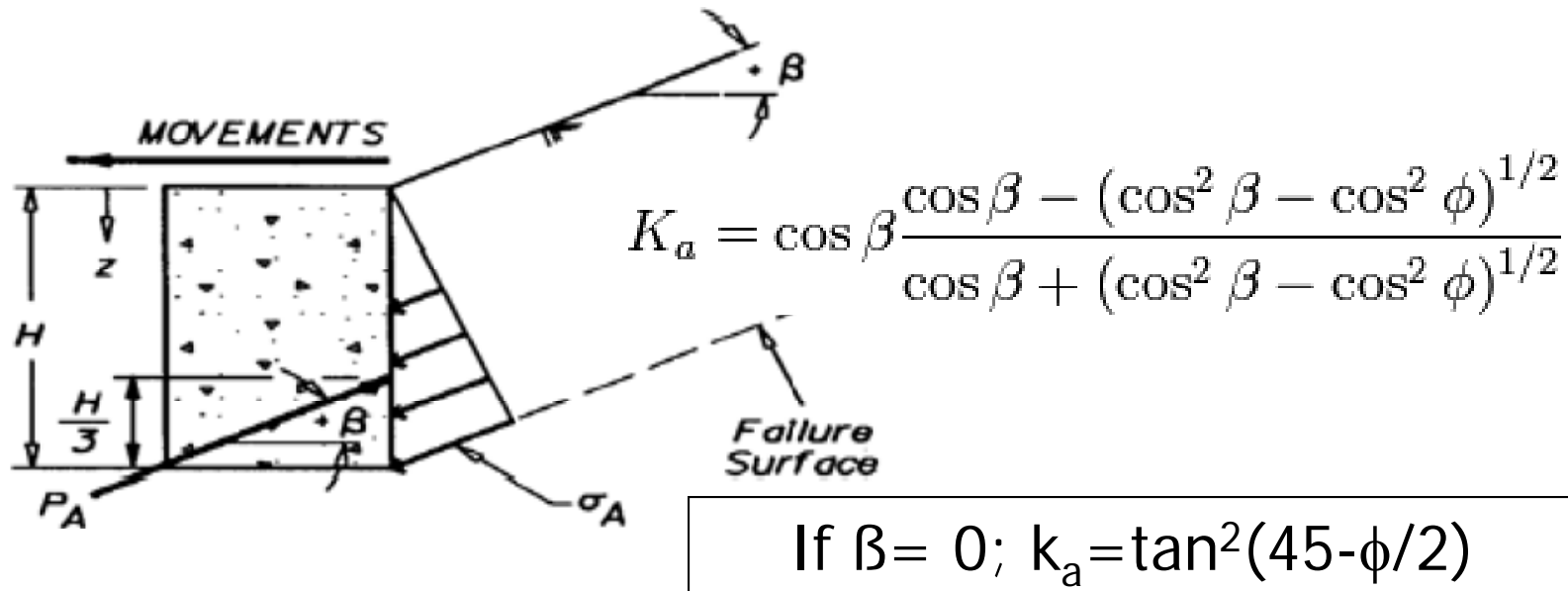
strain in elastic zone; stress at equilibrium (not in failure)

$$k_0 = \mu / (1 - \mu) \text{ where } \mu = \text{Poisson's ratio}$$

$$\text{or } k_0 = 1 - \sin \phi$$

(for sand and normally consolidated clay)

Rankine Analysis



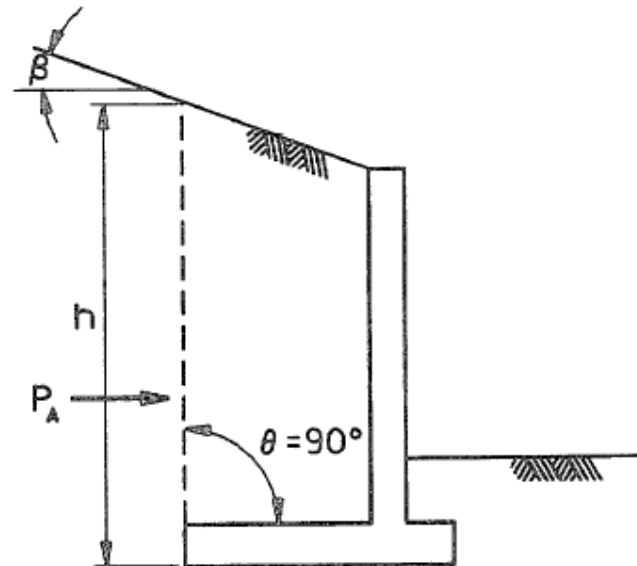
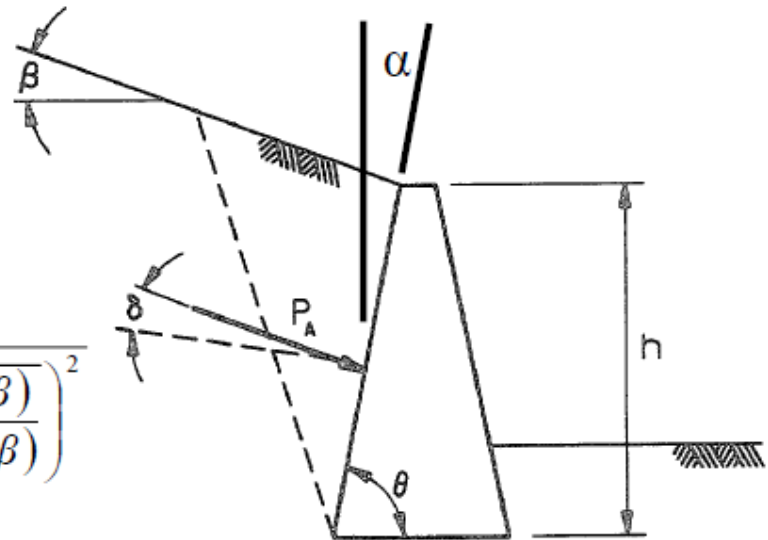
$$K_p = \cos \beta \frac{\cos \beta + (\cos^2 \beta - \cos^2 \phi)^{1/2}}{\cos \beta - (\cos^2 \beta - \cos^2 \phi)^{1/2}}$$

Coulomb Theory

$$K_a = \frac{\cos^2(\varphi - \alpha)}{\cos^2\alpha \cos(\delta + \alpha) \left(1 + \sqrt{\frac{\sin(\varphi + \delta)\sin(\varphi - \beta)}{\cos(\delta + \alpha)\cos(\alpha - \beta)}} \right)^2}$$

$$K_p = \frac{\cos^2(\varphi + \alpha)}{\cos^2\alpha \cos(\delta - \alpha) \left(1 - \sqrt{\frac{\sin(\varphi + \alpha)\sin(\varphi + \beta)}{\cos(\delta - \alpha)\cos(\beta - \alpha)}} \right)^2}$$

- Includes wall friction
- Passive earth coefficients can be UNCONSERVATIVE (too high)



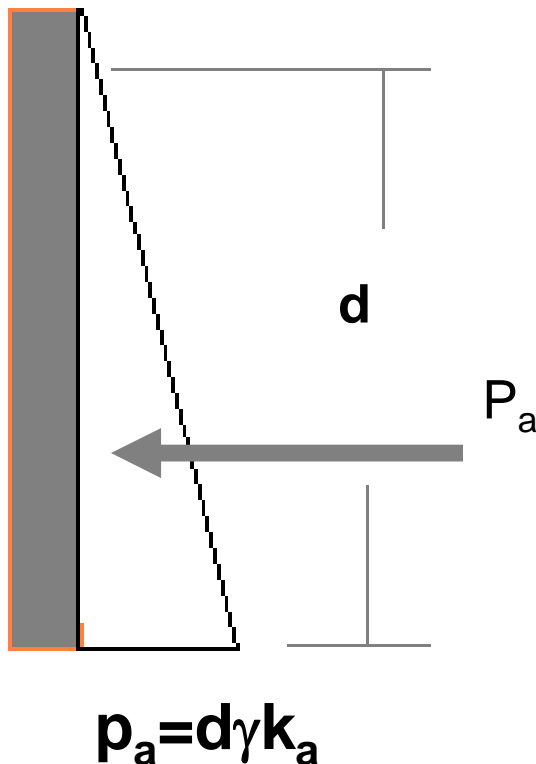
Active Lateral Earth Pressure

$$p_a = d \gamma k_a$$

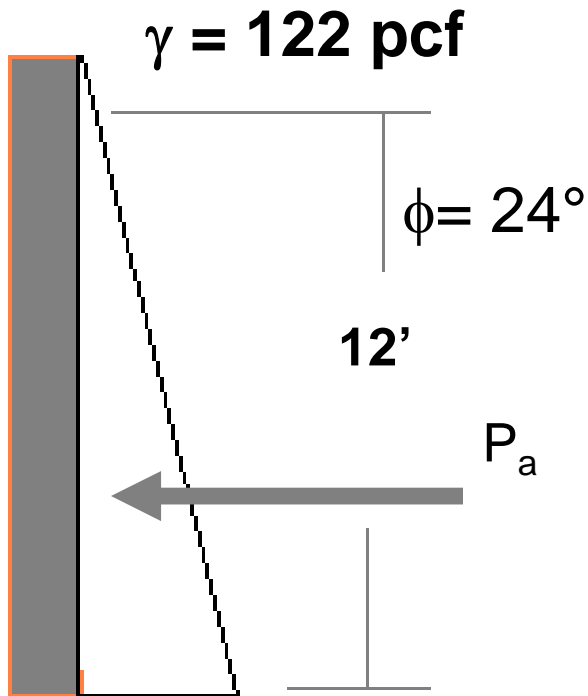
$$k_a = \tan^2(45 - \phi/2)$$

$$p_a = d \gamma \tan^2(45 - \phi/2)$$

$$P_a = 1/2 d p_a = \gamma k_a d^2 / 2$$

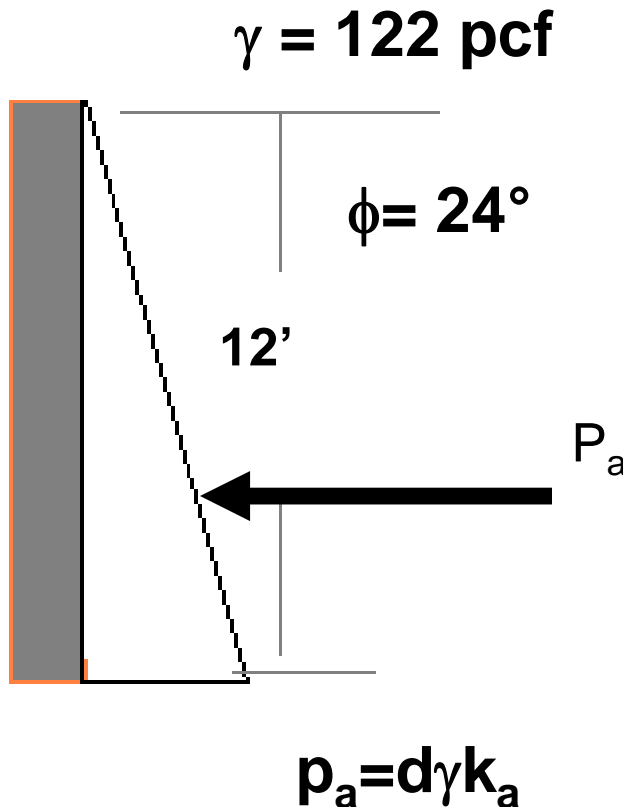


Calculate Active Pressure Total Force per Foot of Wall



- A) 3690 pounds
- B) 615 pounds/ft²
- C) 307 pounds

Calculate Active Pressure Total Force per Foot of Wall



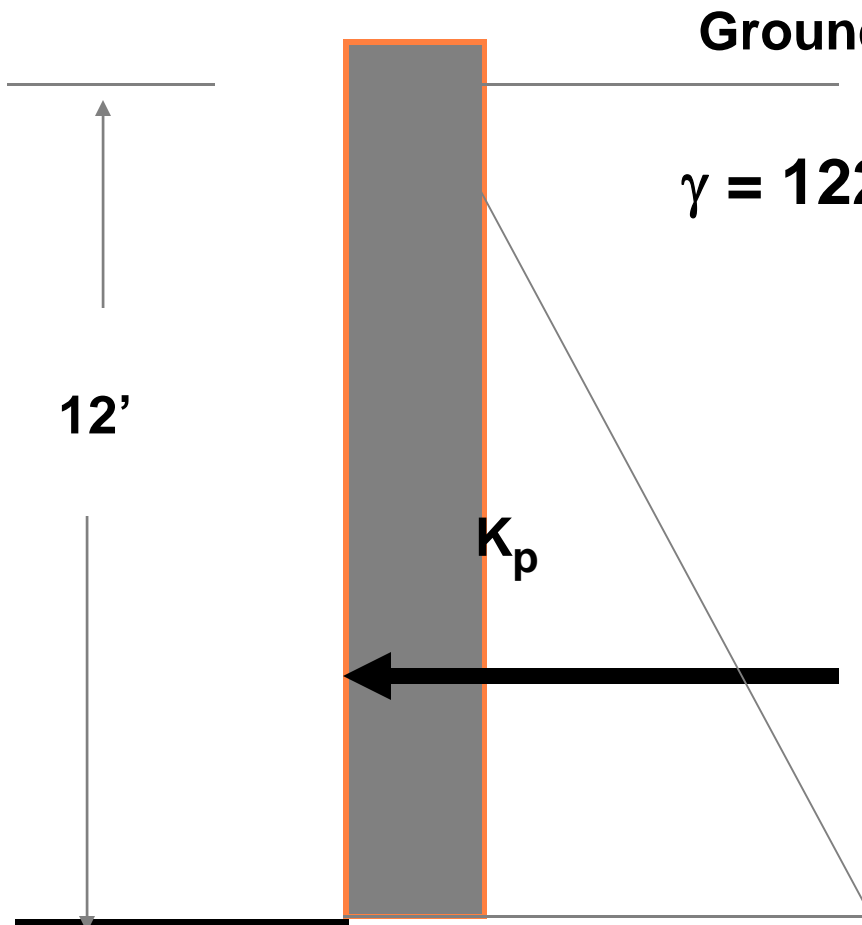
$$k_a = \tan^2(45 - 24/2) = 0.42$$

$$p_a = 12 \times 122 \times 0.42$$
$$= 615 \text{ psf}$$

$$P_a = 122(0.42)12^2/2$$
$$= 3689 \text{ pounds force}$$

Answer is "A"

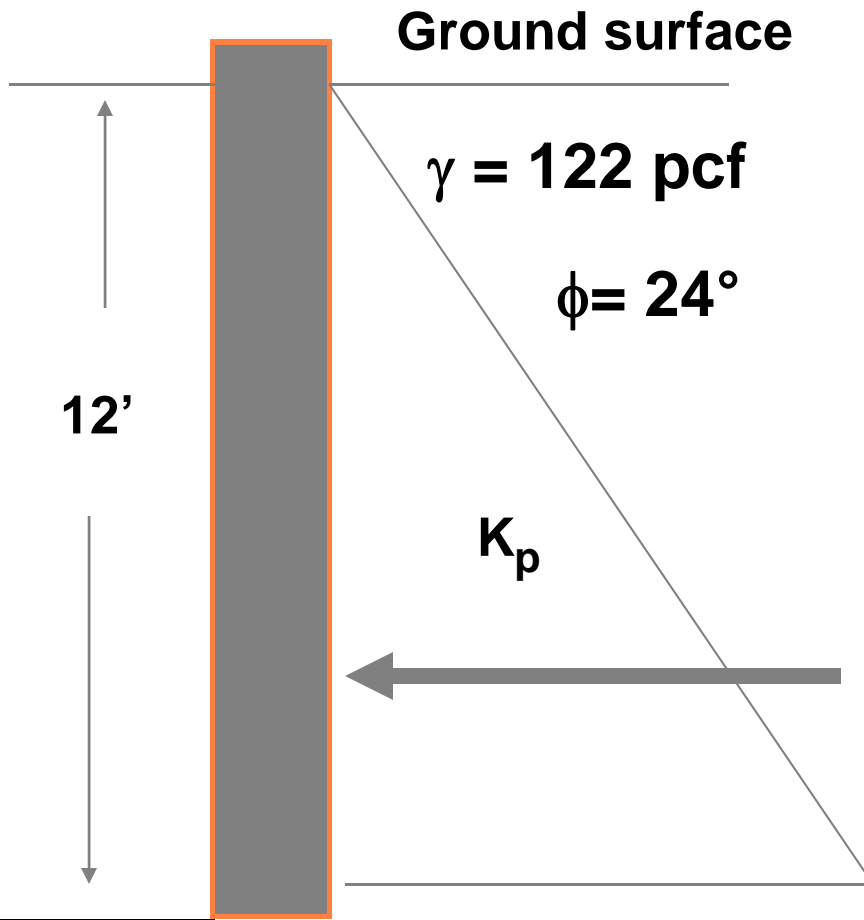
Calculate Total Force Due to Passive Earth Pressure



$$\phi = 24^\circ$$

- A) 2,800 pounds force
- B) 3,470 pounds force
- C) 20,818 pounds force

Calculate Total Force Due to Passive Earth Pressure



$$\gamma = 122 \text{ pcf}$$

$$\phi = 24^\circ$$

$$k_p = \tan^2(45 + 24/2) = 2.37$$

$$p_p = 12 \times 122 \times 2.37$$
$$= 3470 \text{ psf}$$

$$P_a = 122(2.37)12^2/2$$
$$= 20,818 \text{ pounds force}$$

Answer is "C"

