

# S.E. Exam Review: Concrete Buildings

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## NCEES


According to the NCEES website, the exam will use ACI-318-14.

This presentation is based on ACI-318-14.

The main change to ACI-318-14 was a reorganization and some cleaning up of the code language.

Actual changes were limited.

## This Webinar

- Will cover seismic frames to assist with Day 2 of the exam, which covers lateral load design. Due to time limitations, this is the only lateral system that will be addressed.
- Some of the information can be used for wind load, another lateral load.
- In the design example, it will be necessary to design for gravity loads (Day 1). Look for this sign for provisions applicable to gravity loads.   
Gravity
- Applicable ACI Sections will be cited.
- Seismic frames are now CH 18 (were CH 21).

## Exam Areas Covered

Day	Area	Approx. % on Exam
Friday Morning	Analysis of Structures - Load	10%
	Analysis of Structures - Methods	20%
	Design and Details of Structures – General Considerations	7.5%
	Design and Details of Structures – Concrete	12.5%
Friday Afternoon	Concrete Building Structures (if chosen)	25%
Saturday Morning	Analysis of Structures – Lateral Force Distribution	22.5%
	Design and Detailing of Structures – General Considerations	7.5%
	Design and Detailing of Structures – Structural System Integration	5%
	Design and Detailing of Structures – Concrete	12.5%
Saturday Afternoon	Concrete Building Structures (if chosen)	25%

## Seismic Regions

- ACI 318-14 has Seismic Design Categories (SDC) A – F. (Consistent with ASCE-7)
- SDC is determined by the applicable local code (4.4.6.1).
- The relationship between ACI 318-14 and ACI 318-05:
  - Categories A and B were Low Seismic Risk
  - Category C was Moderate Seismic Risk
  - Categories D – F was High Seismic Risk

Table R18.2 ACI 318-14

Component resisting earthquake effect unless noted	Seismic Design Category			
	A (none)	B (18.2.1.3)	C (18.2.1.4)	D-F (18.2.1.5)
Analysis and Design Requirements	None	18.2.2	18.2.2	18.2.2 18.2.4
Materials		None	None	18.2.5 through 18.2.8
Frame Members		18.3	18.4	18.6 through 18.9
Str. Walls and Coupling Beams		None	None	18.10
Precast Str. Walls		None	18.5	18.5 (if permitted); 18.11
Str. Diaphragms and Trusses		None	None	18.12
Foundations		None	None	18.13
Members not proportioned to resist EQ forces		None	None	18.14
Anchors		None	18.2.3	18.2.3

Must also satisfy Ch 1-17, 19-26, except as modified by Ch 18. 14.1.4 on plain concrete walls applies in SDC D-F.

## General – Analysis

- 18.2.2 Applies to SDC B – F
- This covers analysis and proportioning of structural members.
  - Requires the interaction of structural and non-structural elements to be considered in analysis.
  - Allows rigid members to be assumed not part of the seismic resisting system as long as their effect on response and failure is considered.
  - Requires members below the base to be designed according to CH 18 if they transmit load to the foundation.

## Anchoring to Concrete

- Applies to SDC C-F
- Anchors resisting earthquake forces in SDC C, D, E or F **must** meet 17.2.3 (18.2.3.1)
- ACI 318-14 CH 17 discusses required anchor strength.

## Seismic Moment Frames

- Ordinary Moment Frames
  - For lateral loads in areas of low seismic forces (SDC B)
- Intermediate Moment Frame
  - For lateral loads in conjunction with seismic load in SDC C
- Special Moment Frame
  - For lateral loads in conjunction with seismic load in SDC D-F

## Moment Frames – Low or No Seismic

- Moment Frames
  - Used in SDC A .
  - Satisfy ACI 318 Chapters 1-17; 19-26.
  - Do not need to satisfy CH 18
- Principals of Ordinary Moment Frame design apply but CH 18 provisions are ignored.

## Ordinary Moment Frames

- Ordinary Moment Frames
  - Used in SDC B.
  - Satisfy ACI 318 Chapters 1-17; 19-26.
  - Satisfy 18.2.1.3 – 7; 4.4.64 as applicable
    - General items such as materials, splices, etc.
  - Satisfy 18.3
    - Specific requirements for OMFs

## Intermediate Moment Frames

- Intermediate Moment Frames (18.4)
  - Used in SDC C
  - Satisfy ACI 318 Chapters 1-17; 19-26.
  - Satisfy Chapter 18.2.1.3 – 7; 4.4.6.4 (General Requirements)
  - Satisfy Chapter 18.4
    - Special provisions for IMFs

## Special Moment Frames

- Special Moment Frames
  - Used in SDC D - F
  - Satisfy ACI 318 Chapters 1-17; 19-26.
  - Satisfy Chapter 18.2.1.3 – 7; 4.4.6.4
  - Satisfy Chapters 18.2.3-8
  - Satisfy Chapter 18.9

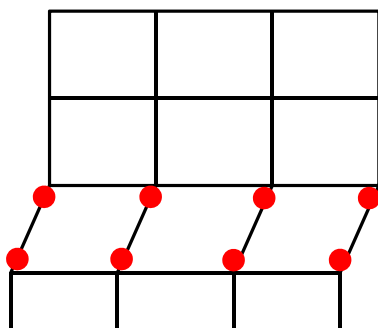
## Seismic Frame Philosophy

Seismic failure of frames occurs when plastic hinges form.

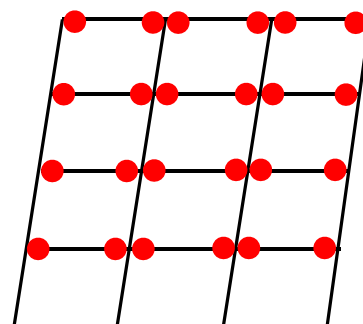
There are two basic ways a building can fail:

The hinges form in the columns (Story Mechanism)

The hinges form in the beams (Sway Mechanism)



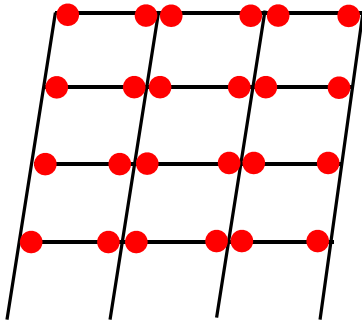
Story Mechanism  
Weak Column/Strong Beam  
Undesirable!



Sway Mechanism  
Strong Column/Weak Beam  
Required by Code!



## Seismic Frame Philosophy



Sway Mechanism  
Strong Column/Weak Beam  
Required by Code!

Note: The Code uses both  $N_u$  and  $P_u$  for axial loads, but in CH 18 it always uses  $P_u$ .

We want the beams to fail before the columns.

ACI MAY require:

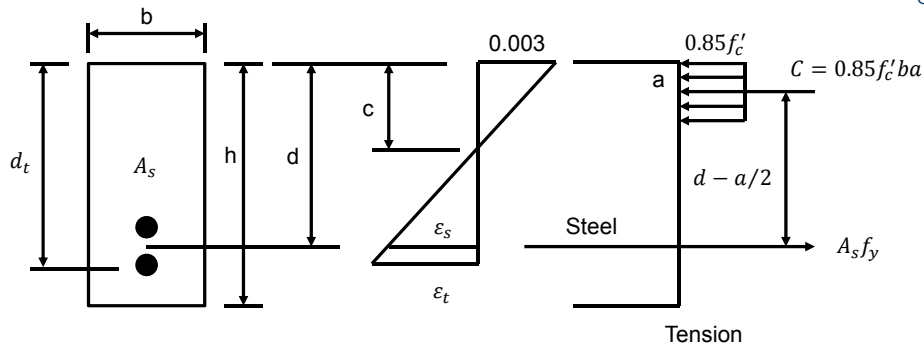
- 1) If there is a certain level of axial load,  $P_u$ , in a beam, it may have to be designed as a beam/column.
- 2) There may be a requirement for relative strength of columns and beams and joints.
- 3) There may be requirements for relative strength along the beams.
- 4) There may be special requirements for shear.
- 5) There may be a requirement to consider both maximum and minimum material strength.