C-φ Soils Lateral Earth Pressure

Active Case

Cohesionless

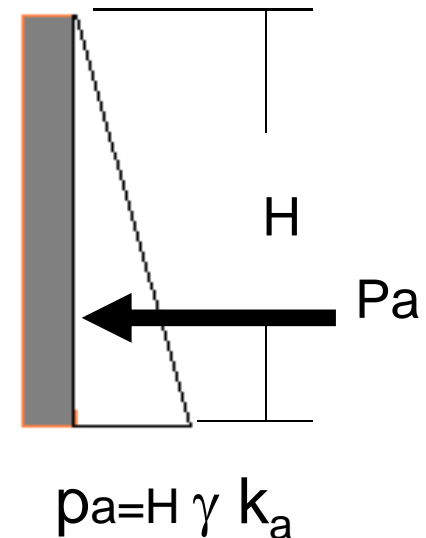
$$p_a = H \gamma \tan^2(45 - \phi/2)$$

For C & φ Soils

$$p_a = H \gamma \tan^2(45 - \phi/2) - 2C \tan(45 - \phi/2)$$

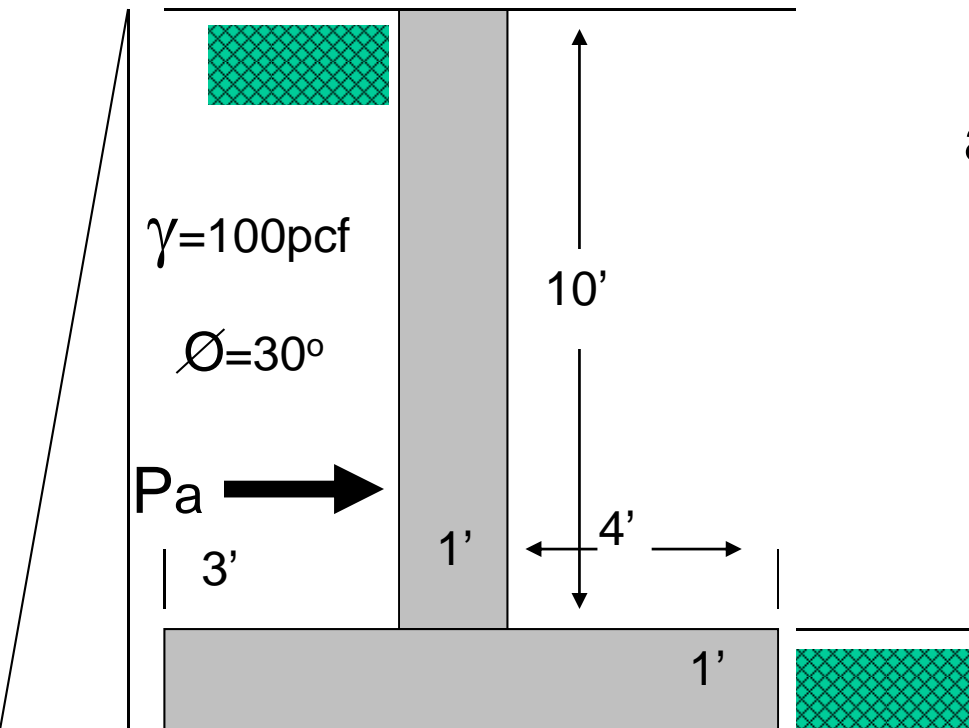
$$P_a = 1/2 H^2 \gamma \tan^2(45 - \phi/2) - 2C H \tan(45 - \phi/2)$$

$$P_a = \sigma_h = K_a \sigma_v - 2c \sqrt{K_a}$$



For Passive case change
negative signs to positive

Lateral Earth Pressures



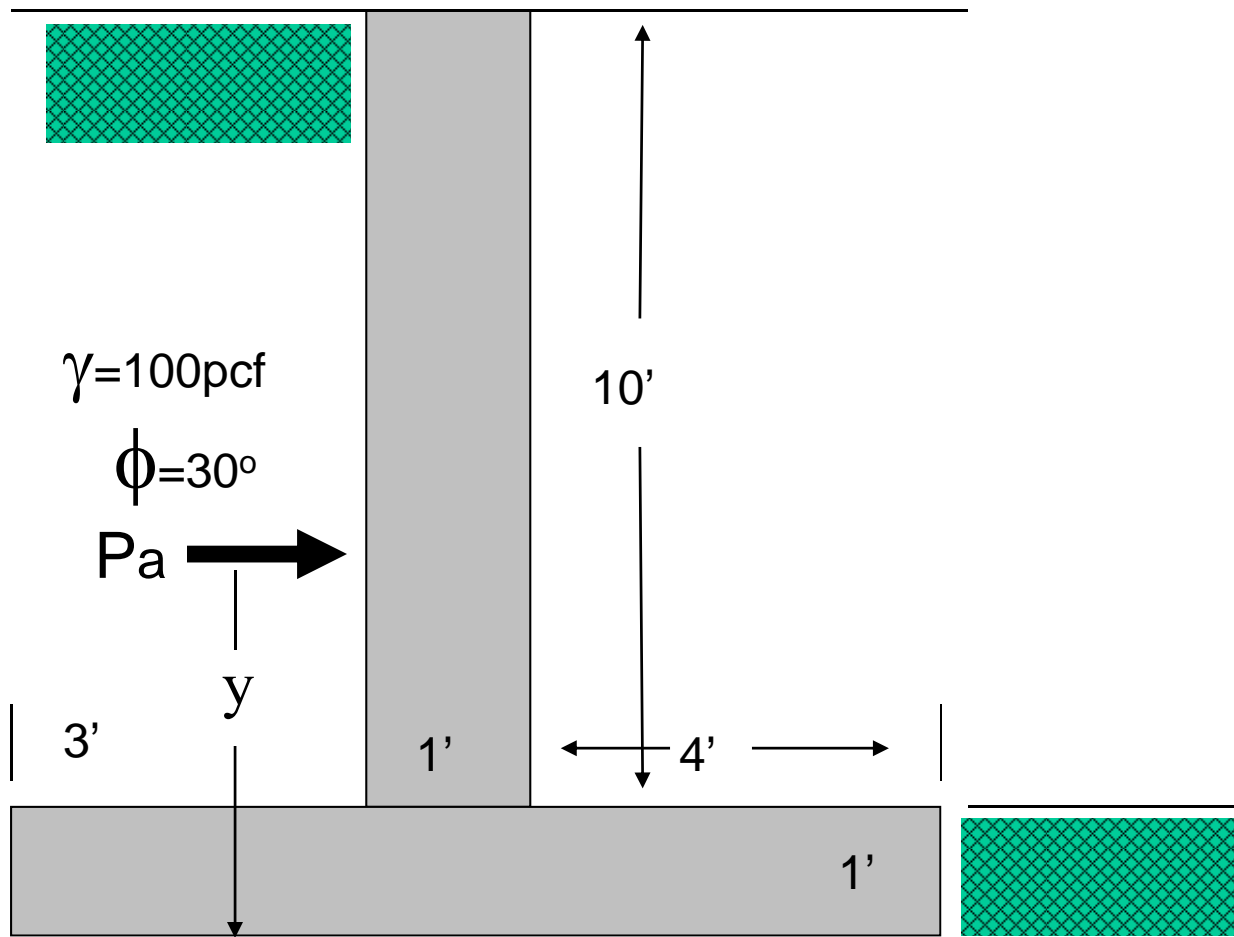
$$\text{active coefficient} = k_a = \tan^2(45 - \phi/2)$$

$$\text{or } \frac{1 - \sin \phi}{1 + \sin \phi} = 0.33$$

max pressure at base of wall

$$p = \gamma K_a H = 100(0.33)11 = 363 \text{ psf}$$

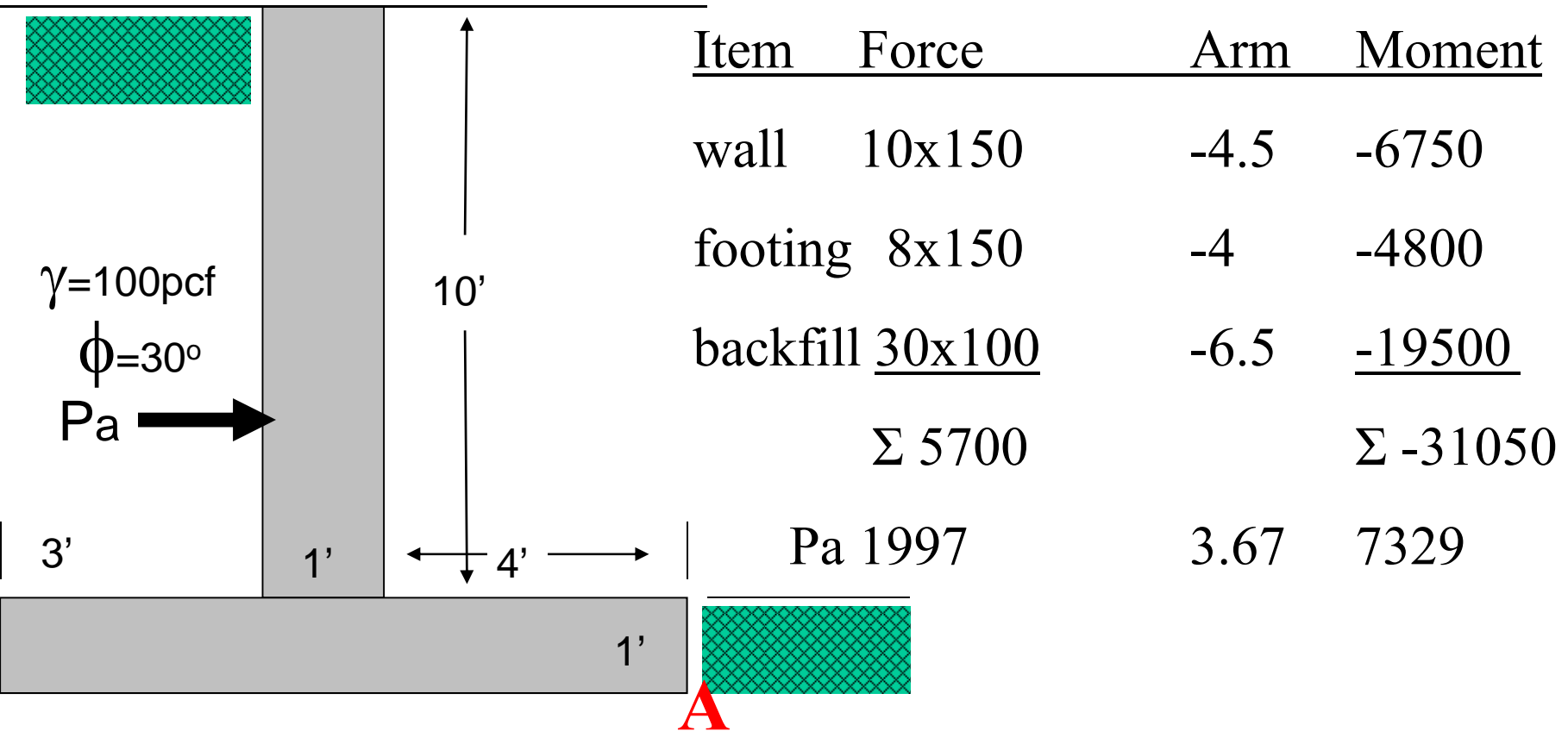
$$\begin{aligned}
 P_a = \text{Resultant Force} &= \frac{1}{2} K_a \gamma H^2 = \frac{1}{2} \gamma K_a H(H) \\
 &= \frac{1}{2} 363(11) = 1997 \text{ pounds/ft}
 \end{aligned}$$



Moment due to force acts at $\frac{1}{3}$ wall height

$$y = \frac{10}{3} = 3.67' \quad P_a y = 3.67(1997) = 7329 \text{ ft-lbs/ft}$$

Overturning- Take Moments About “A”



$$\text{Overturning FS} = \text{Resisting/Driving} = 31050/7329 = 4.2$$

Sliding Resisting Forces:

Base Friction + Passive Pressure at toe

Passive Pressure at toe

$$P_p = \frac{1}{2} K_p \gamma H^2 = \frac{1}{2} \times 3 \times 100 \times 1$$

$$P_p = 150 \text{ plf}$$

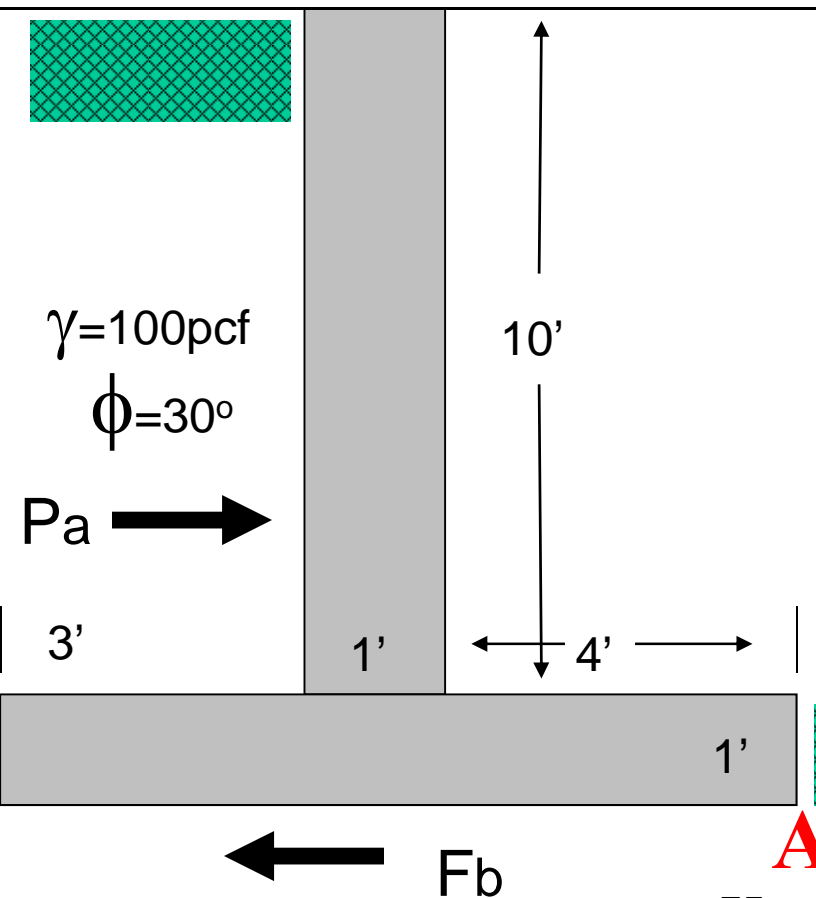
acts at 1/3' above base

Bottom Friction = $F_b = \text{weight} \times \tan \frac{2}{3}\phi$

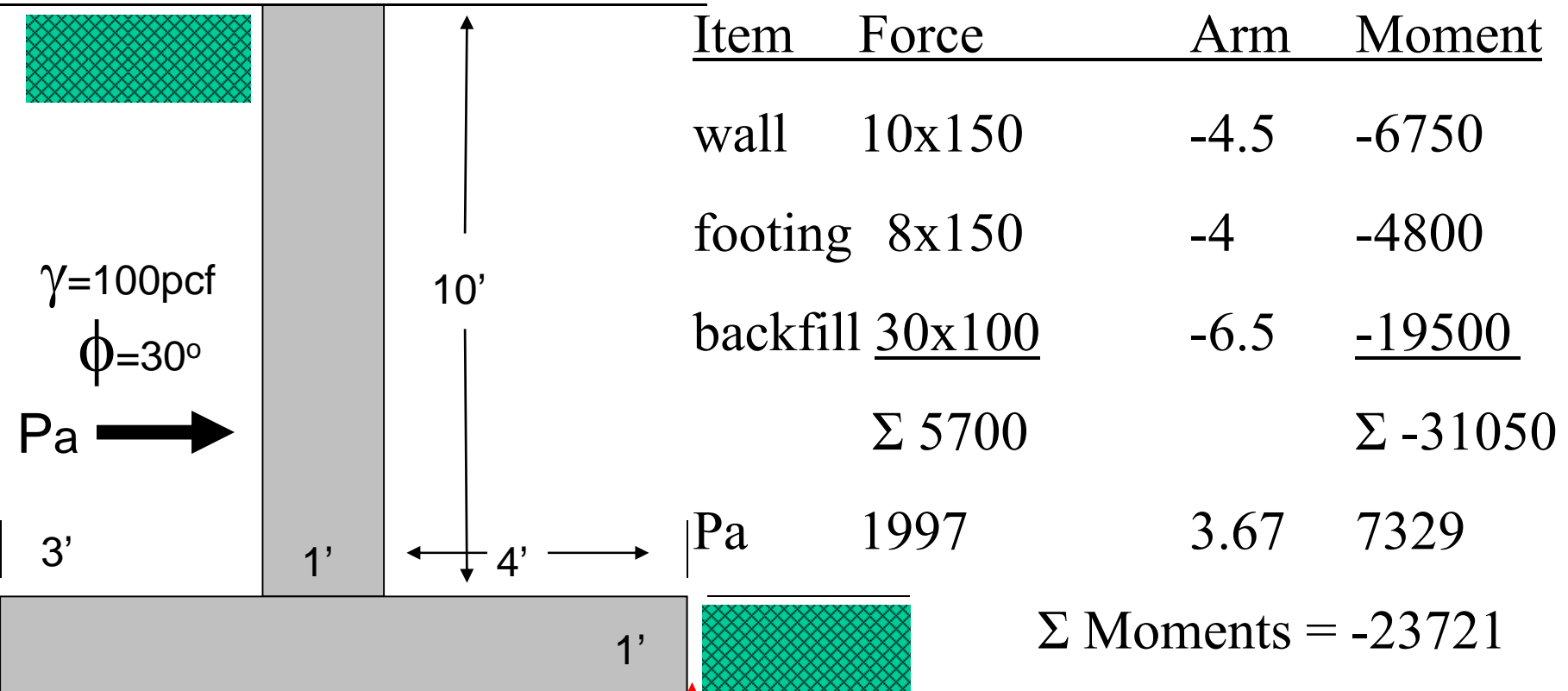
$$K_p = \tan^2 (45 + \phi/2) = \tan^2 (45 + 30/2) = 3$$

$$F_b = 5700 \tan (2/3)30 = 2075$$

$$\text{Sliding FS} = \text{Resisting/Driving} = (2075 + 150) / 1997 = 1.1$$



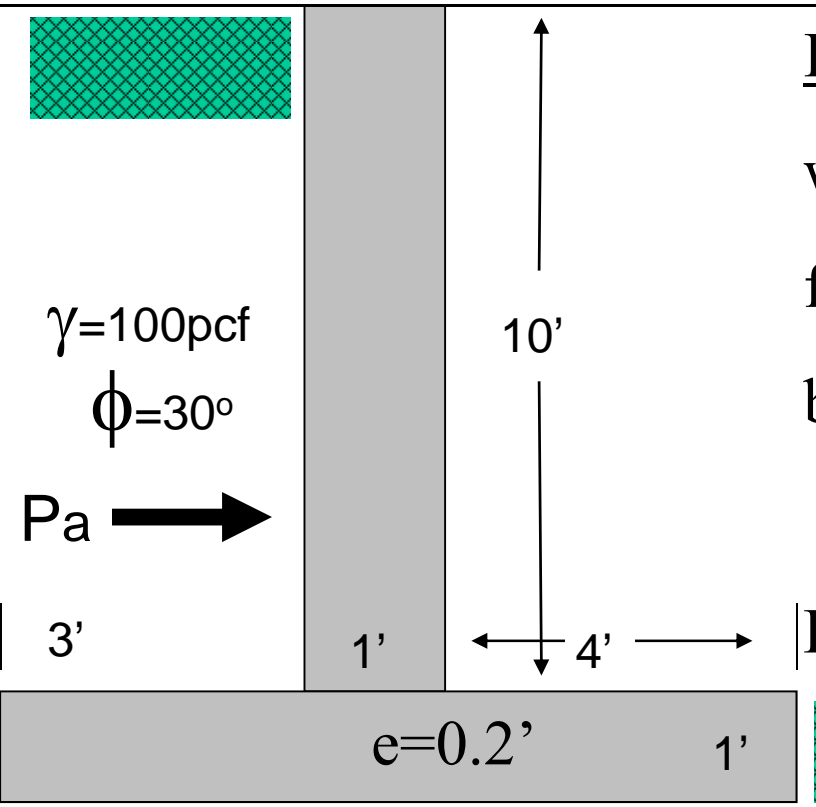
Calculate Eccentricity



Distance to Resultant X-axis: (Σ moments/resisting force)

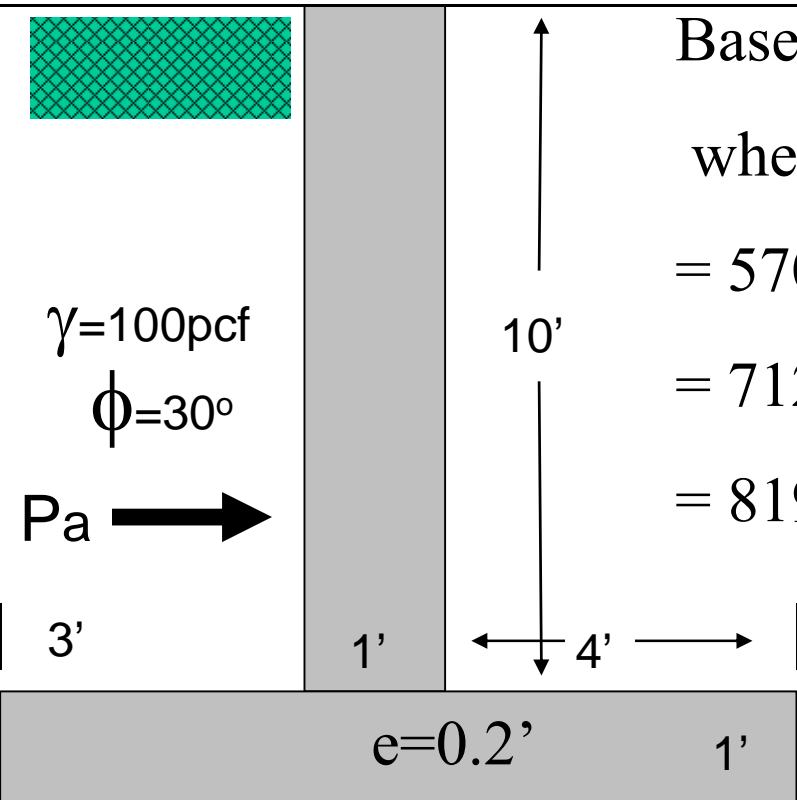
$$\Sigma M / \Sigma V = 23721 / 5700 = \underline{4.2'} \text{ from point A}$$

Middle 1/3 = 2.7 to 5.3, eccentricity = $e = 4 - 4.2 = 0.2'$ beyond middle



Item	Force	Arm	Moment
wall	10x150	-4.5	-6750 \curvearrowright
footing	8x150	-4	-4800 \curvearrowright
backfill	<u>30x100</u>	-6.5	<u>-19500</u> \curvearrowright
	Σ 5700		Σ -31050 \curvearrowright
P_a	1997	3.67	7329 \curvearrowright
			Σ Moments = -23721 \curvearrowright

Base Pressure = $P/A \pm Mc/I$; or $P/A \pm Pec/I$; where $I = bh^3/12$
 $= 5700/8 \pm (5700 \times 0.2 \times 4)/(1/12 \times 1 \times 8^3) = 712.5 \pm 106.9$
 $= 819.4$ (heel) & 605.6 (toe) heel increases due to \curvearrowright moment sum



$$\text{Base Pressure} = P/A \pm Mc/I$$

$$\text{where } I = bh^3/12$$

$$= 5700/8 \pm (5700 \times 0.2 \times 4)/(1/12 \times 1 \times 8^3)$$

$$= 712.5 \pm 106.9$$

$$= 819.4 \text{ psf (heel) \& } 605.6 \text{ psf (toe)}$$

or

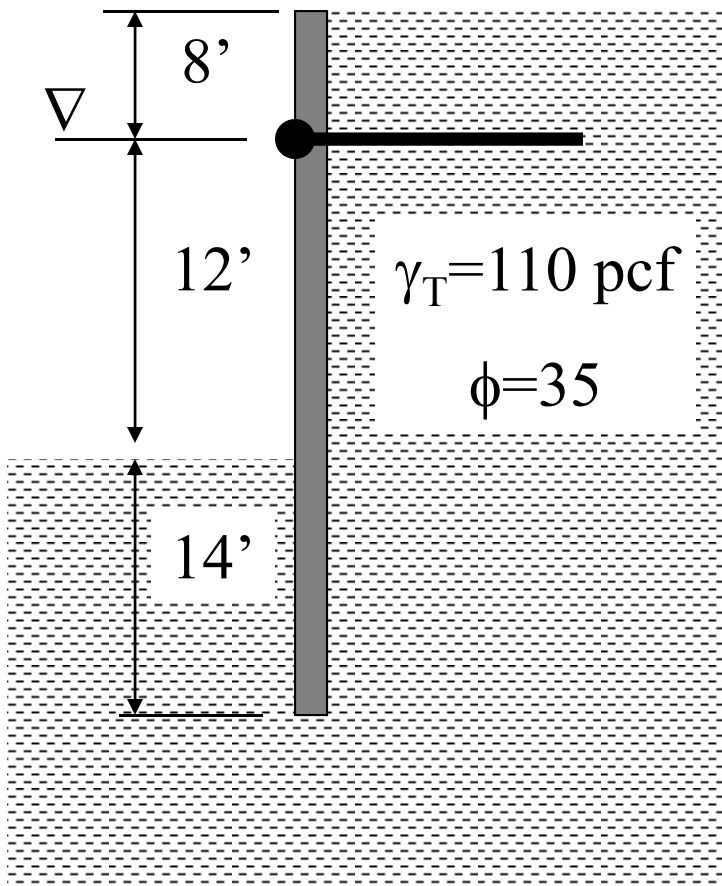
$$\text{X-axis reaction} = P/B(1 \pm 6e/B)$$

$$= 5700 / 8 (1 + 6 \times 0.2 / 8)$$

$$= 819.4 \text{ psf (heel)}$$

Anchored Bulkhead

free earth method



$$K_a = \tan^2 (45 - \phi / 2) = 0.27$$

$$K_p = \tan^2 (45 + \phi / 2) = 3.7$$

$$\text{Active Pressure} = \gamma K_a H$$

at anchor

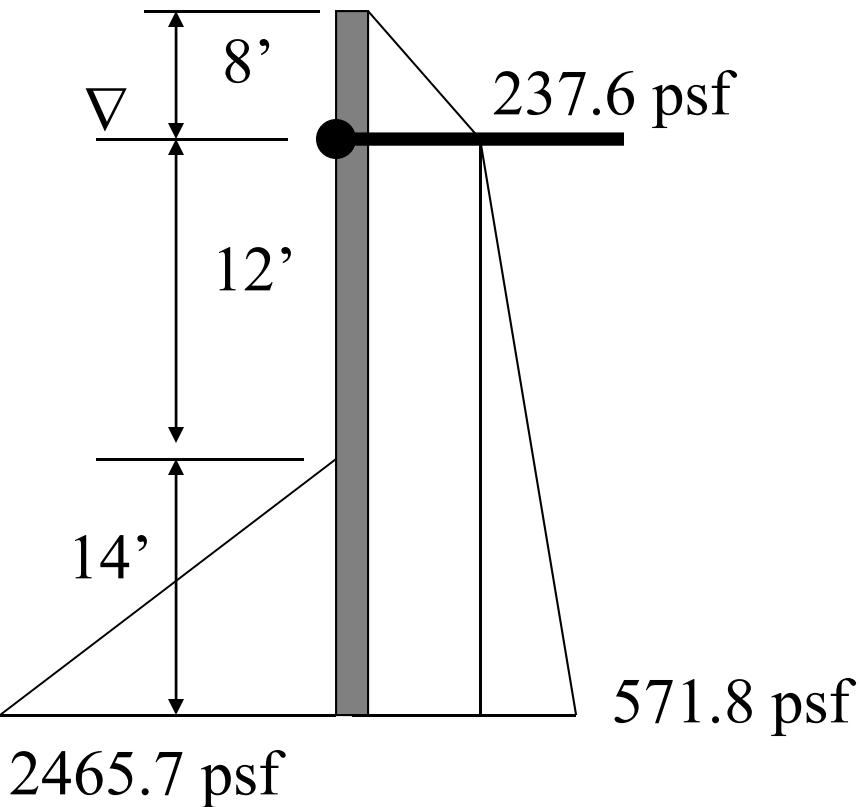
$$= 110 (0.27) 8 = 237.6 \text{ psf per linear foot}$$

at base of bulkhead

$$= 237.6 + (110 - 62.4) 0.27 (26) = 571.8 \text{ psf}$$

per linear foot of wall

Anchored Bulkhead



$$K_p = \tan^2 (45 + 35 / 2) = 3.7$$

$$\text{Passive Pressure} = \gamma K_p H$$

below dredge line

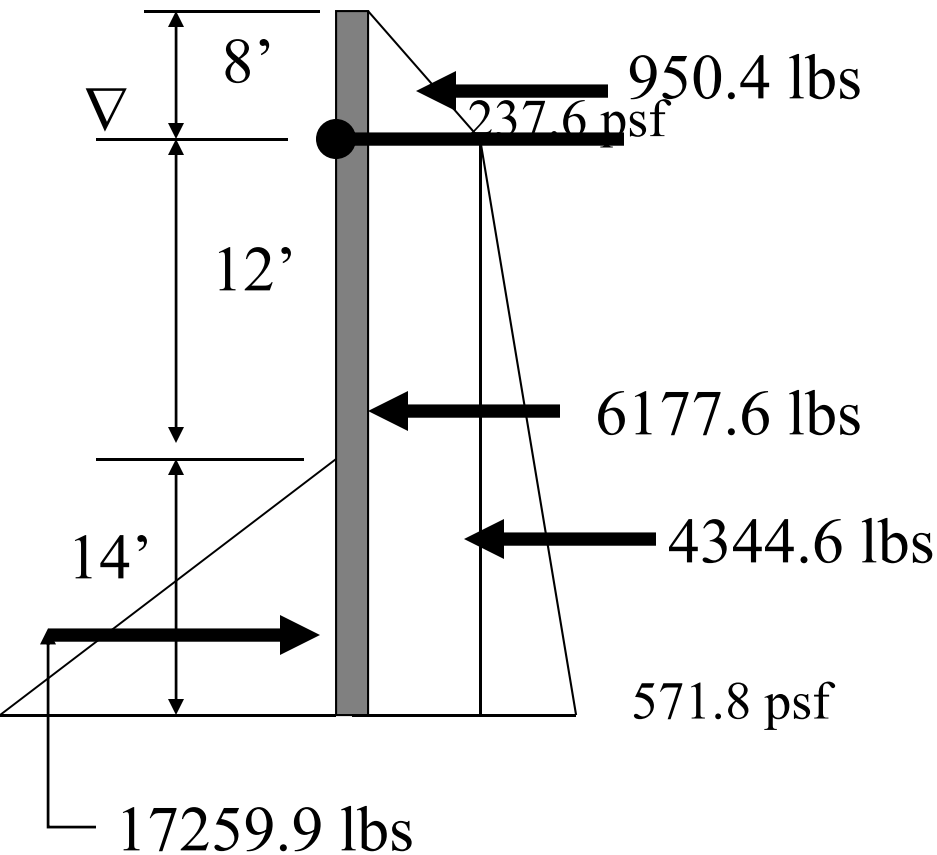
$$= (110 - 62.4) 3.7 (14) = 2465.7 \text{ psf}$$

$$\text{Lateral Passive Force} = 1/2 \gamma K_p H^2$$

$$= 1/2 (2465.7) 14 = 17259.9 \text{ lbs/ft}$$

Toe Failure Factor of Safety?