## Ordinary Moment Frames

- Used for resisting various lateral loads. May only be used in SDC A or B.
- Note that Chapter 18 does not place restrictions on  $P_u$  for beams in an ordinary moment frame.

## Reminder

$M_n$  is the nominal moment strength.



$$C = T$$

$$0.85f'_c b a = A_s f_s \quad M_n = A_s f_y \left( d - \frac{a}{2} \right) = 0.85f'_c b a \left( d - \frac{a}{2} \right)$$

$$a = \frac{A_s f_s}{0.85f'_c b}$$

*Note:  $d$  is the depth to the centroid of all the tensile steel,  $d_t$  is the depth to the tensile steel furthest from the compression face.*

## Reminder

**Recall:**

$$\beta_1 c = a$$



Where:

$c$  = depth of neutral axis

$a$  = depth of stress block for finding  $M_n$ .

$\beta_1 = 0.85$  if  $f'_c \leq 4$  ksi

0.65 if  $f'_c \geq 8$  ksi

interpolate in between

Example: For  $f'_c = 6$  ksi,  $\beta_1 = 0.75$

## Ordinary Moment Frames

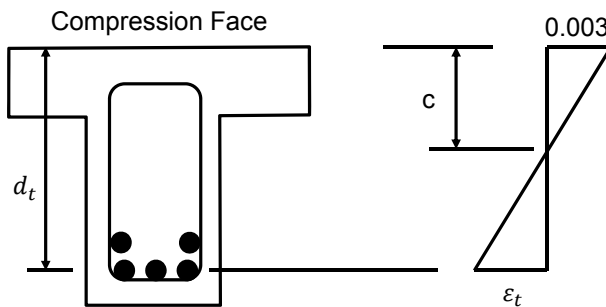
For **non-prestressed** flexural members:



If  $P_u \leq 0.1f'_c A_g$ , then:

Extreme steel tensile strain at  $M_n$ :

$$\varepsilon_t \geq 0.004 \quad (9.3.3.1)$$



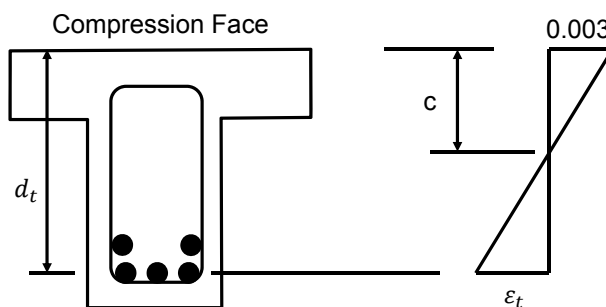
Remember –  $M_n$  is defined as the moment capacity when the extreme compressive strain = 0.003. A linear strain diagram is used to find  $\varepsilon_t$ . The term “c” is the depth to the neutral axis. The width of the compression face is b.

## Definition of Section Types (ACI 21.2.2)



Strain in the extreme tensile steel, $\varepsilon_t$	Type of Section	$\phi$
$\varepsilon_t \leq f_y/E_s$	Compression Controlled $c/d_t \geq 3/5^*$	0.65 Tied Conf. 0.75 Spiral Conf.
$0.005 > \varepsilon_t > f_y/E_s$	Transition $3/8 < c/d_t < 3/5^*$	Interpolated based on $\varepsilon_t$
$\varepsilon_t > 0.005$	Tension Controlled $c/d_t \geq 3/8$	0.9

\*For Grade 60 steel and prestressing steel, where  $f_y/E_s$  may be taken as 0.002.



## Ordinary Moment Frames

- Non Prestressed Flexural Members (including those not in OMFs)
  - Must meet Section 9.6.1.2 (minimum flexural reinforcement  $3\sqrt{f'_c}b_wd/f_y \geq 200b_wd/f_y$ ).
  - At each section,  $M_u \leq \Phi M_n$  (9.5.1.1)
    - No requirement on relative positive and negative moment strengths at face of joint.
    - No requirement relative moment strength at any section as compared to joint moment strength.

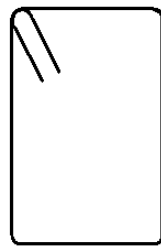


## Ordinary Moment Frames

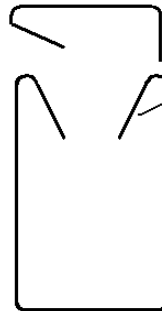
- Non Prestressed Flexural Members (including those not in OMFs)
  - Must meet structural integrity requirements of Section 9.7.7 if not EQ resistant or SDC A; perimeter beams
    - At least 1/6 of the tension reinforcement required for negative moment at the support (2 bars min) shall be made continuous.
    - At least 1/4 of the tension reinforcement required for positive moment at midspan (2 bars min) shall be made continuous.
    - Longitudinal structural integrity reinforcement must pass through the region bounded by the longitudinal reinforcement of the column.
    - Longitudinal structural integrity reinforcement must be enclosed by closed stirrups (25.7.1.6) or hoops along the clear span.
    - Longitudinal structural integrity reinforcement must develop  $f_y$  at the face of the support.
    - Positive steel is spliced at or near a support, negative steel is spliced at or near midspan. Use Class B, welded or mechanical splices



## Stirrup Options



Closed hoop with 135° hooks.



Seismic stirrup + hairpin with a 135° hook and a 90° hook

Extensions must be  $6d_{bh}$   
 $\geq 3$  inches  
Extension on the 90° hook is  $6d_{bh}$

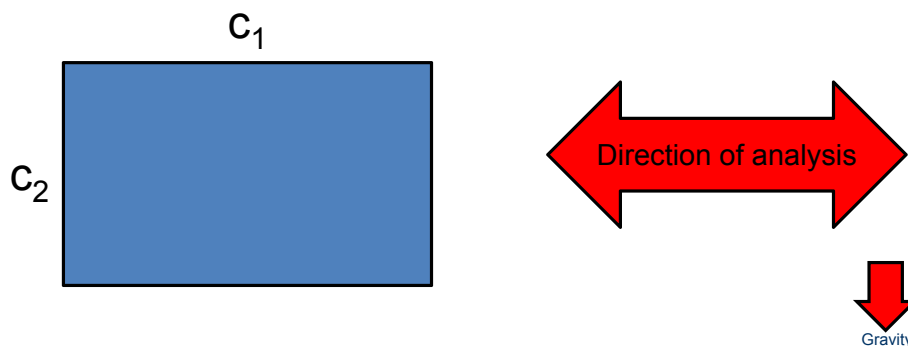


Options for beam hoops. For the stirrups on the right, the 90° hook is always on the slab side for a perimeter beam.

25.7.1.6

## Definition of $c_1$ and $c_2$

**Definition:** The term  $c_1$  is the dimension of the rectangular column, or equivalent rectangular column, capital or bracket in the direction of analysis. The term  $c_2$  is the column dimension in the perpendicular direction. This definition applies to all columns, even those not in moment frames.



## Ordinary Moment Frames

In SDC B – Ch 9.7.7 is modified by Ch 18.3:

### 18.3.3

Beams must have 2 continuous bars on the top face and on the bottom face.

These bars must develop  $f_y$  developed at the face of the support.

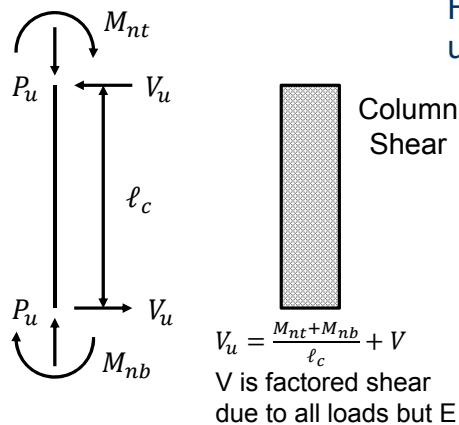
Continuous bottom bars must have at least  $\frac{1}{4}$  of the maximum bottom steel area.