At toe failure, bulkhead will rotate about the anchor



Lateral Active Forces:

(Linearly Increasing)

$$= 1/2 \gamma K_a H^2$$

$$= 1/2 (237.6)8 = 950.4 \text{ lbs/ft}$$

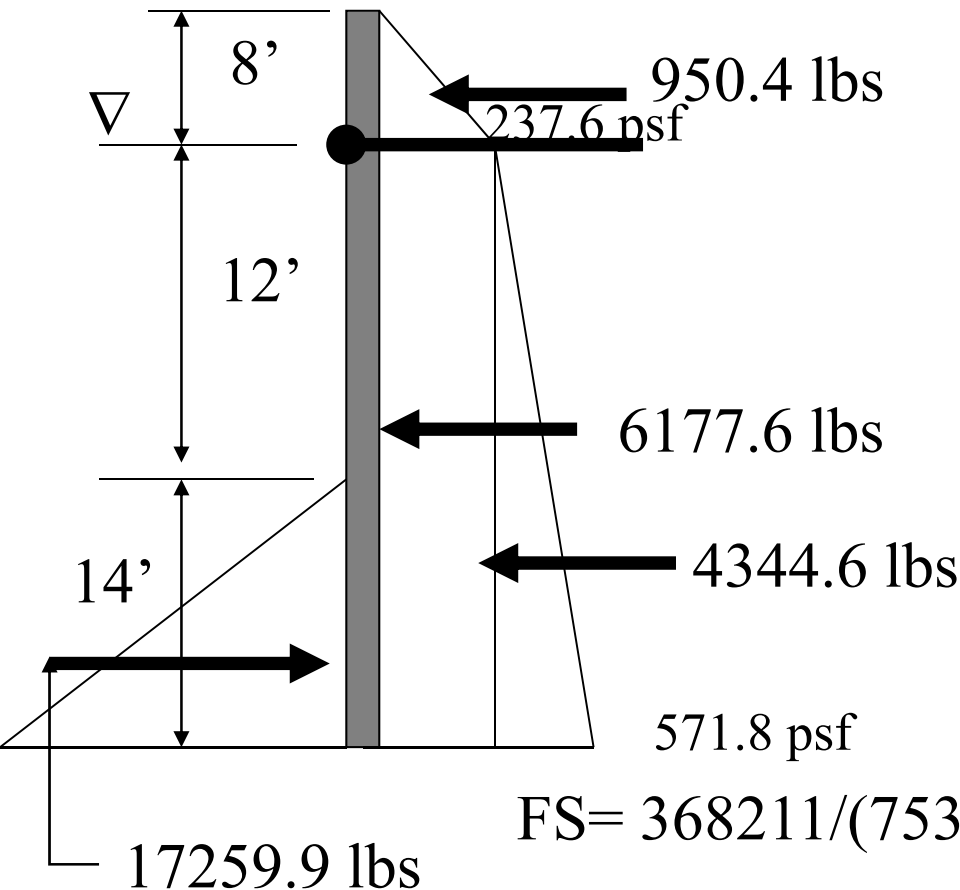
$$= 1/2 (571.8-237.6)26 = 4344.6 \text{ lbs}$$

(Uniform Forces)

$$237.6(26) = 6177.6 \text{ lbs}$$

Toe Failure Factor of Safety?

At toe failure, bulkhead will rotate about the anchor ?



$$FS = \frac{\text{Resisting Moments}}{\text{Driving Moments}}$$

Driving Forces:

$$950.4 \times 8/3 = -2534.4 \text{ ft-lbs}$$

$$6177.6 \times 26/2 = 80308.8 \text{ ft-lbs}$$

$$4344.6 \times (2/3)26 = 75306.4 \text{ ft-lbs}$$

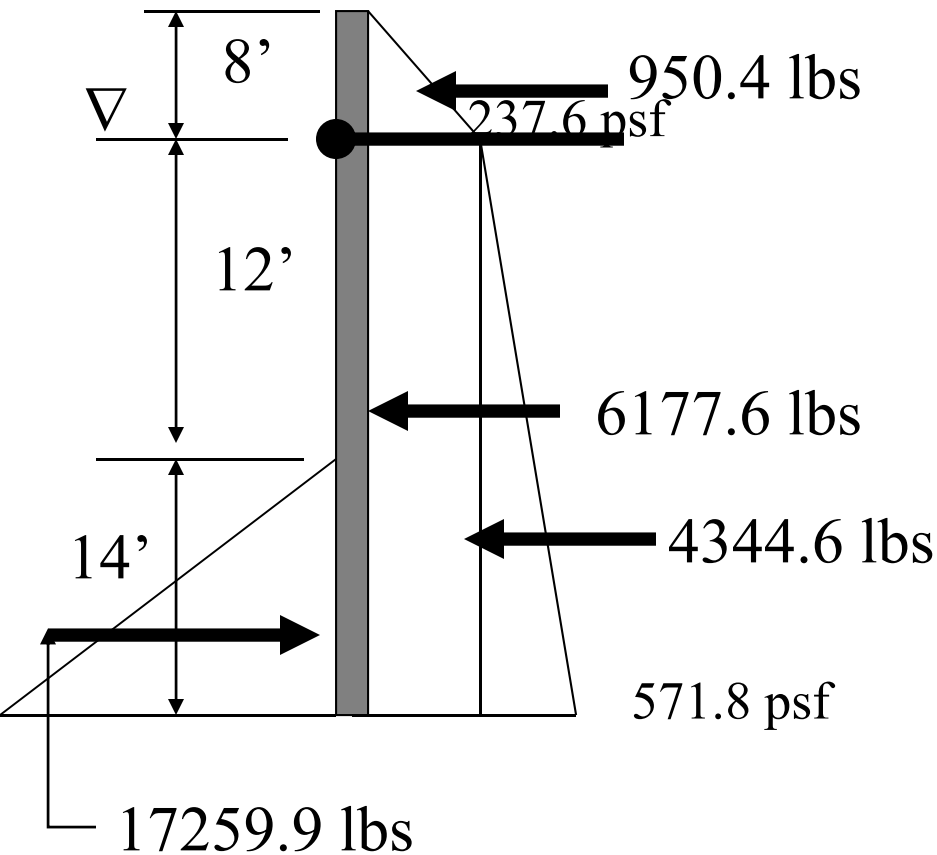
Resisting Forces:

$$17259.9[12 + 14(2/3)] = 368211 \text{ ft-lbs}$$

$$FS = 368211 / (75306.4 + 80308.8 - 2534.4) = 2.4$$

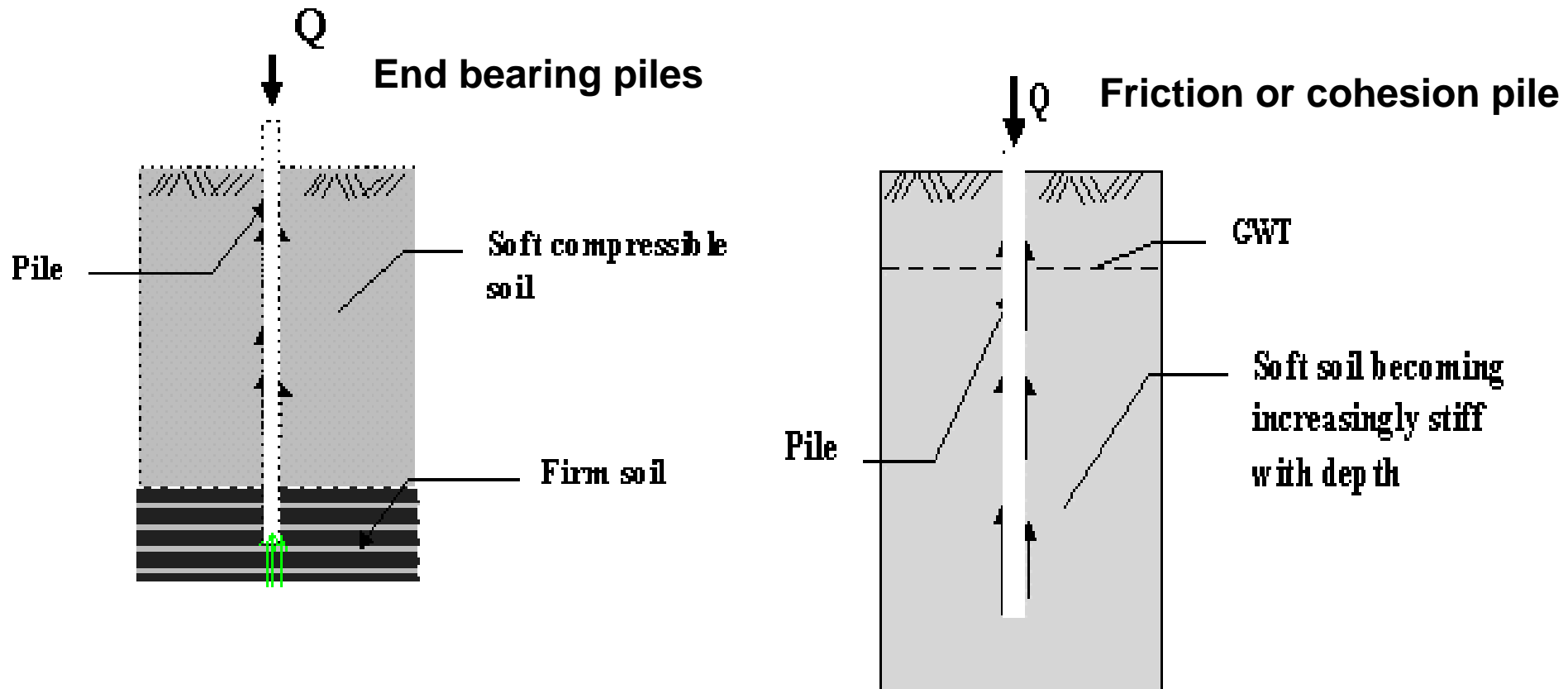
What Force in Anchor for FS = 3?

Sum horizontal forces



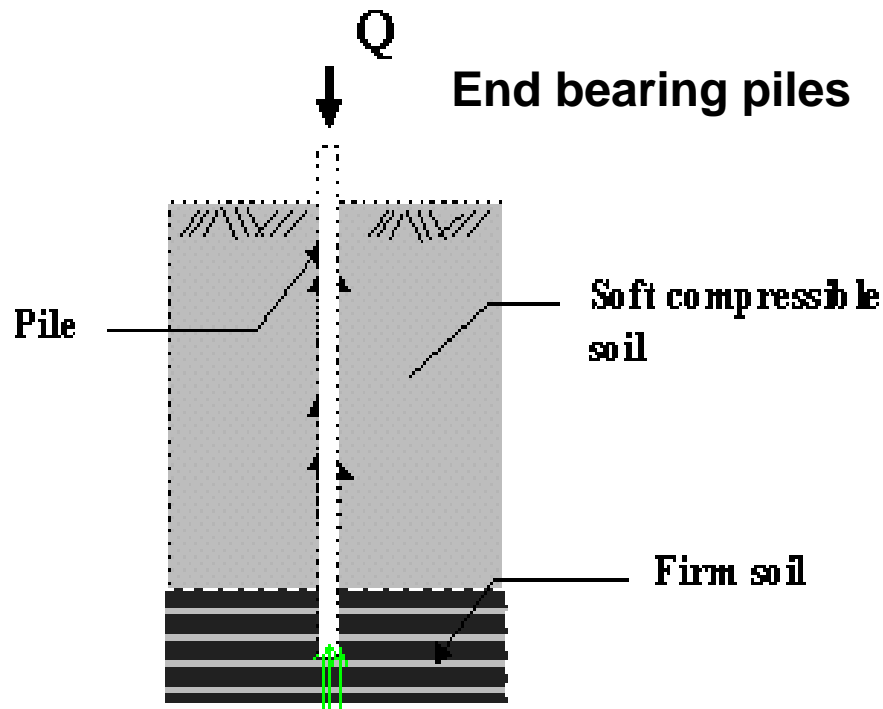
$$\begin{aligned}
 T &= \Sigma P_a - \Sigma P_p / 3 \\
 &= 950.4 + 6177.6 + 4344.6 - 17259.9 / 3 \\
 &= 5719.3 \text{ lbs/ft of wall} \\
 &\text{if anchors at 5' OC} \\
 &\text{Force per anchor} = 28,597 \text{ lbs}
 \end{aligned}$$

Pile Capacity



Friction (Side Shear) + End Bearing

Pile Capacity



A_T = Tip Area (B^2 or πR^2)

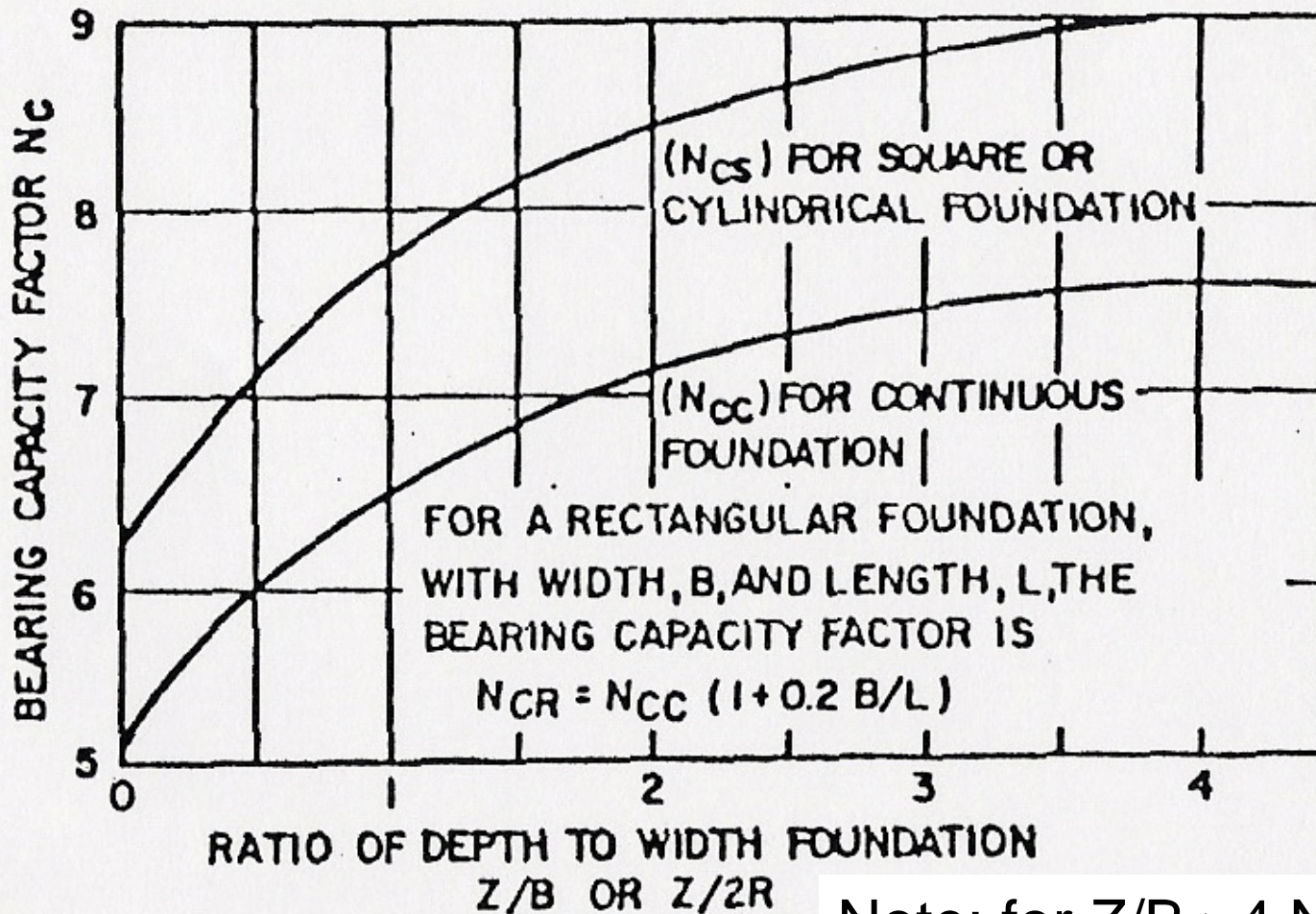
C = cohesion

q = overburden pressure

N_c & N_q Deep Bearing Factors

$$\text{Tip capacity} = A_T (c N_c + q N_q)$$

Pile End Bearing Factors Cohesive Soil



Note: for $Z/B > 4$ $N_c = 9$

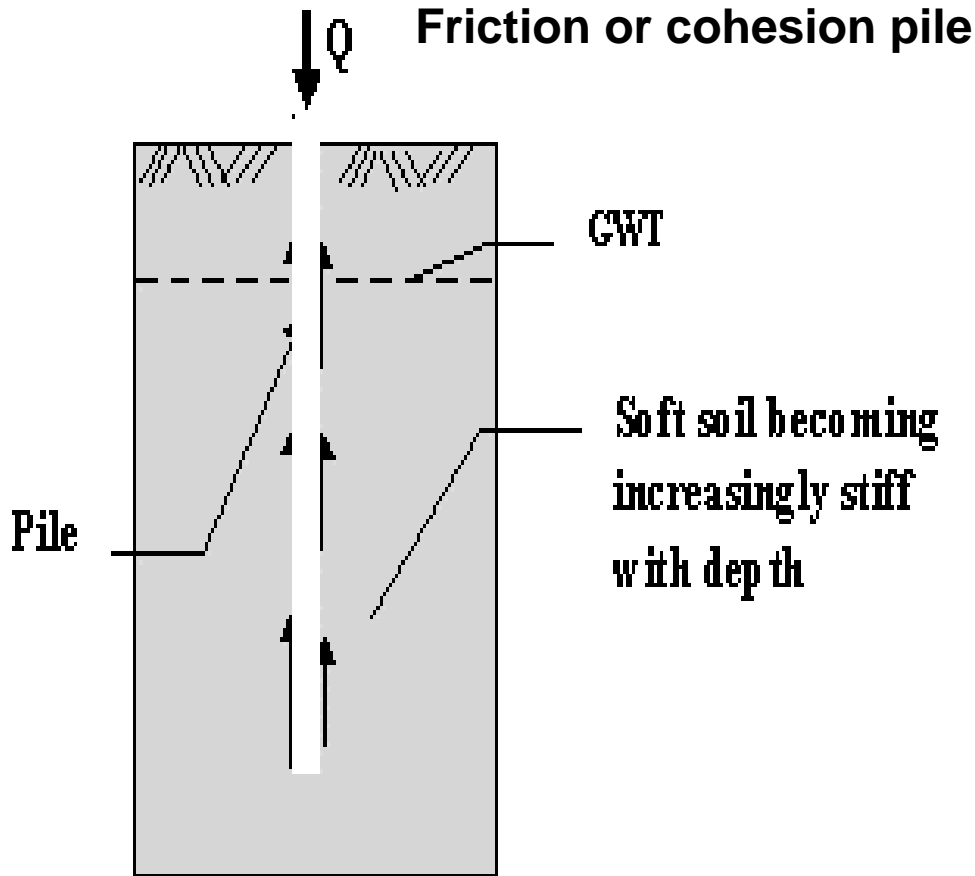
Pile End Bearing Factors Cohesionless Soil