## Ordinary Moment Frames

18.3.3: Columns with an unsupported length of  $< 5c_1$  shall have  $\phi V_n$  at least the lesser of:

- a) The shear associated with development of nominal moment strengths of the column at each restrained end of the unsupported length due to reverse curvature bending. Column flexural strength shall be calculated for the factored axial force, consistent with the direction of lateral forces considered, resulting in the highest flexural strength.
- b) The maximum shear obtained from design load combinations that include E, with  $\Omega_0 E$  substituted for E.

## Ordinary Moment Frames



Here is the rule for columns with an unsupported length of  $< 5c_1$ .

18.3.3: Use the lesser of applied  $V_u$  or the shear caused by

$$U = 1.2D + 1.0L + 0.2S + \Omega_0 E$$

$\Omega_0$  is the overstrength factor in ASCE 7; currently = 3

$\ell_c$  is the clear height.

Recall,  $c_1$  is column dimension in direction of analysis. To determine  $M_{nt}$ , use the interaction diagram value corresponding to  $P_u$ . If there are different values of  $M_{nt}$ , use the biggest.

## Ordinary Moment Frames

- Non Prestressed Flexural Members (including those not in OMFs)
  - No special requirements to encase splices in hoops unless required for bond, development length or splices.
  - No added restrictions on the use of lap splices.
  - For shear and torsion, meet the requirements of the appropriate chapter.
  - **For flexural members subject to stress reversals, provide closed stirrups around the flexural reinforcement.**

## Ordinary Moment Frames

- Columns (including those in not in OFMs) (compression members)
  - There are no special rules for columns (except as previously stated for short columns)
  - Columns must meet the requirements of Ch 10.
  - Columns **may** be “slender” and in a non-sway or sway frame. In these cases, the requirements of 6.6.4 must be met.
- Beam Column Joints
  - No special requirements. Meet 15.4.



## Intermediate Moment Frames

- Used in SDC C
- Must meet Chapter 18.2.2 for analysis and proportioning.
- Must meet Chapter 18.4



## Intermediate Moment Frames

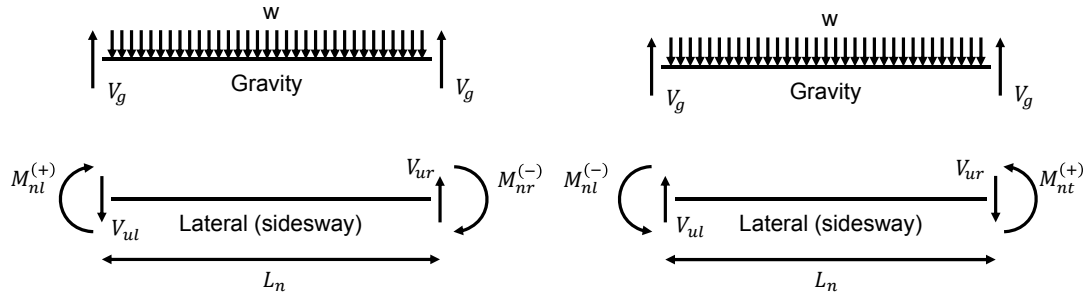
- Beam
  - Is a member primarily subject to flexure and shear; may or may not have axial load and torsion. In a moment resisting frame, they are primarily horizontal (2.3 terminology)
  - 18.4.2.1 Must have at least two top and bottom continuous bars. Continuous bottom bars (positive moment reinforcement) must have at least  $\frac{1}{4}$  the maximum area of bottom bars along the span. Continuous bars must be anchored to develop  $f_y$  at the face of the support.

## Intermediate Moment Frames

- IMF Flexural Members and Columns
  - 18.4.2.3 – The design shear force shall be the lesser of:
    - a) The sum of the shear associated with the development of the nominal moment strength at the end of the member + gravity load.
    - b) The maximum shear from any load combination containing E, when E is that prescribed by the governing code for earthquake resistant design, multiplied by the appropriate factor.

This provision is illustrated on the next few slides.

## Intermediate Moment Frame Shear Requirements (18.4.2.3)



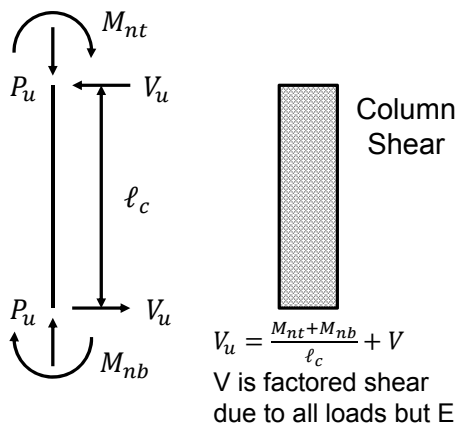
Use:  $w = 1.2D + 1.0L + 0.2S$

Assume that each joint develops  $M_n$  and calculate the corresponding shear. Consider sideways in **both** directions, using the greater of  $V_{ul}$  and  $V_{ur}$  at each end.

Use the lesser of  $V_{ul}$  and  $V_{ur}$  or the shear caused by  $2E$ .

Add the **factored** gravity shear,  $V_g$ .

## Intermediate Moment Frames



Use the lesser of  $V_u$  or the shear caused by

$$U = 1.2D + 1.0L + 0.2S + \Omega_0 E$$

$\Omega_0$  is the overstrength factor in ASCE 7; currently = 3

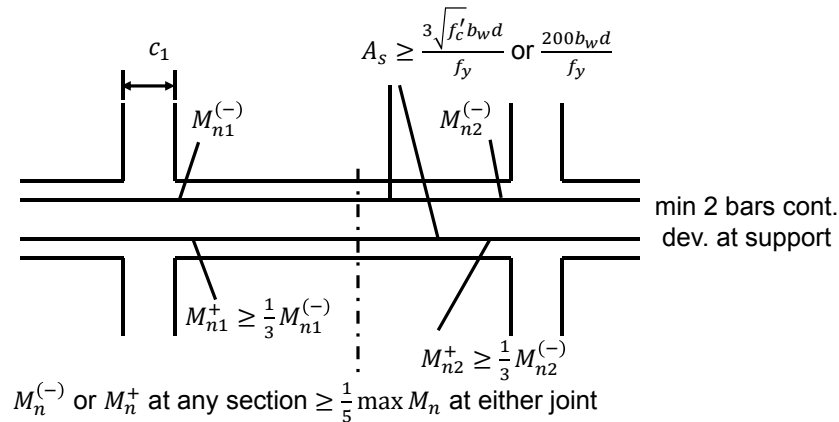
Here is the same rule for columns.  $\ell_c$  is the clear height.

This is the OMF rule (18.3.3).

## Intermediate Moment Frames

### ■ IMF Flexural Members (18.4.2.2) – Required Relative Moment Strengths:

- At the face of a joint,  $M_n^+ \geq M_n^{(-)}/3$
- At every section, provide  $M_n^+$  and  $M_n^{(-)} \geq 1/5$  of the **maximum**  $M_n$  (either + or -) at the face of either joint.