BEARING CAPACITY FACTORS - N_q

ϕ^* (DEGREES)	26	28	30	31	32	33	34	35	36	37	38	39	40
N_q (DRIVEN PILE DISPLACEMENT)	10	15	21	24	29	35	42	50	62	77	86	120	145
N_q^{**} (DRILLED PIERS)	5	8	10	12	14	17	21	25	30	38	43	60	72

* & ** limit ϕ to 28 if jetting or bailer used

Pile Capacity



C = Cohesion

α = adhesion/cohesion ratio

d = pile diameter

L = pile length

K = earth pressure coefficients

P = overburden pressure

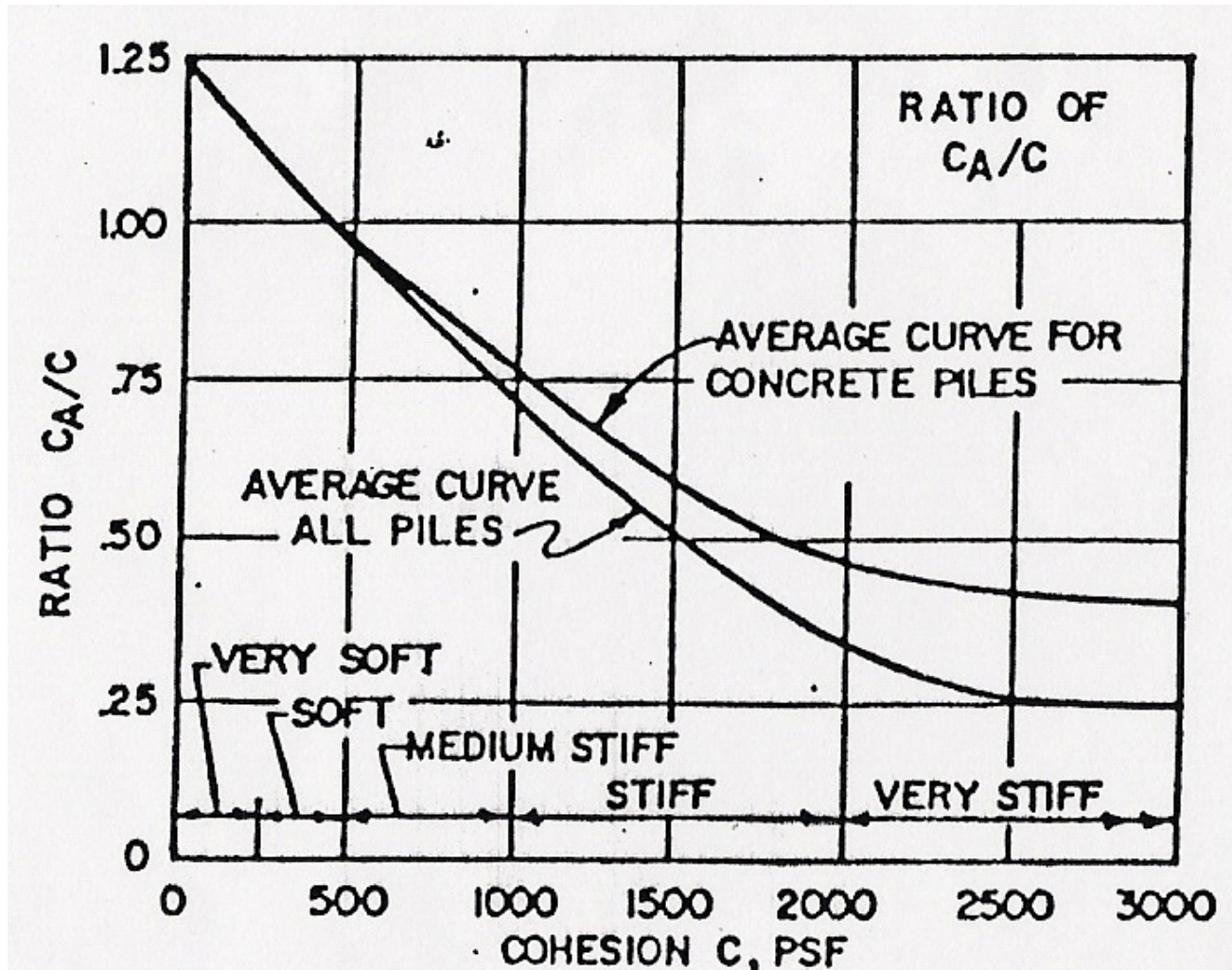
δ = pile material friction angle

Side Shear

= adhesion + friction

$$= C \alpha \pi dL + KP \tan \delta \pi dL$$

Adhesion to Cohesion Ratio



Pile Earth Pressure Coefficients

EARTH PRESSURE COEFFICIENTS K_{HC} AND K_{HT}

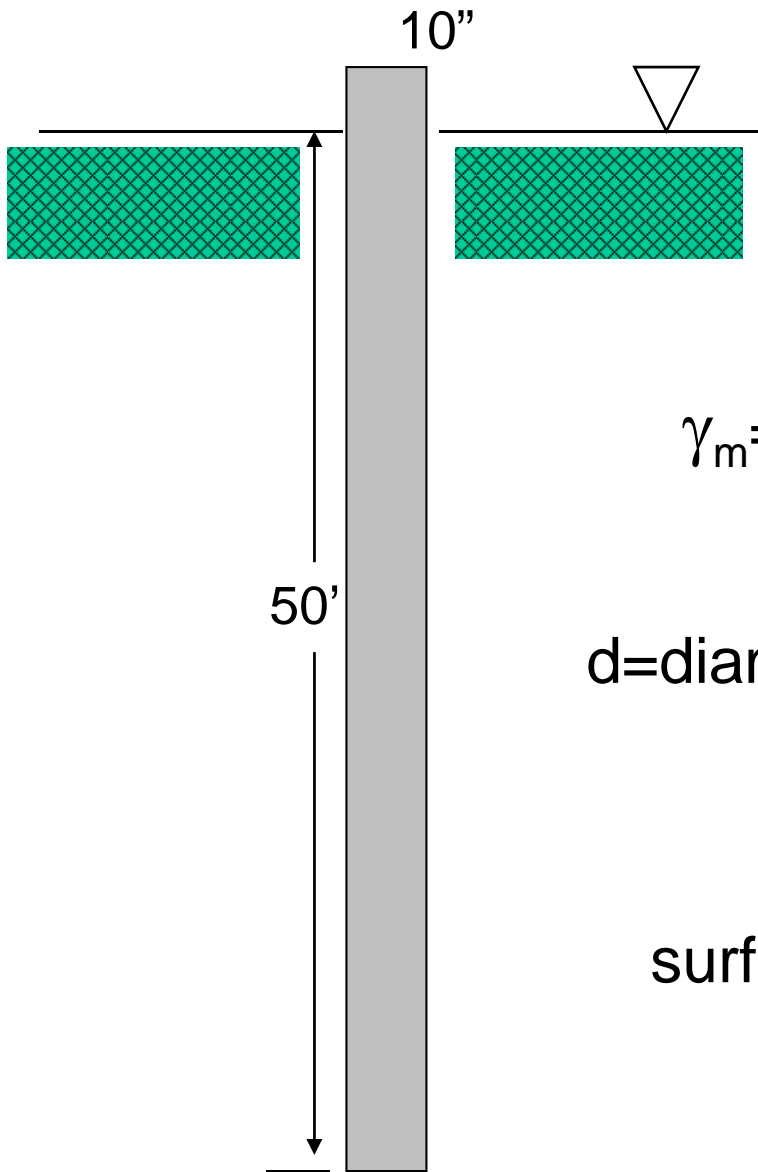
PILE TYPE	K_{HC}	K_{HT} <i>Tension</i>
DRIVEN SINGLE H-PILE	0.5 - 1.0	0.3 - 0.5
DRIVEN SINGLE DISPLACEMENT PILE	1.0 - 1.5	0.6 - 1.0
DRIVEN SINGLE DISPLACEMENT TAPERED PILE	1.5 - 2.0	1.0 - 1.3
DRIVEN JETTED PILE	0.4 - 0.9	0.3 - 0.6
DRILLED PILE (LESS THAN 24" DIAMETER)	0.7	0.4

Pile Material Friction Angle

FRICITION ANGLE - δ

PILE TYPE	δ
STEEL	20°
CONCRETE	$3/4 \phi$
TIMBER	$3/4 \phi$

Pile Capacity - Clay



10" diameter concrete pile

$$q_u = 2800 \text{ psf} ; c = 1400 \text{ psf}$$

$$\gamma_m = 120 \text{ pcf}$$

$$\phi = 0$$

$$d = \text{diameter} = \frac{10''}{12} = 0.83' \quad \text{End Area} = \frac{\pi 0.83^2}{4}$$

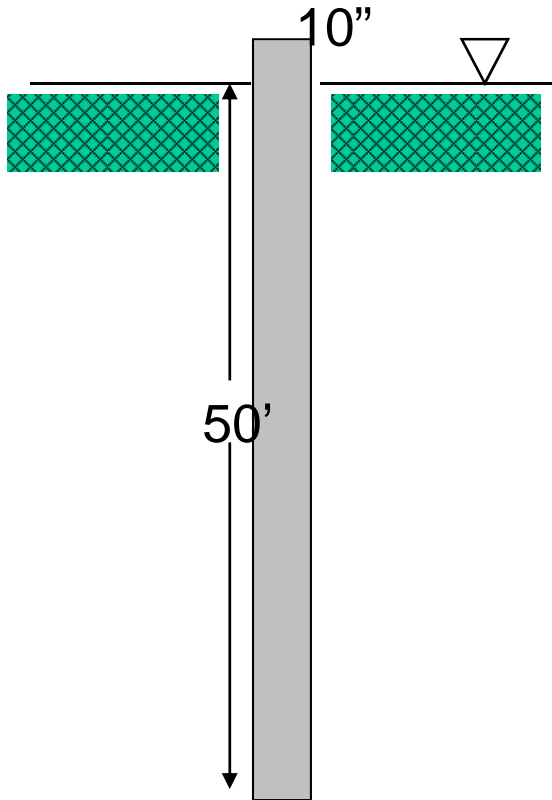
$$A = 0.54 \text{ ft}^2$$

$$\text{surface area} = \pi d L = \pi 0.83 \times 50 = 130.4 \text{ ft}^2$$

Pile Capacity - Clay

concrete driven pile;

$$C=1400 \text{ psf} \quad \alpha \cong 0.6$$



$$\text{Tip capacity} = A(CN_c + qN_q)$$

$$= ACN_c = 0.54(1400)9 = 6804 \text{ lbs}$$

$$\text{Side Shear} = C \alpha \pi d L$$

$$= 1400(0.6)130.4 = 109,536 \text{ lbs}$$

Pile Capacity - Clay



Total Capacity

$$\begin{aligned} &= 6804 + 109536 \\ &= 116,340 \end{aligned}$$

or

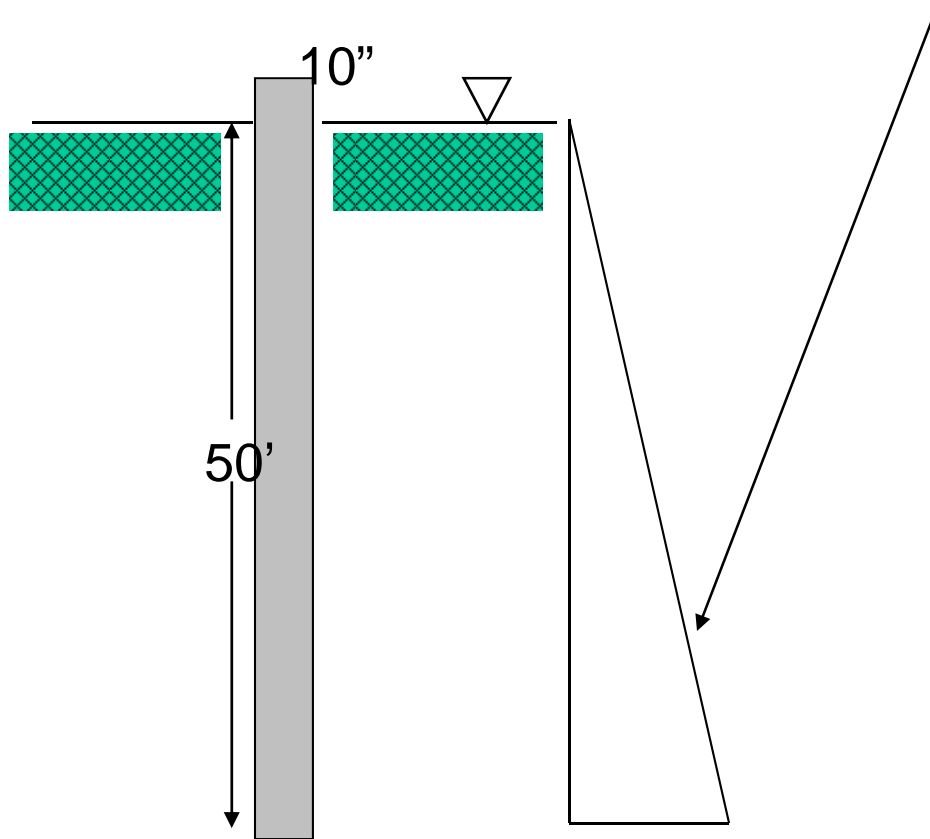
= 58 tons ultimate

for FS = 2

Working Capacity
= **29 tons**

Pile Capacity - Sand

Load Capacity in Sand Depends on Confining Pressure

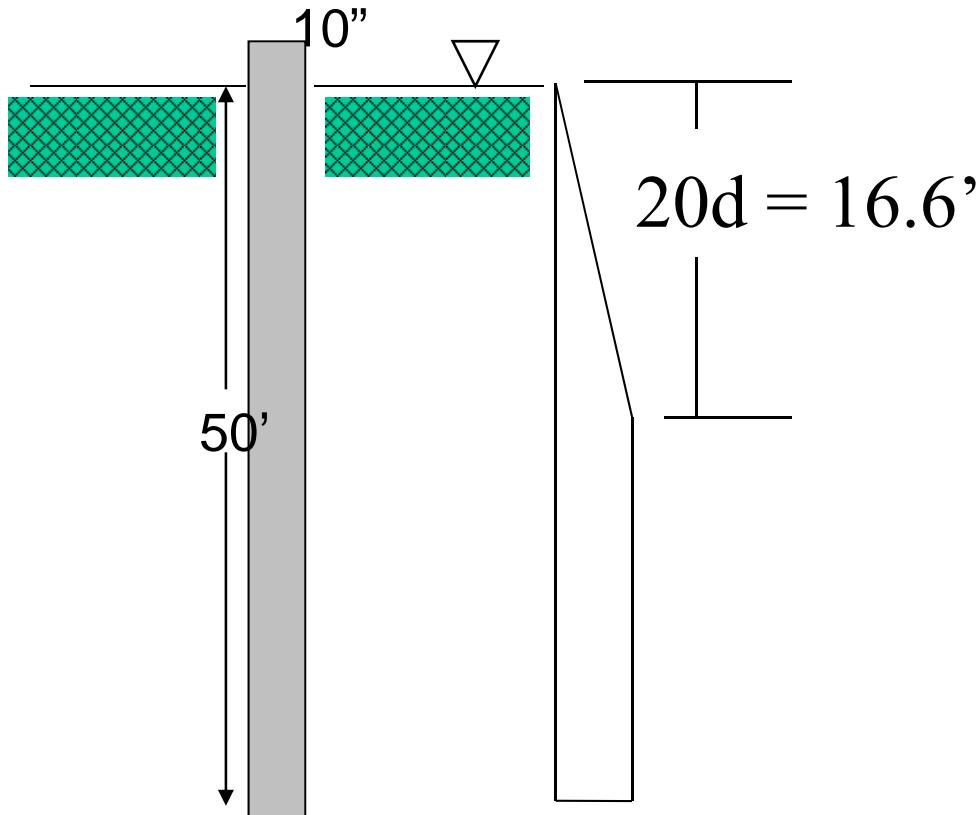


Do end bearing and side shear therefore increase infinitely with depth?

- A) Yes
- B) No

Pile Capacity - Sand

Answer is “B” No - Tests show confinement effects are constant below “critical depth”



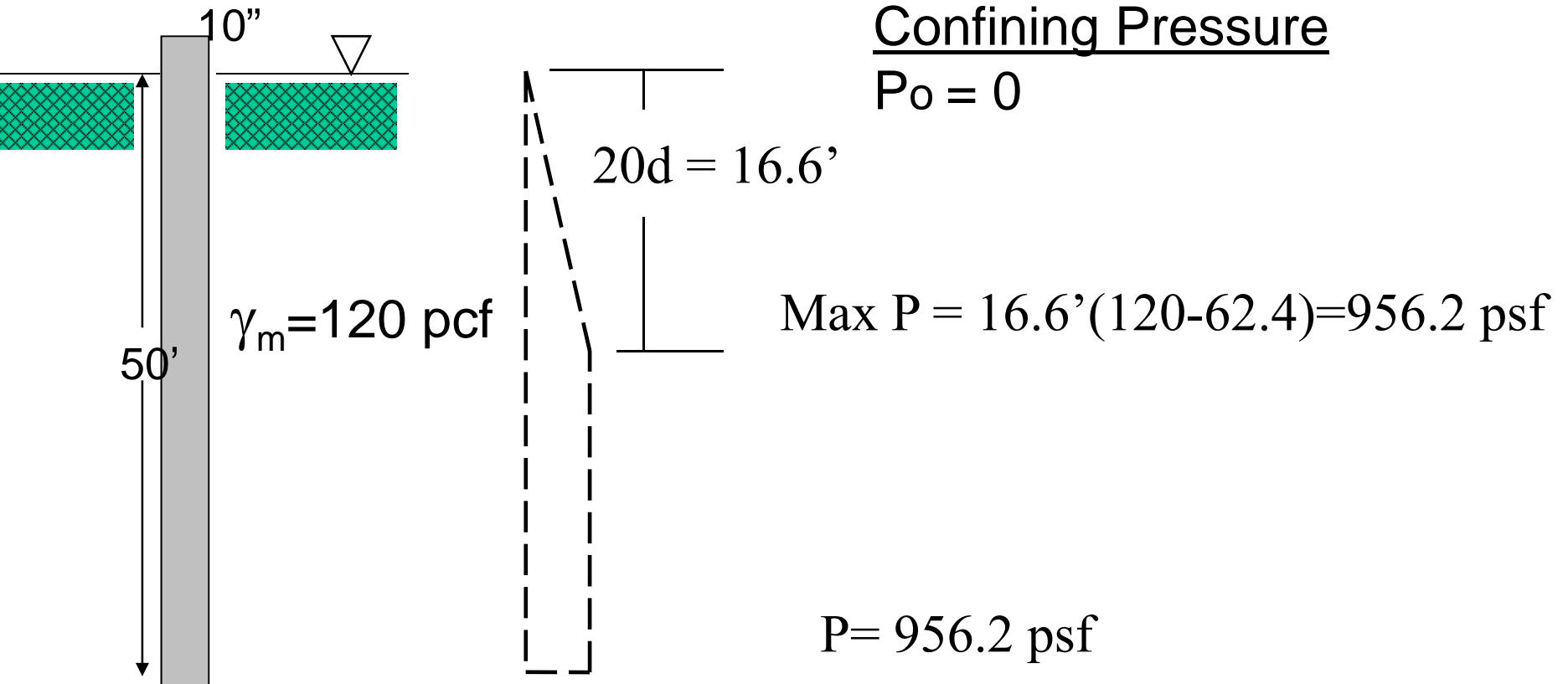
Critical Depth

20d for dense sand

15d for medium sand

10d for loose sand

Pile Capacity - Sand



Pile Capacity - Sand

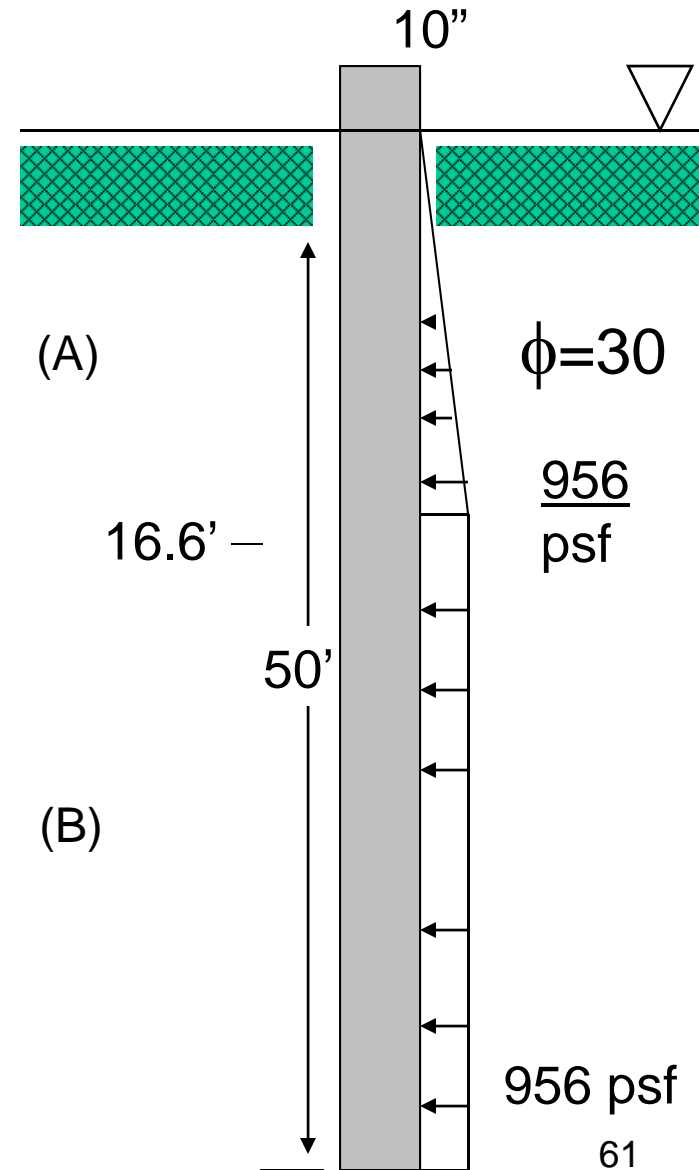
$$N_q = 21; K = 1.5$$

$$\delta = \frac{3}{4}\phi = .75(30) = 23^\circ$$

$$\text{Tip Capacity} = A_q P_{\max} N_q$$

$$= 0.54(956)21$$

$$= \underline{10,841} \text{ lbs}$$

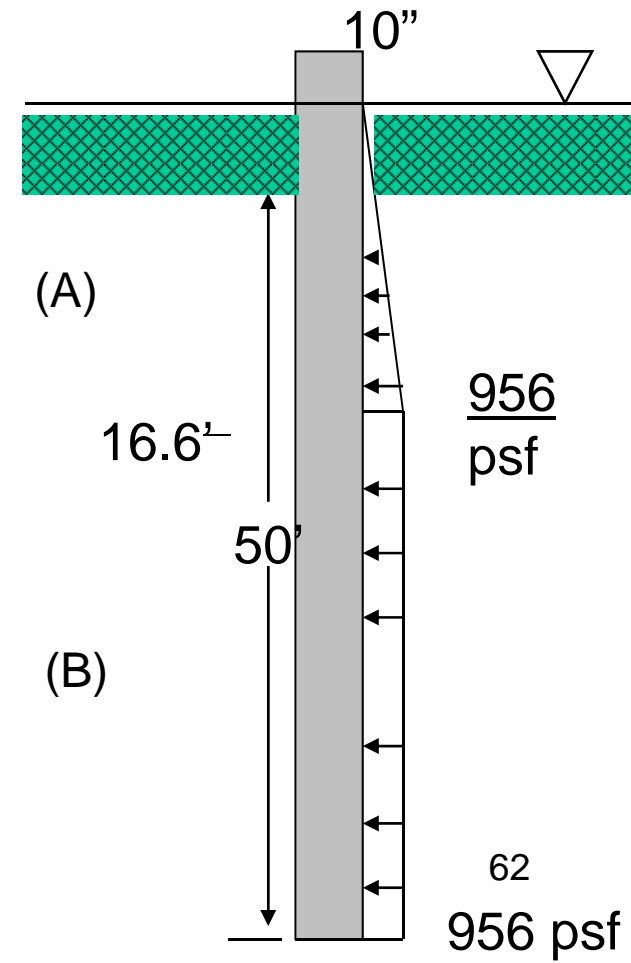


$$\text{Side shear (friction)} = KP \tan \delta \pi dL$$

Section A:

$$= 1.5 (956 / 2) \tan 23 \pi 0.83 (16.6)$$

$$= \underline{13,174 \text{ lbs}}$$

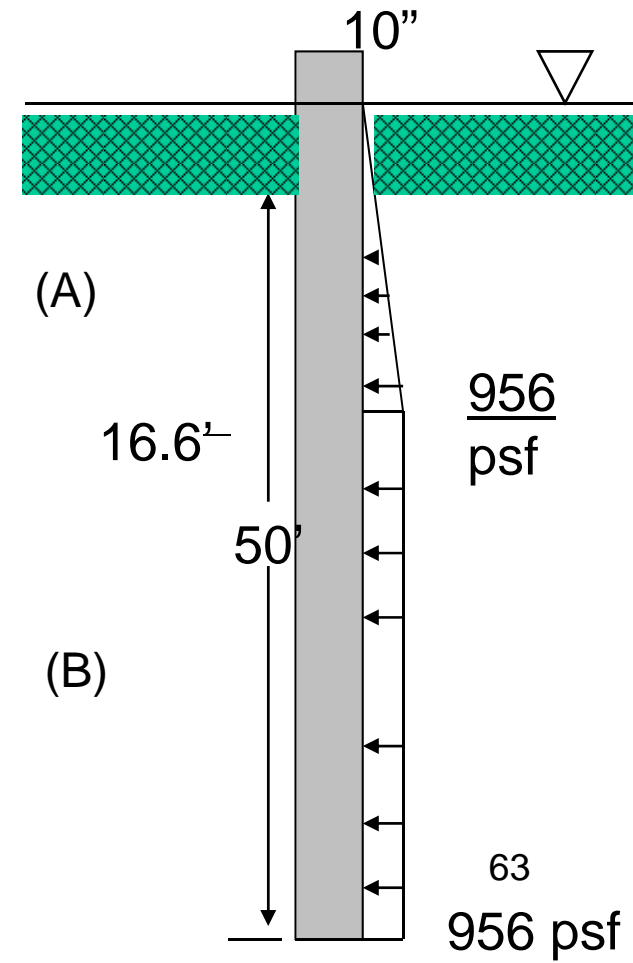


$$\text{Side shear (friction)} = KP \tan \delta \pi d L$$

Section B

$$= 1.5(956) \tan 23 \pi 0.83(33.4)$$

$$= \underline{53,012 \text{ lbs}}$$



$$\text{Side shear (friction)} = K P \tan \delta \pi d L$$

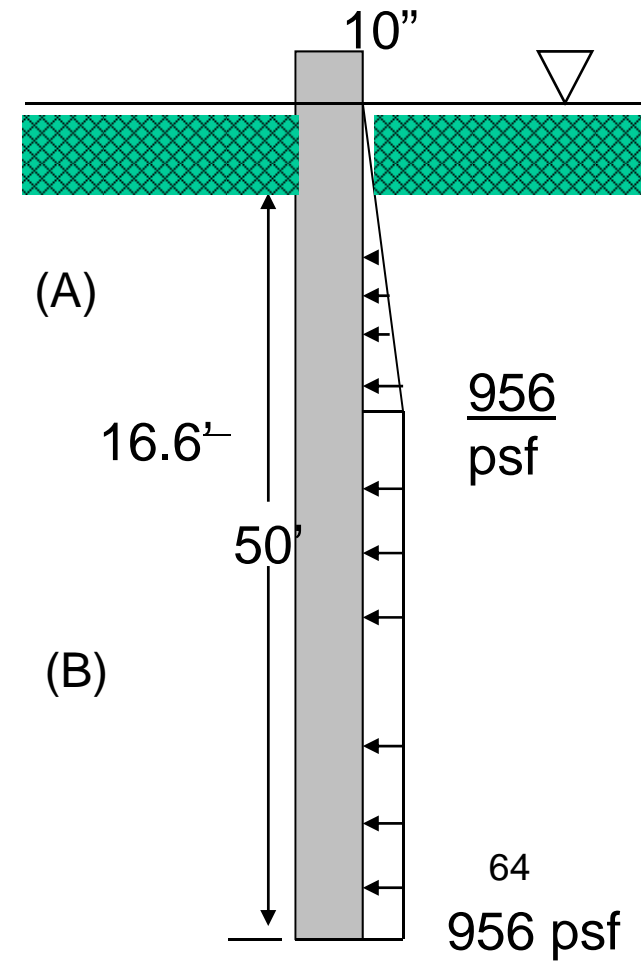
Total Capacity = tip + side shear

$$= 10841 + 13174 + 53012$$

$$= 77027 \text{ lbs}$$

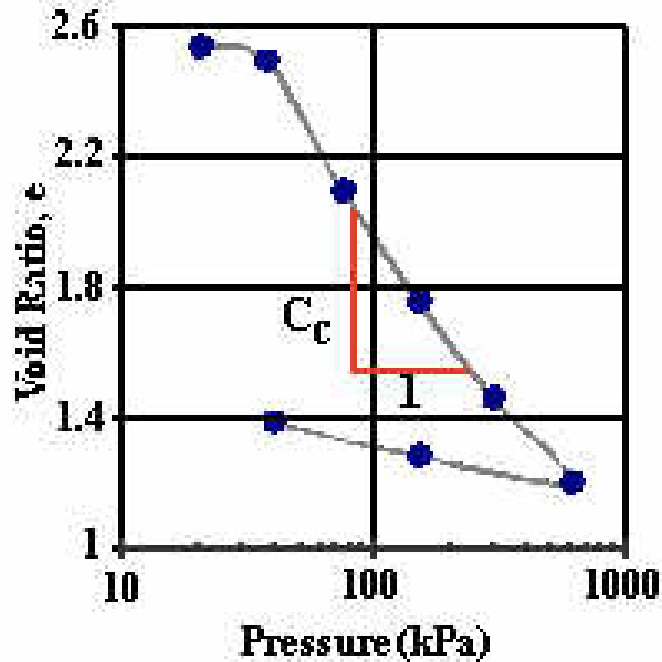
$$= 38.5 \text{ tons Ultimate}$$

$$\text{for FS} = 2, = 19 \text{ tons}$$



Settlement Calculation

Soils Laboratory



Void ratio versus pressure

Compression index is obtained from the slope of the virgin compression curve.

$$S = \Delta H = (H \times \Delta e) / (1 + e_0)$$

or

$$S = HC_c / (1 + e_0) \log (p_0 + \Delta p) / p_0$$

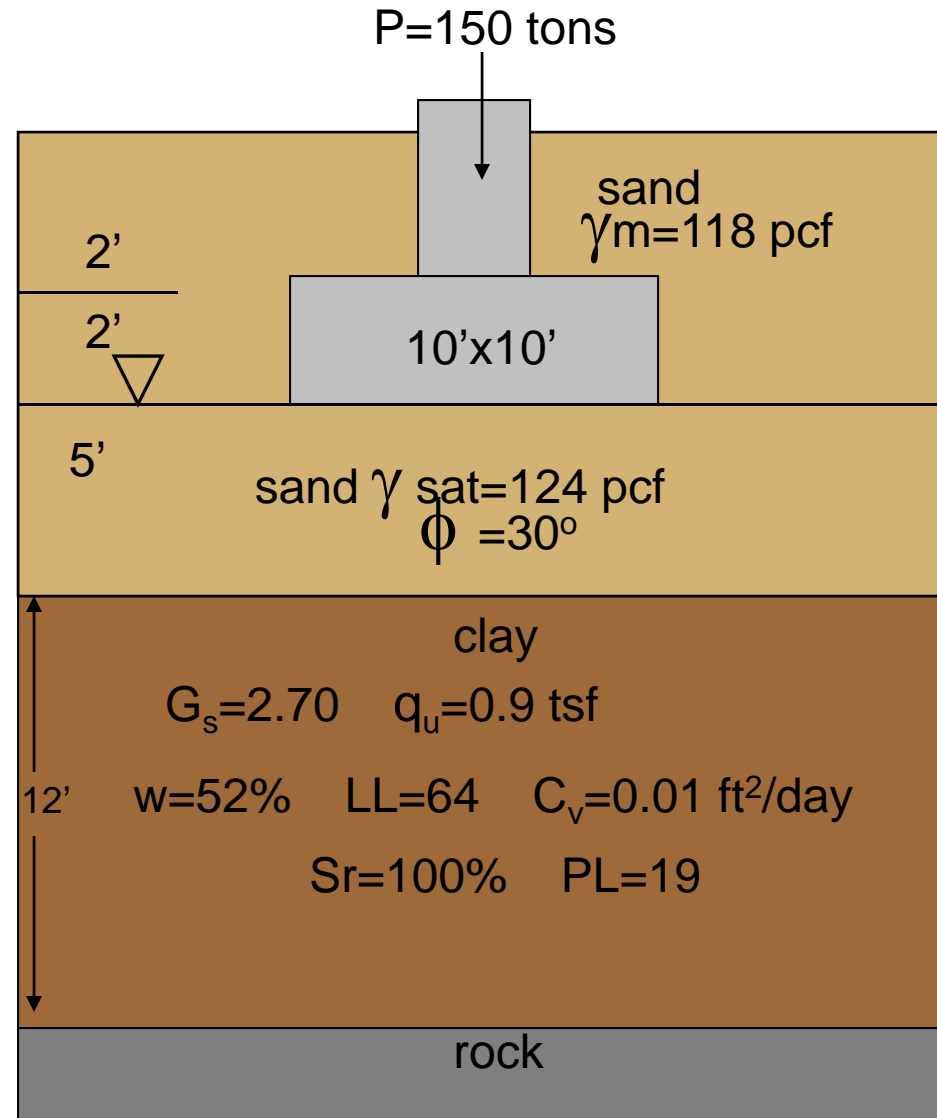
Footing Settlement

Calculate Bearing Pressure

$$BP = \frac{150 \times 2000}{10^2} = 3000 \text{ psf}$$

What is the stress change ΔP_{at} mid-height in clay layer?