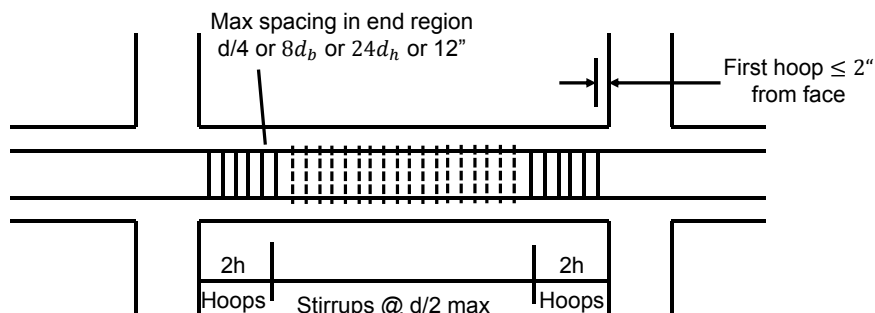


## Intermediate Moment Frames

### ■ IMF Flexural Members

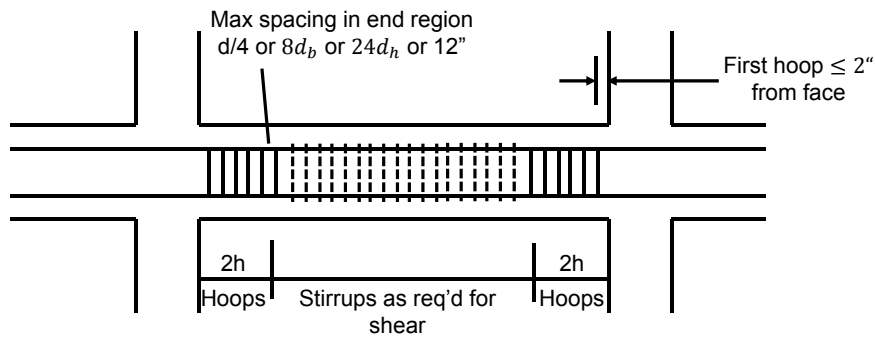
#### ■ Transverse Reinforcement (18.4.2.4)

- Hoops are required over a length equal to  $2h$  from the face of the support toward midspan on both ends.
- Maximum hoop spacing is  $d/4$ ;  $8d_b$ ;  $24d_h$  or 12 in. The term  $d_b$  is longitudinal bar diameter and  $d_h$  is the hoop bar diameter. First hoop within 2 inches of the face of support.



## Intermediate Moment Frames

- IMF Flexural Members (con't)
  - Transverse Reinforcement (18.4.2.5)
    - Where hoops are not required, provide stirrups as needed for shear throughout the entire member. Maximum spacing as permitted for shear.
    - This provision is not specific about the stirrup type. Probably, the stirrup must be a hoop or a U with seismic ( $135^\circ$ ) hooks.



## Intermediate Moment Frames

- IMF Flexural Members (con't)
  - Transverse Reinforcement (18.4.2.6)
    - If  $P > 0.1A_gf'_c$  then provide transverse reinforcement according to 25.7.2.2 and either 25.7.2.3 or 4. (These are the normal provisions for column ties; so basically reinforce as a column).

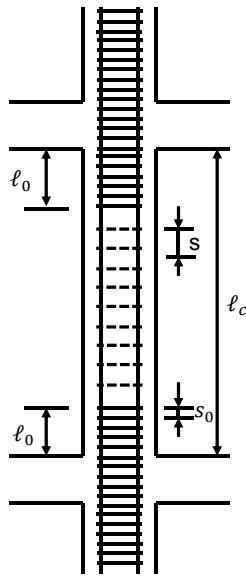
## Intermediate Moment Frames

- Columns (18.4.3)
  - A member is considered a column if it is vertical and is used to primarily support axial load; may or may not have shear, flexure and torsion. (2.3 – Terminology).
  - It must meet all requirements for compression members given in Ch 10 (normal rules for columns).
  - Columns must have:
    - Spiral reinforcement meeting 25.7.3
    - **Or** vertical bars and ties meeting 18.4.3.3 through 18.4.3.5, as applicable.

## Intermediate Moment Frames

- Columns (18.4.3.3 - 5)
  - Transverse reinforcement (non-spiral)
    - Define  $\ell_o$  as the maximum of  $h$ ,  $b$ ,  $1/6$  clear span of the column or 18 in
    - Within  $\ell_o$ , the maximum spacing of transverse reinforcement,  $s_o$ , is the minimum of  $8d_b$ ,  $24d_h$ ,  $h/2$ ,  $b/2$  or 12 in. The first hoop  $\leq s_o$  from the joint face (21.3.5.3). The terms  $d_b$  = longitudinal bar diameter and  $d_h$  = tie diameter.
    - Outside  $\ell_o$ , the maximum spacing of transverse reinforcement,  $s$ , as specified in 10.7.6.5.2 and 25.7.2.3 (normal column rules).

## Transverse Reinforcement Requirements for Columns



$l_c$  is clear height of column

$l_0$  max of  $c_1$ ,  $c_2$ ,  $l_c/6$  or 18 in

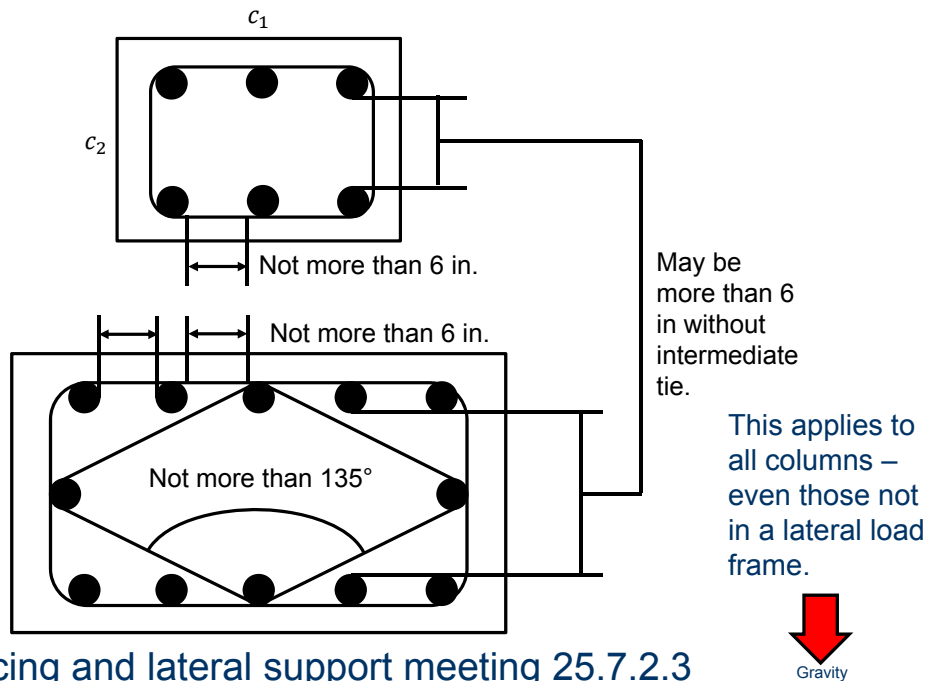
$s_0$  min of  $8d_b$ ,  $24d_{b, \text{tie}}$ ,  $c_1/2$ ,  $c_2/2$  or 12 in.

$s = c_1, c_2, 16d_b, 48d_{b, \text{tie}}$  (25.7.2) but  $s_{\text{max}} = d/2$  or 24 in (9.7.6.2.2)

First tie within  $s_0$  of face.

Splice at slab/beam (normal splice)

## Transverse Reinforcement Requirements for Columns



Bar spacing and lateral support meeting 25.7.2.3

## Intermediate Moment Frames

- Columns (con't)
  - Joint transverse reinforcing must meet Ch 15.
  - When loads cause transfer of moment, the resulting shear must be considered.
  - Joint reinforcing must meet equation 15.4.

$$A_{v,min} = 0.75\sqrt{f'_c} \frac{b_w s}{f_{yt}} \geq \frac{50b_w s}{f_{yt}}$$



## Intermediate Moment Frames

- See 18.4.3.6 for columns supporting discontinuous stiff members (like walls).
- See 18.4.5 for two way slabs without beams.