- A) 680 psf**
- B) 3000 psf**
- C) 2000 psf**



Footing Settlement

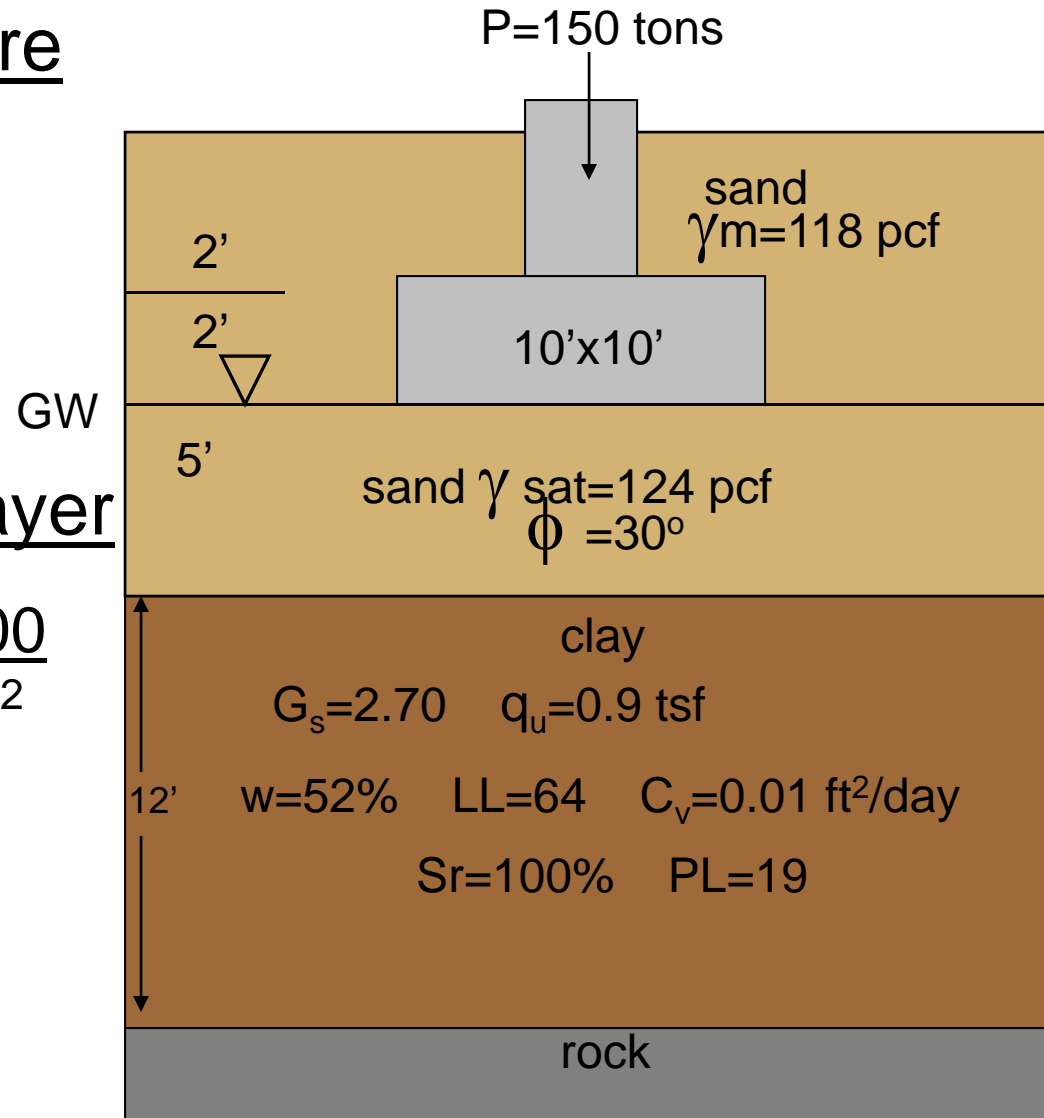
Calculate Bearing Pressure

$$BP = \frac{150 \times 2000}{10^2} = 3000 \text{ psf}$$

ΔP at mid-height in clay layer

$$\Delta P = \frac{P}{(B+Z)(L+Z)} = \frac{150 \times 2000}{(10+11)^2}$$
$$= 680 \text{ psf}$$

Answer is "A"

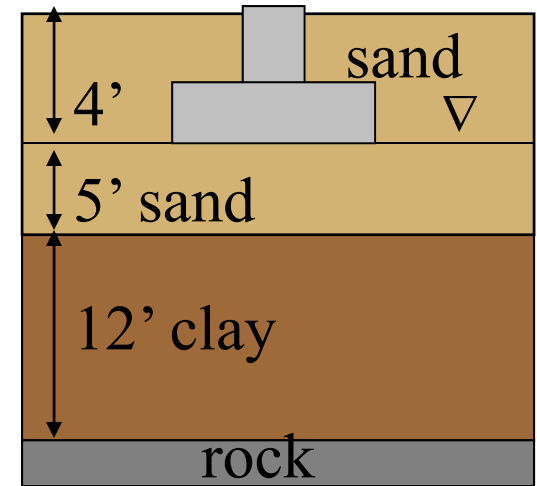


Calculate e_0

$$e_0 = \frac{wG_s}{S} = \frac{0.52(2.7)}{1} = 1.404$$

Calculate Unit Weight of Clay

$$\gamma_{\text{sat}} = \frac{(G_s + e)\gamma_w}{(1 + e)} = \frac{(2.7 + 1.404) 62.4}{(1 + 1.404)} = 106.5 \text{ pcf}$$



Calculate effective stress at mid height of clay layer

$$\begin{aligned} P_o &= \sigma' = \sigma_T - \mu \\ &= 4 \times 118 + 5 \times 124 + 6 \times 106.5 - 11 \times 62.4 \\ &= 1045 \text{ psf} \end{aligned}$$

Calculate settlement of clay layer

Note: moisture is close to LL, void ratio is high & loading is large; expected settlement will be large.

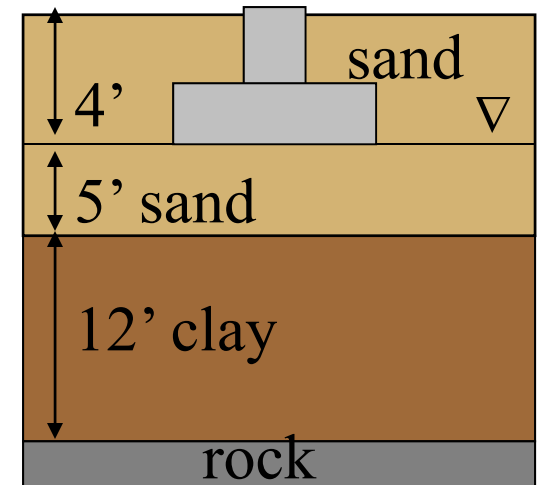
$$C_c = .009(LL - 10) \text{ after Skempton}$$

$$C_c = .009(64 - 10) = 0.49$$

$$S = \Delta H = [C_c / (1 + e_o)] H \log [(P_o + \Delta P) / P_o]$$

$$= [0.49 / (1 + 1.404)] 12 \log [(1045 + 680) / 1045]$$

$$= 0.53' \text{ or } 6.4''$$



Calculate settlement
using e-log p curve

$$P_1 = 1045; \quad e_1 = 1.395$$

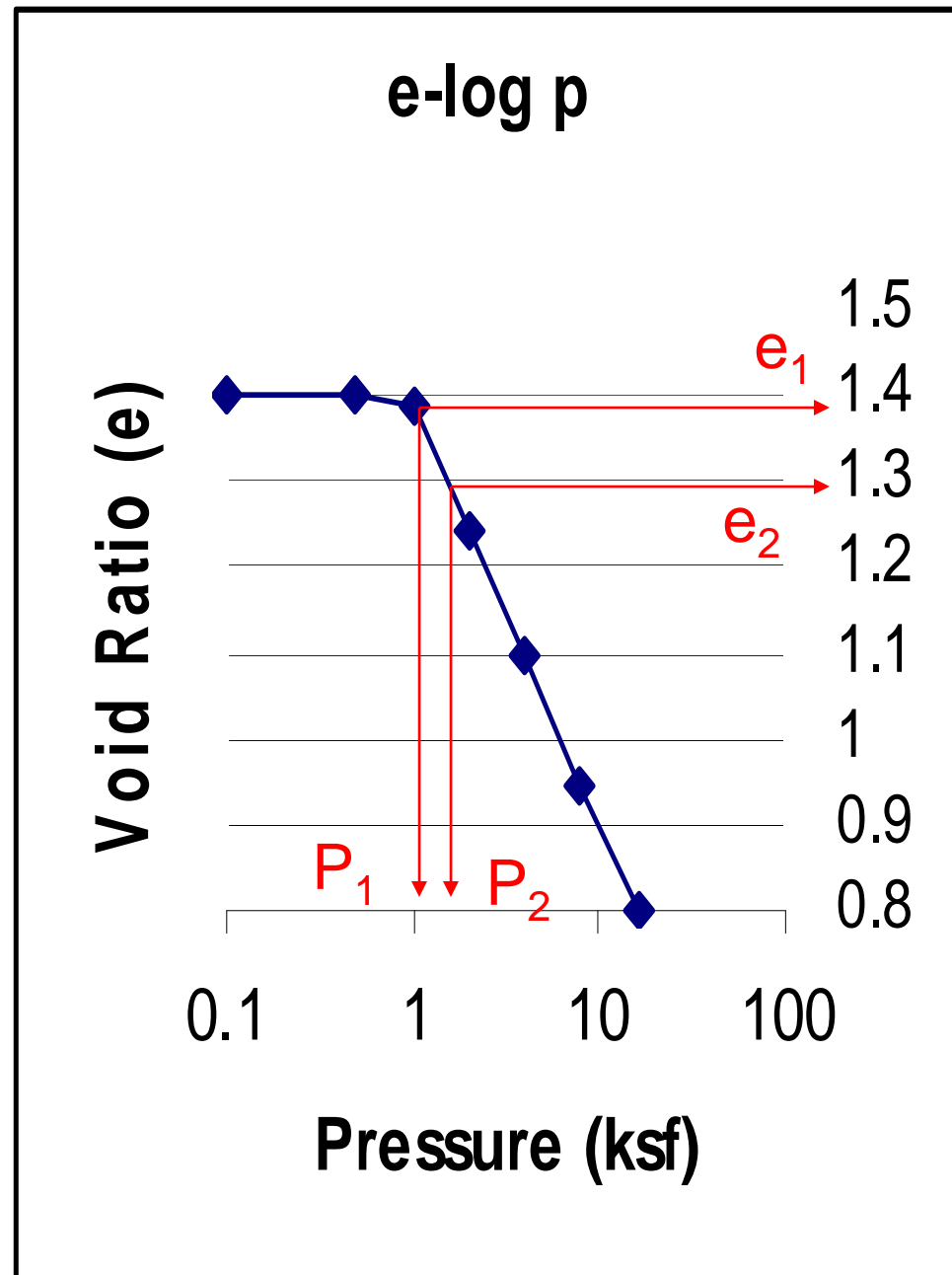
$$\Delta P = 680 \text{ psf}$$

$$P_2 = 1725; \quad e_2 = 1.288$$

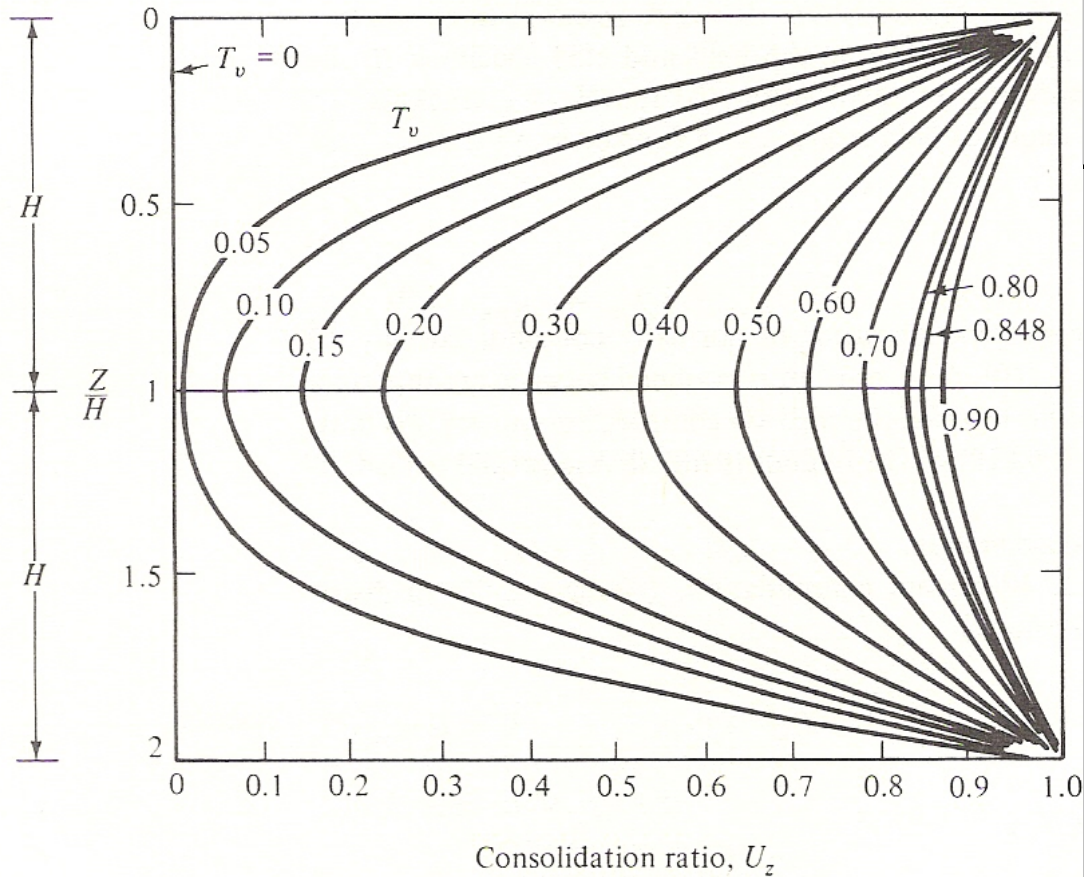
$$S = \Delta H = H \Delta e / (1 + e_o)$$

$$= 12(1.395 - 1.288) / (1 + 1.404)$$

$$= 0.53' \text{ or } 6.4''$$



Rate of Consolidation



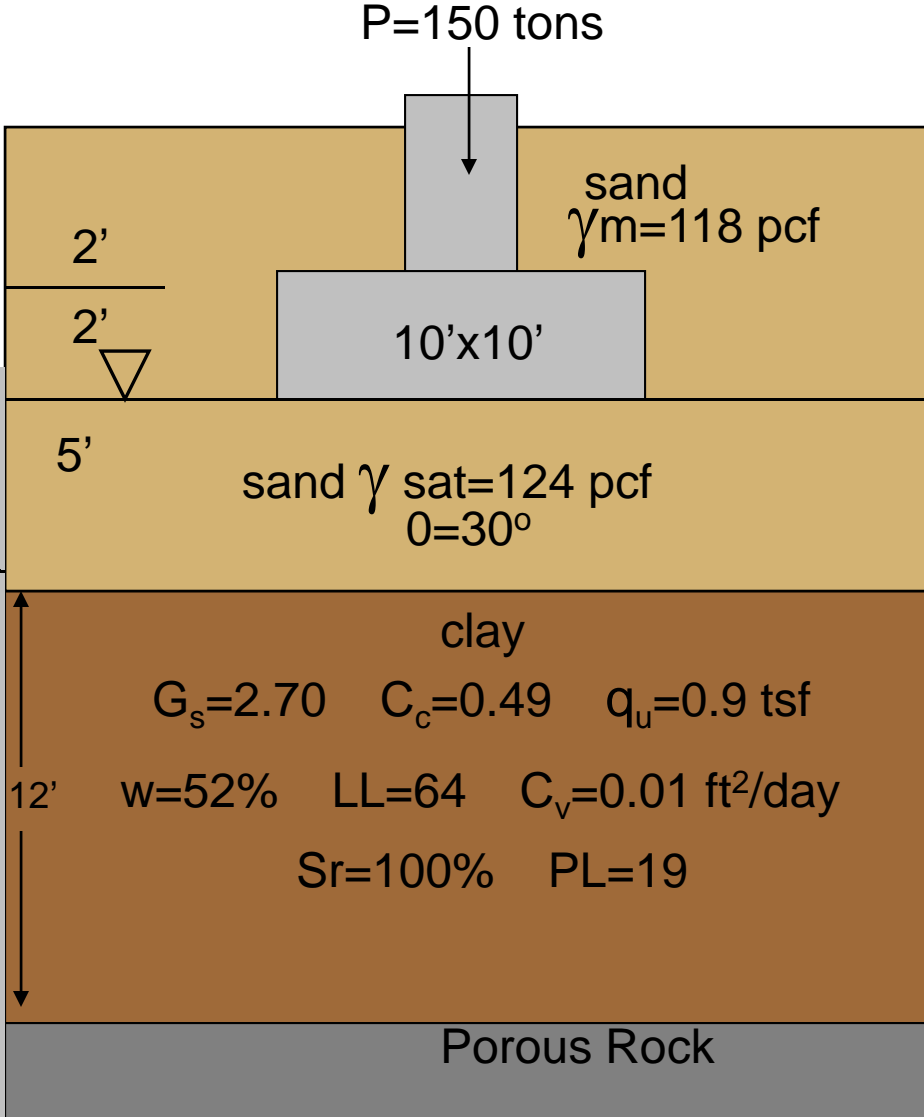
$$T_v = C_v t / H^2$$

Avg. Degree of Consolidation	Time Factor
U%	T_v
10	0.008
20	0.031
30	0.071
40	0.126
50	0.197
60	0.287
70	0.403
80	0.567
90	0.848
100	

How Long Will it Take to Achieve 70 Percent Consolidation?