## Special Moment Frames

- Excellent reference: **Seismic Design of Reinforced Concrete Special Moment Frames: A Guide for Practicing Engineers (NIST GRC 8-917-1) Moehle, Hooper, Lubke.**
- Can download PDF online.

## Special Moment Frames

- Special Moment Frames have material requirements, Table 19.2.1.1\*.
- Concrete strength  $f'_c \geq 3$  ksi.
- Lightweight concrete  $f'_c \leq 5$  ksi, unless there is experimental evidence that structural members made with that lightweight concrete have toughness and strength equal to structural members made of normal weight concrete of the same strength.

\*This is correct – material specification have been moved to Chapter 19!



## Special Moment Frames

- Have special reinforcing steel requirements (20.2.2.5)
- Must be ASTM A706 Gr 60 **only!**
- ASTM A615 GR 40 or 60 **may** be used **if**
  - Actual yield strength from mill tests  $< f_y + 18$  ksi (retests cannot exceed  $f_y + 18$  ksi).
- **And** the  $f_{u,actual}/f_{y,actual} \geq 1.25$ .
- Transverse steel (hoops, ties, stirrups) specified yield strength ( $f_{yt}$ )  $\leq 100$  ksi.

## Special Moment Frames

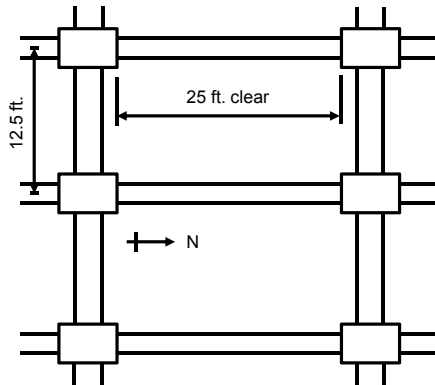
- Mechanical Splices 18.2.7.
  - Type 1
    - must develop  $1.25f_y$  (25.5.7)
    - May not be used within a distance  $2d$  from the face of a column or beam or from sections where yielding may occur due to inelastic displacement.
  - Type 2
    - must develop  $1.25f_y$  (25.5.7) and must develop the tensile strength of the bar
    - May be used anywhere

## Special Moment Frames

- Welded splices (18.2.8)
  - Must develop  $1.25f_y$
  - May not be used within a distance  $2d$  from the face of a column or beam in a special moment frame or from sections where yielding may occur due to inelastic displacement.
- Welding of stirrups, ties, inserts, etc. to longitudinal steel is forbidden!

**Design of Special Moment Frames Will Be Shown by  
Example**

## Design Example



Consider the portion of a building shown. This is a **plan view**.

We want to design a moment frame in the N/S direction.

Given: Concrete:  $f'_c = 6,000$  psi.  $\beta_1 = 0.75$

Steel: GR 60 A706

These meet SMF material requirements.

Note, if A615 is used, it must be tested to assure the yield is not too high!

## Reminder

### Recall:

$$\beta_1 c = a$$



Gravity

Where:

$c$  = depth of neutral axis

$a$  = depth of stress block for finding  $M_n$ .

For  $f'_c = 6$  ksi,  $\beta_1 = 0.75$

## Design Example

A note on the calculations:

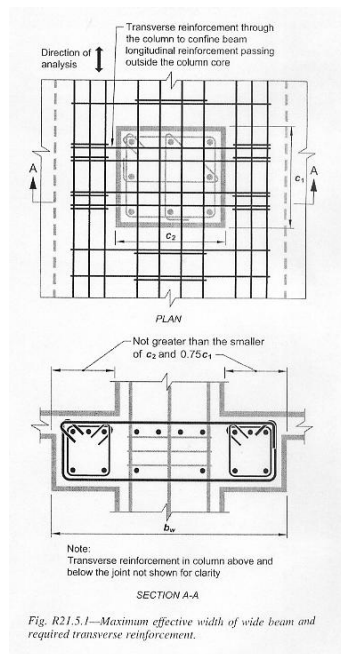
The calculation in this example were done in a spreadsheet. The results shown are rounded off to the correct number of significant digits.

However, the spreadsheet carries a large number of decimal places through the calculations. Thus, if you try to duplicate the calculations you might find slight differences due to round-off.

## Special Moment Frames – Flexural Members

- According to **NIST GRC 8-917-1**: Suggested spans are usually 20-30 feet.
  - Allows support of gravity and lateral loads without overloading adjacent columns or joints.
- 18.6.2.1 – The clear span,  $\ell_n$ , of a flexural member shall not be less than 4 times the effective depth.
- Width  $b_w$  at least the lesser of 0.3h and 10 inches.
- Projection of the beam width beyond the width of the supporting column on each side of supporting column on each side shall not exceed the lesser of  $c_2$  and  $0.75c_1$ .

## Special Moment Frames – Flexural Members



18.6.2.1 – The width of the member,  $b_w$  shall not be less than the smaller of 10 in or  $0.3h$ , where  $h$  is the overall depth of the beam.

The width of the member that projects beyond the edge of the column shall not exceed the lesser of  $c_2$  and  $0.75c_1$ :

$$b_w < c_2 + 2c_2 = 3c_2$$

$$b_w < c_2 + 1.5c_1$$

$c_2$  is the width of the supporting member and  $c_1$  is the width of the supporting member in the other direction.

R18.6.2 is shown in the figure from ACI 318-14.

## Design Example

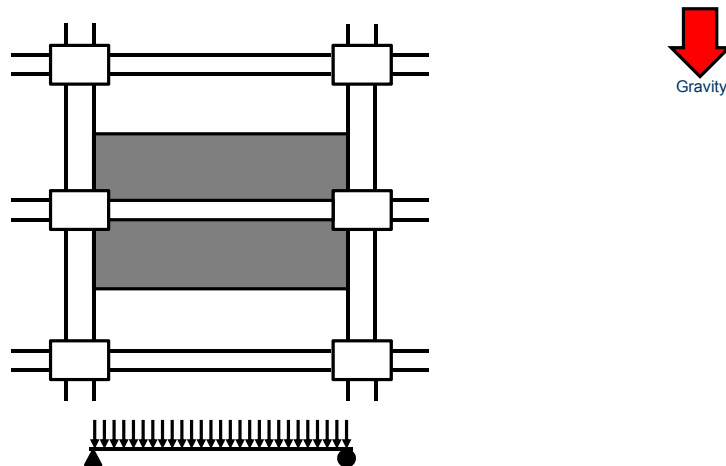
- The following slides show the results of analysis for the beam.
- The analysis was performed according to ASCE-7. The seismic analysis looked at:
  - North/South earthquake with 30% East/West
  - East/West earthquake with 30% North/South
- Because the analysis was done in this way, we can design the N/S frame independently of the E/W.

## Beam Loads

- The DL is 1.3 k/ft on the beam.
- The LL is 65 psf which translates to 0.812 k/ft on the beam.
- Assume the slab is a one way slab (because the length is 2 or more times the width).
- The beam is on the upper story a building. Analysis shows some roof live load effect,  $L_r$ , but it is orders of magnitude less than other loads, so it was ignored.
- Wind and Earthquake forces were found from ASCE 7.  
**Note** – Strength Level Forces are used!

## Beam Tributary Areas

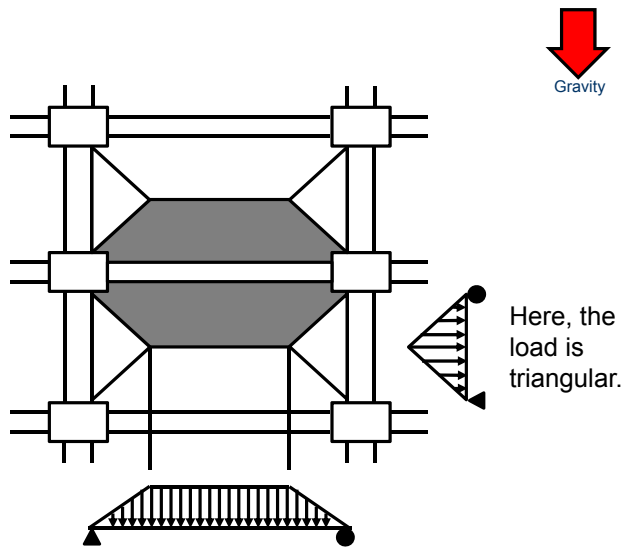
For a one way slab (this example), the tributary areas are shown:



## Beam Tributary Areas

Two way slabs:

If this had been a two way slab, the tributary areas would have looked like this.



## Beam Loads at Supports Unfactored

	Negative Moment Left k-ft	Shear Left k	Negative Moment Right k-ft	Shear Right k
D (Dead)	-75	16.5	-68.8	16
L (Live)	-39.1	10	-42.9	10.3
L <sub>r</sub> (Roof)	0	0	0	0
W (Wind +)	-53.8	4.3	54.1	4.3
W- (Wind -)	54.1	-4.3	-53.8	-4.3
E (Seismic +)	-203	15.9	194.6	15.9
E- (Seismic -)	194.6	-15.9	-203	-15.9

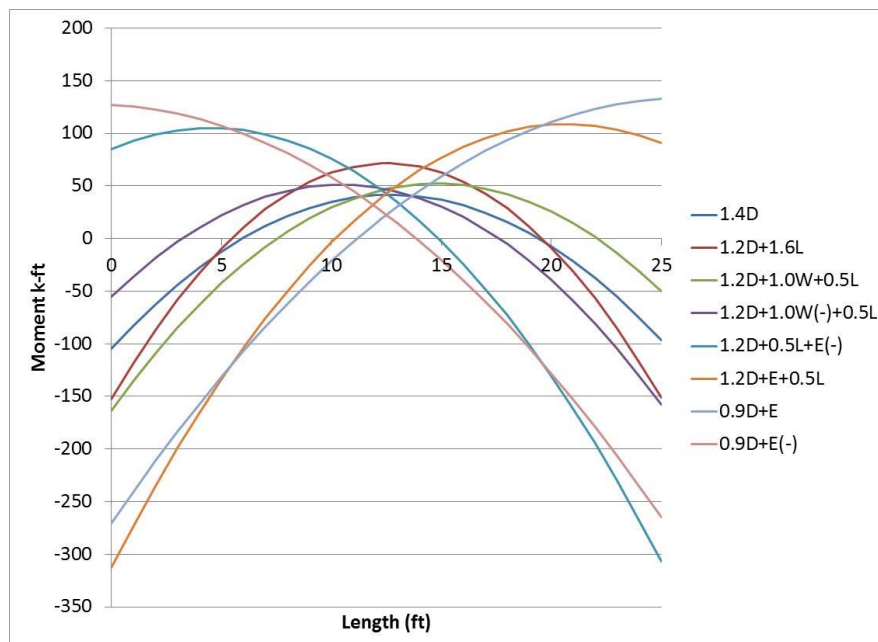
Must consider +/- Wind and Seismic.

## Applicable Load Combinations (5.3)

- $1.4D$
- $1.2D + 1.6L$
- $1.2D + 1.0W + 0.5L$ 
  - May use  $0.5L$  because  $LL < 100$  psf (5.3.1 note a)
- $1.2D + 1.0E + 0.5L$
- $0.9D + 1.0E$
- Other load combinations do not apply or clearly do not control.
- Must consider +/- for Seismic (E) and Wind
- W and E are Strength Level Loads. If Service Level Loads are used, use  $1.6W$  and/or  $1.4E$ .

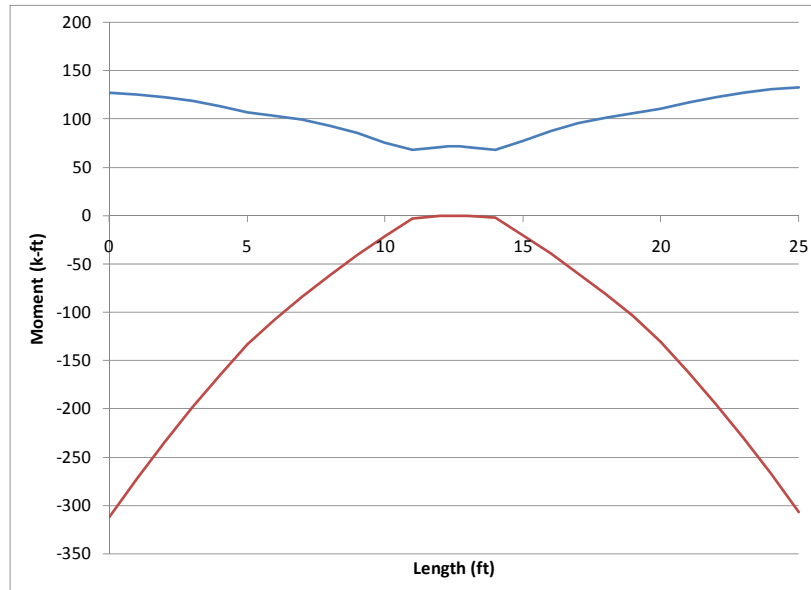


## Factored Load Moment Diagrams from Analysis



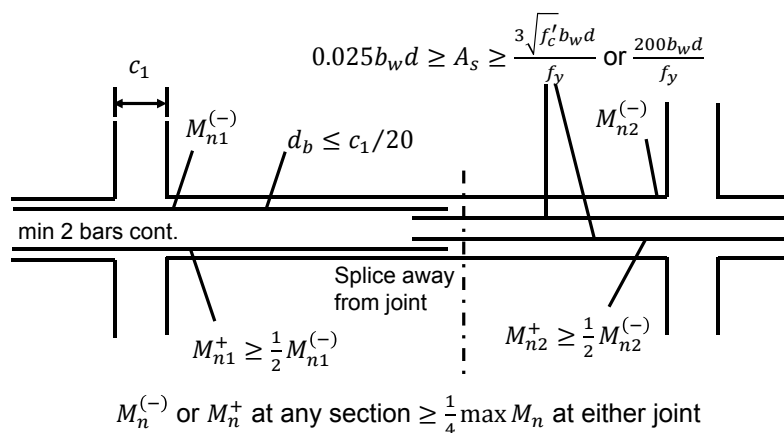


## Moment Envelope



$$M_u^{(-)} = 312.4 \text{ k} \cdot \text{ft}; M_u^{+} = 132.8 \text{ k} \cdot \text{ft}$$

## Longitudinal Steel Requirements

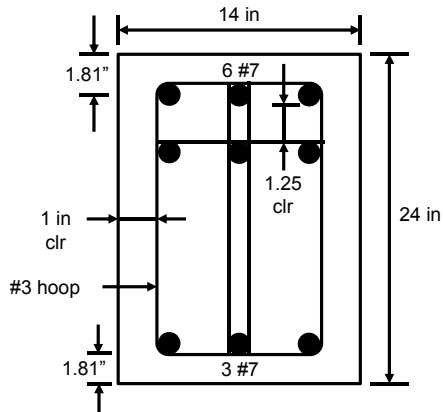


18.6.3 lists minimum steel and relative moment capacity requirements. These requirements are summarized in this figure.

(Adapted from **NIST GRC 8-917-1**)

## Proposed Section

Assume the beam will be 14 inches x 24 inches with the reinforcing shown:



Note the use of the #3 double hoop and hairpin. This is to assure confinement.