- A) 16 years
- B) 4 years

Degree of Consolidation	Time Factor
U%	T _v
10	0.008
20	0.031
30	0.071
40	0.126
50	0.197
60	0.287
70	0.403
80	0.567
90	0.848
100	∞



Time to 70 Percent Consolidation

$$t = \frac{T_v (H/2)^2}{C_v} = \frac{0.403 (12/2)^2}{0.01}$$

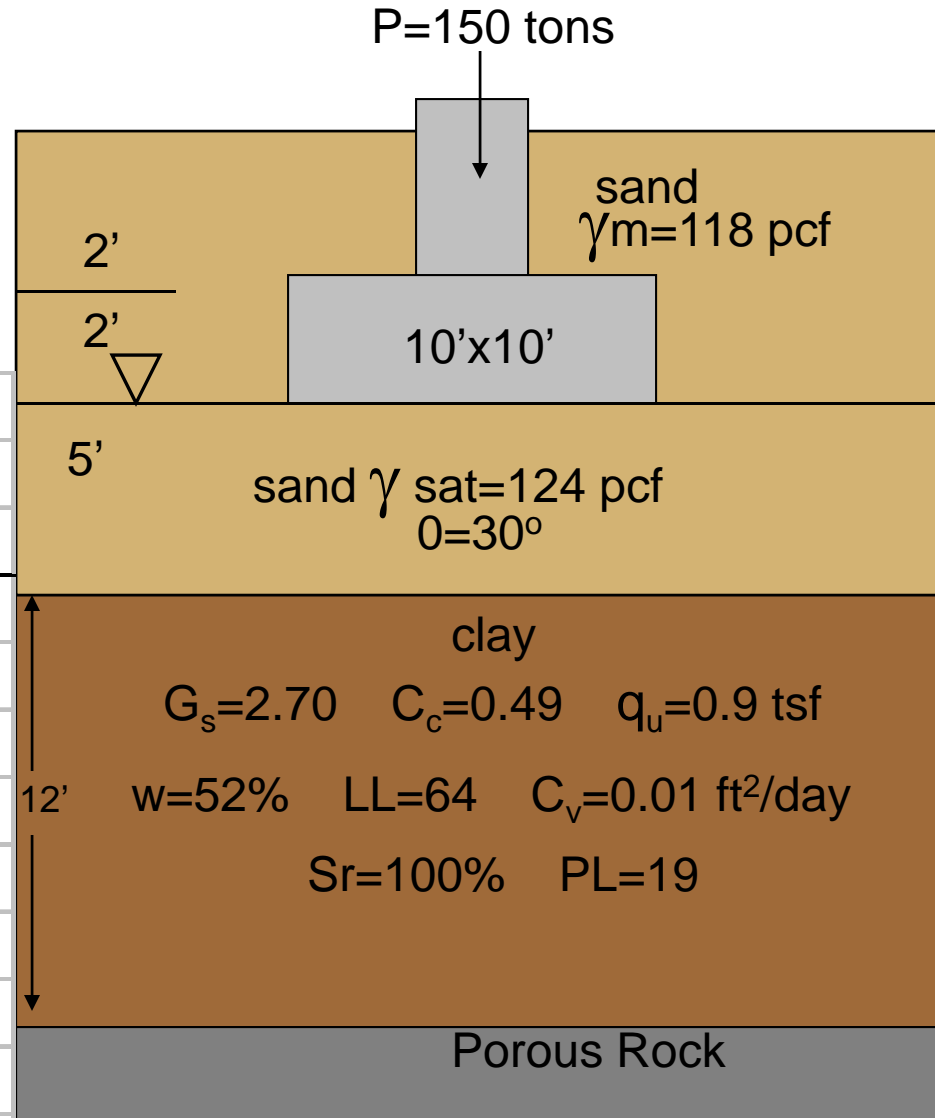
= 1450.8 days

or

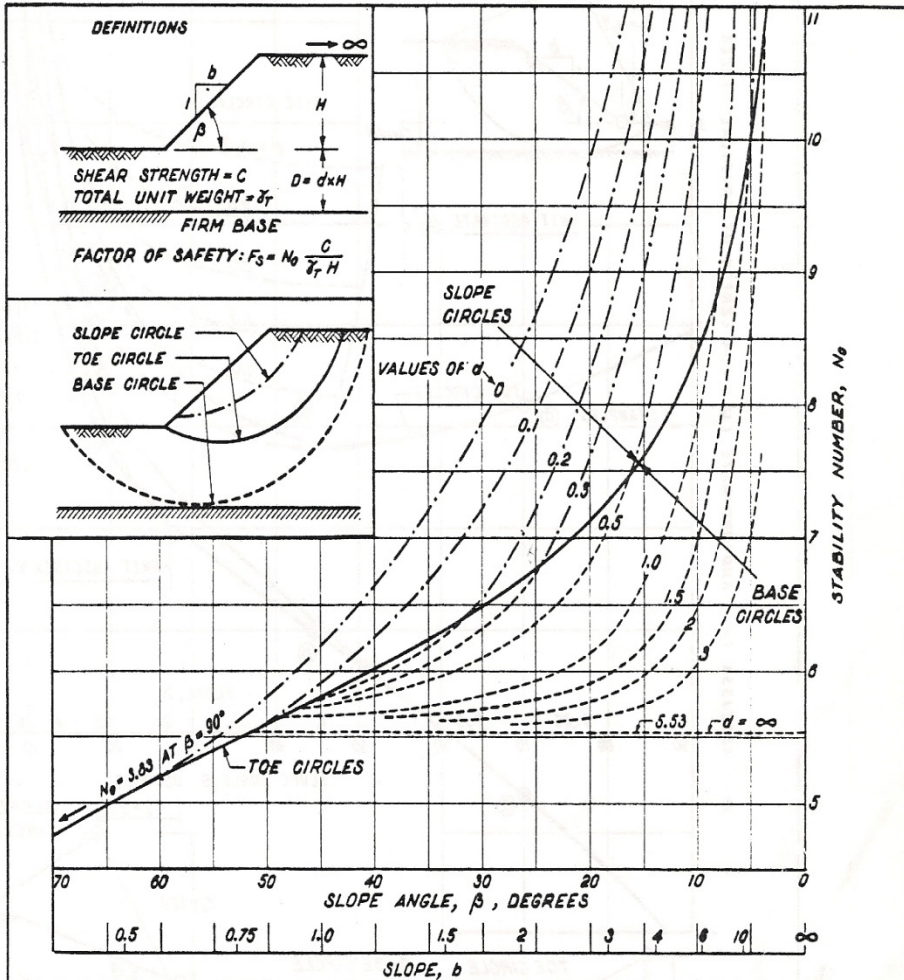
±4 years

**Answer is
"B"**

Degree of Consolidation	Time Factor
U%	Tv
10	0.008
20	0.031
30	0.071
40	0.126
50	0.197
60	0.287
70	0.403
80	0.567
90	0.848
100	∞

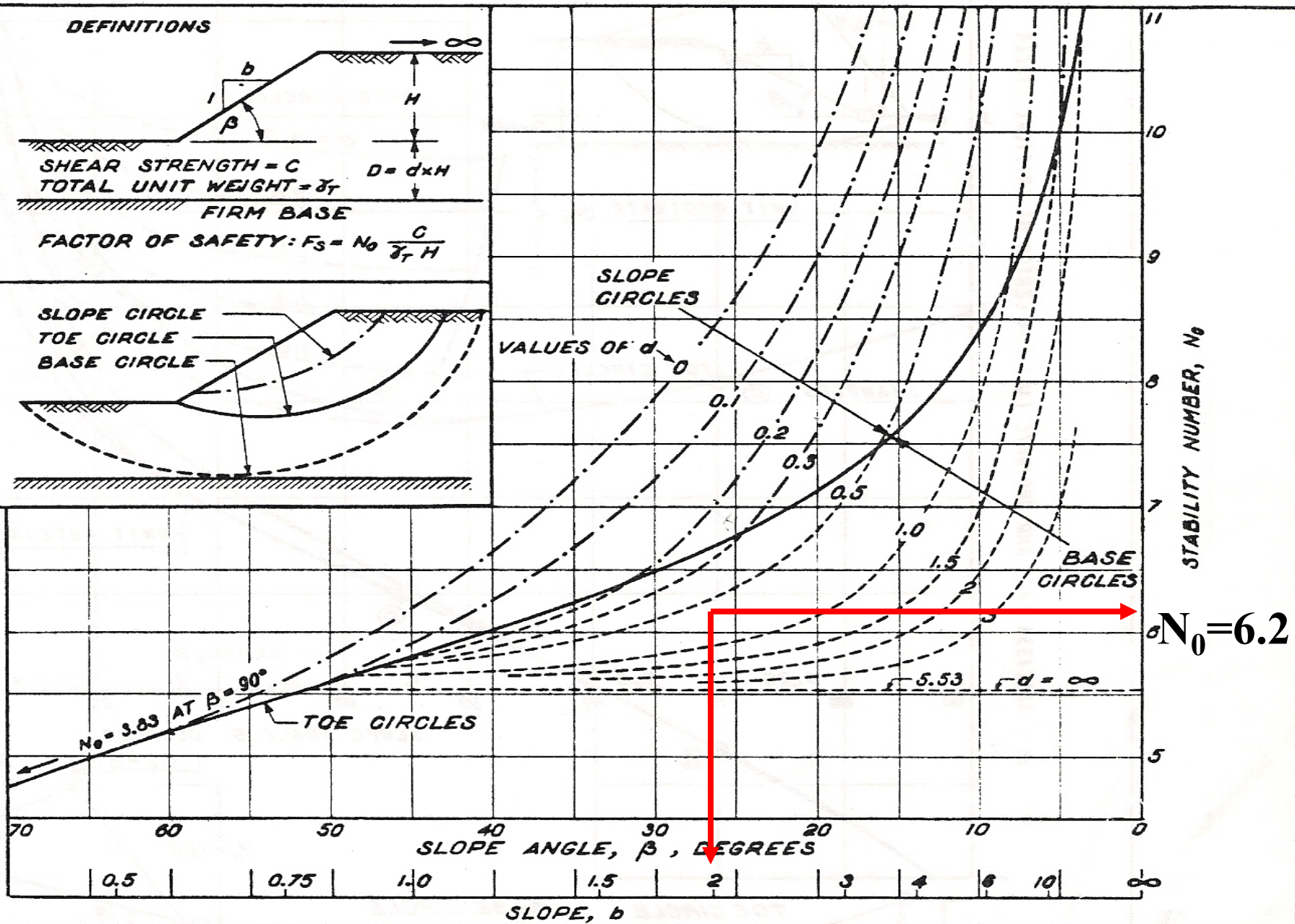
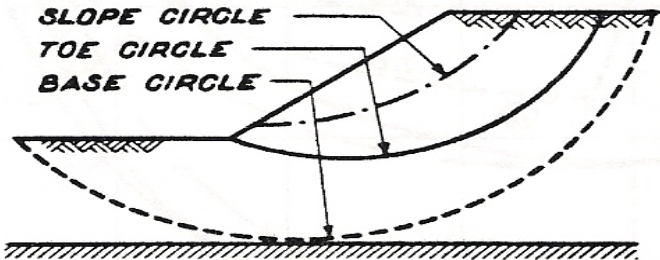
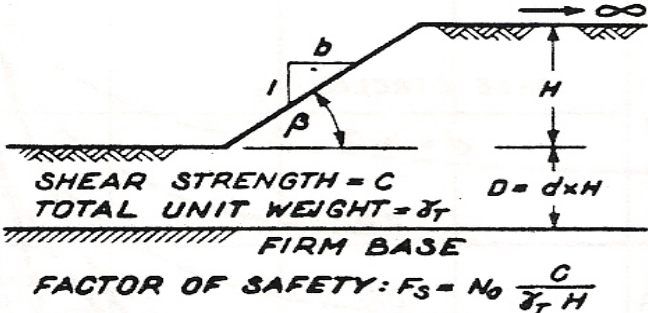


Circular Failure Stability

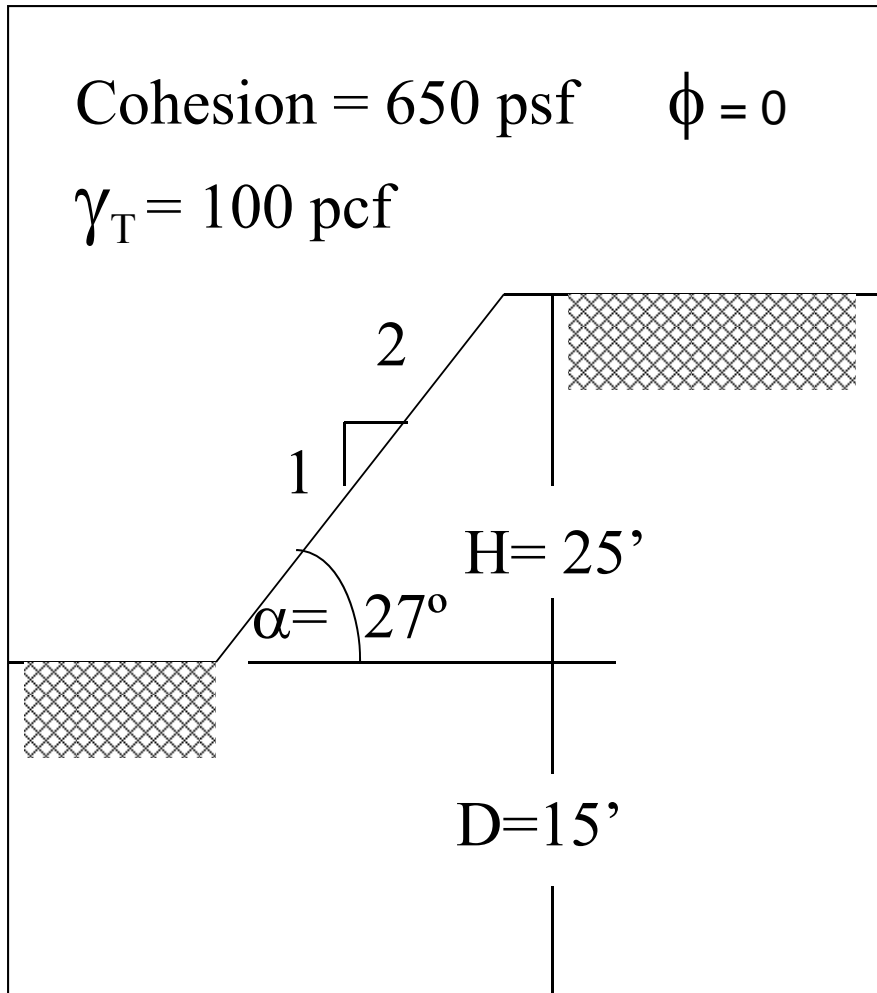


- Homogeneous soils
- No surcharge
- No tension cracks
- $\phi = \text{zero}$
- Circular arc failure
- No water on slope

DEFINITIONS



Slope Stability by Charts



$$d = 15/25 = 0.6$$

$$FS = N_0 C / (\gamma_T H)$$

$$FS = 6.2(650) / (100 \times 25)$$

$$FS = 1.6$$

Thanks for participating in the PE review course on
Foundation Engineering!

More questions or comments?



You can email me at:
gtv@gemeng.com