According to 18.6.2.1:

$$b_w > 10 \text{ in}$$

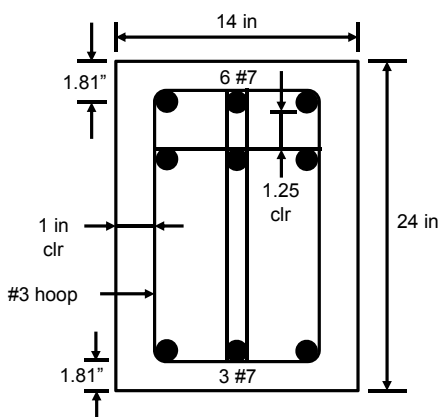
$$> 0.3h = 7.2 \text{ in}$$

So  $b_w = 14 \text{ in}$  is OK!

No overhang – so OK.

18.6.2.1 – The clear span,  $\ell_n$ , of a flexural member shall not be less than 4 times the effective depth. So  $d = 21.14''$ , so  $\ell_{n,min} = 84.6 \text{ in} = 7 \text{ ft} < 25 \text{ ft}$   
OK

## Proposed Section



18.6.4.7 – Factored axial load,  $P_u$ , may not exceed  $A_g f'_c / 10$  (if it does, additional ties are needed).

$$P_u < A_g f'_c / 10 \text{ so OK.}$$

The column will be  $c_1 = 18''$  and  $c_2 = 18''$ , so the maximum bar diameter for bars through the joint is  $c_1/20 = 18/20 = 0.9 \text{ in}$  (18.8.2.3). #7 is largest allowed.

(For LW concrete, the max. bar size =  $c_1/26$ )

### 18.6.4.7

If  $P_u > A_g f'_c / 10$ , provide hoops as required by 18.7.5.2 - 4\* over  $2h$  at each support and on  $2h$  at each side of any place likely to yield due to inelastic deformation from lateral loads.

Over the remaining length, hoops satisfying 18.7.5.2\* are required with a spacing the lesser of 6 times the smallest flexural bar diameters or 6 in.

If the cover exceeds 4 inches, additional transverse reinforcement must be provided with cover  $< 4$  inches and spacing  $< 12$  inches.

\* 18.7.5.2 - 4 details the requirements for columns. This will be shown later.

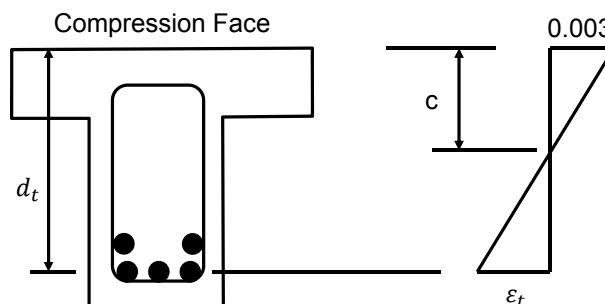
### Definition of Section Types (ACI 21.2.2)



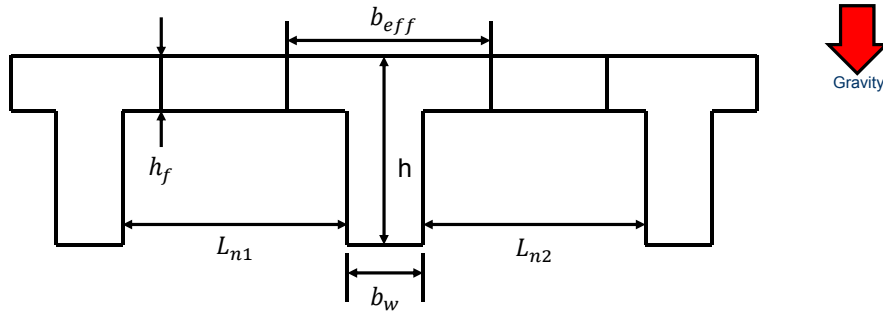
Strain in the extreme tensile steel, $\epsilon_t$	Type of Section	$\phi$
$\epsilon_t \leq f_y/E_s$	Compression Controlled $c/d_t \geq 3/5^*$	0.65 Tied Conf. 0.75 Spiral Conf.
$0.005 > \epsilon_t > f_y/E_s$	Transition $3/8 < c/d_t < 3/5^*$	Interpolated based on $\epsilon_t$
$\epsilon_t > 0.005$	Tension Controlled $c/d_t \geq 3/8$	0.9

\*For Grade 60 steel and prestressing steel, where  $f_y/E_s$  may be taken as 0.002.

For transition sections,  $\Phi$  is interpolated based on  $\epsilon_t$ .  
 Example:  $\epsilon_t = 0.004$   
 Section uses ties for transverse reinforcement ( $\Phi = 0.65$  at  $\epsilon_t = 0.002$ ).  
 $\Phi = 0.82$



## T Beam



There is a slab on the beam. ACI is **not** always clear about whether or not to include the slab for negative bending. However for positive and negative bending, the effective flange width is given by (6.3.2.1):

For “T” beams with two overhanging flanges

$$b_{eff} = b_w + \frac{L_{n1} + L_{n2}}{2}$$

$$= \frac{Span}{4} + b_w$$

$$= b_w + 16h_f$$

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Note: Change in 2014! This was:  $\frac{Span}{4}$

For “T” beams with an overhang on one side only

$$b_{eff} = b_w + \frac{L_{n1}}{2}$$

$$= \frac{Span}{12} + b_w$$

$$= b_w + 6h_f$$

71

## T Beam

The flange width is the smallest of:

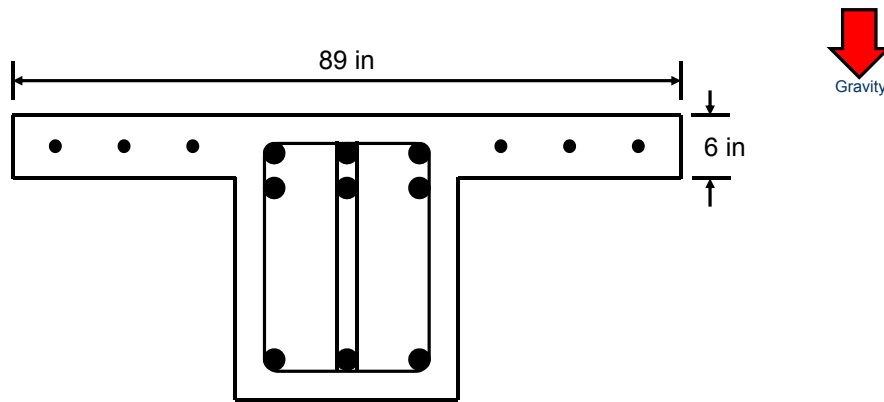
$$Span/4 + b_w = 25 \text{ ft (12)}/4 + 14 = 89 \text{ in} \quad \text{controls}$$

$$c/c \text{ distance between beams} = 12.5 \text{ ft} = 150 \text{ in}$$

$$b + 16 h_f = 14 \text{ in} + 16(6 \text{ in}) = 110 \text{ in}$$

Assume the slab has #3 @ 12, so 6 bars in flange (picture on next slide).

## T Beam



So, find “d” for the negative moment section. Assume the #3 bars are at 3 inches from the top:

$$y_{bs} = \frac{6(0.11 \text{ in}^2)(3 \text{ in}) + 3(0.6 \text{ in}^2)(1.81 \text{ in}) + 3(0.6 \text{ in}^2)(3.93 \text{ in})}{0.66 \text{ in}^2 + 3.60 \text{ in}^2}$$

$$y_{bs} = 2.89 \text{ in}$$

$$d = 24 - 2.89 \approx 21.1 \text{ in}$$

## Negative Moment Capacity Ignoring Slab



First layer is 1" (clear) + 0.375 (hoop) + 0.875"/2 (bar) = 1.81";  $d_t = 24 - 1.81 = 22.2 \text{ in}$  (distance to extreme tensile steel)

Second Layer is 1.81" + 1.25" (clear) + 0.875" (bar) = 3.93"

$$A_s = 6 \times 0.6 \text{ in}^2 = 3.60 \text{ in}^2$$

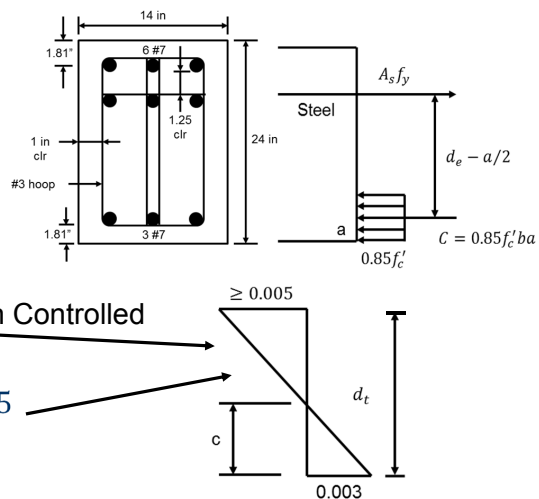
$$d = 24 - \frac{3(0.6)1.81 + 3(0.6)3.93}{3.60} = 21.12 \text{ in}$$

$$a = \frac{A_s f_y}{0.85 f'_c b} = \frac{3.60 \text{ in}^2 (60 \text{ ksi})}{0.85 (6 \text{ ksi}) (14 \text{ in})} = 3.02 \text{ in}$$

$$c = \frac{a}{\beta_1} = \frac{3.02}{0.75} = 4.03 \text{ in}$$

$$\frac{c}{d_t} = \frac{4.03}{22.2} = 0.182 < 0.375$$

$$\text{Or } \epsilon_s = \left( \frac{d_t}{c} - 1 \right) 0.003 = 0.013 > 0.005$$



## Reminder

$\varepsilon_t \geq 0.005$  Tension control  $\Phi = 0.9$

$\varepsilon_t \geq \varepsilon_y$  Compression control  $\Phi = 0.65$  tied

$\Phi = 0.75$  spiral

Transition, interpolate  $\Phi$  based on  $\varepsilon_t$ .

$\phi = 0.9$  Tension controlled

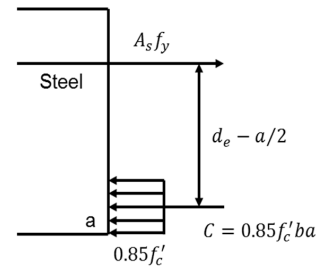
$$\phi M_n = \phi A_s f_y \left( d - \frac{a}{2} \right)$$

$$\phi M_n = 0.9(3.60 \text{ in}^2)60 \text{ ksi} \left( 21.12 - \frac{3.02}{2} \right) = 3,812 \text{ k-in}$$

$$\phi M_n = 317.7 \text{ k-ft}$$

$$M_u = 312.4 \text{ k-ft} < \phi M_n \text{ OK}$$

$M_u$  is from the moment envelope shown previously. The section is adequate for negative moment.



## Negative Moment Strength Including Slab Steel

$$a = \frac{(0.66 + 3.60) \text{ in}^2 (60 \text{ ksi})}{0.85(6 \text{ ksi})14 \text{ in}} = 3.58 \text{ in}$$

$$c = \frac{3.58}{0.75} = 4.77 \text{ in}; \frac{c}{d_t} = \frac{4.77 \text{ in}}{22.2 \text{ in}} = 0.22 < 0.375; \phi = 0.9$$

$$\phi M_n = 0.9(4.26 \text{ in}^2)(60 \text{ ksi}) \left( 21.1 \text{ in} - \frac{3.58 \text{ in}}{2} \right)$$

$$\phi M_n = 4,935 \text{ k-in} = 370 \text{ k-ft} > M_u$$



## Positive Moment

The positive moment at the support is 132.8 k-ft.



BUT 16.2.3.2 requires that  $\phi M_n^{(+)}$  be at least  $0.5 \phi M_n^{(-)}$ .

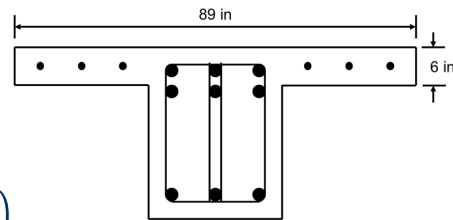
(Section is tension controlled by inspection; it has the same cross section, but less steel than the tension controlled negative moment section.)

$$a = \frac{3(0.6 \text{ in}^2)60 \text{ ksi}}{0.85(6 \text{ ksi})89 \text{ in}} = 0.24 \text{ in}$$

$$d = 24 - 1.81 \text{ in} = 22.2 \text{ in}$$

$$\phi M_n = 0.9(1.8 \text{ in}^2)(60 \text{ ksi}) \left( 22.2 \text{ in} - \frac{0.24 \text{ in}}{2} \right)$$

$$\phi M_n = 2,146 \text{ in} - \text{k} = 179 \text{ k} - \text{ft} > M_u = 132.8 \text{ k} - \text{ft}$$



## Slab

If the slab is ignored,  $0.5 \phi M_n^{(-)} = 159 \text{ k} - \text{ft}$ , so  $\phi M_n^{(+)}$  is greater.

If slab is counted,  $0.5 \phi M_n^{(-)} = 185 \text{ k} - \text{ft}$ , so  $\phi M_n^{(+)}$  is slightly less.

However, the code is not clear about counting the slab steel. The **only** time the code **requires** counting the slab steel is when determining the relative strengths of the beam and column.

**NIST GRC 8-917-1** and several text books indicate that both methods – count or ignore the slab – are used. We will ignore the slab unless the code requires us to count it. However, if you choose to include the slab it is not incorrect.

## Maximum and Minimum Steel 18.6.3.1

$$\rho_{w,max} = 0.025 \quad 18.6.3.1$$

$$\rho_w = \frac{A_s}{b_w d}$$

$$\rho_{w,min} = \frac{3\sqrt{f'_c}}{f_y} > \frac{200}{f_y} \quad 9.6.2.1$$
$$\frac{200}{f_y} = \frac{200}{60,000} = 0.0033$$
$$\frac{3\sqrt{f'_c}}{f_y} = \frac{3\sqrt{6,000}}{60,000} = 0.004$$

Where  $b_w$  is the **web** width and  $d$  is the effective depth from compression face to centroid of all tensile steel.



Gravity  
Provisions in the box apply to gravity loads

$$0.025 > \rho_{w,negative} = \frac{3.60 \text{ in}^2}{14 \text{ in}(21.12 \text{ in})} = 0.012 > 0.004$$

$$0.025 > \rho_{w,positive} = \frac{1.80 \text{ in}^2}{14 \text{ in}(22.2 \text{ in})} = 0.006 > 0.004$$

In addition, 18.6.3.1 requires **at least 2 bars** be continuous top and bottom!

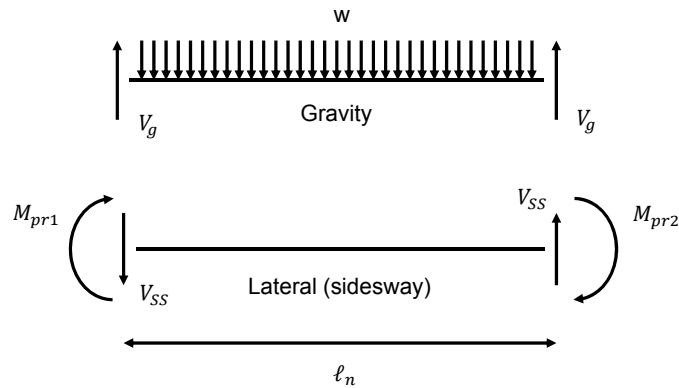
## Beam

The beam meets all requirements. We only designed steel at the supports. We do need to check:

- 1) Adequate along the entire beam? Yes. The end moments are maximum for the entire beam **in this example**.
- 2) Is the strength at **any** section  $\geq 0.25M_{n,max}$  at support? **Yes**. We do not change the steel so this is met.

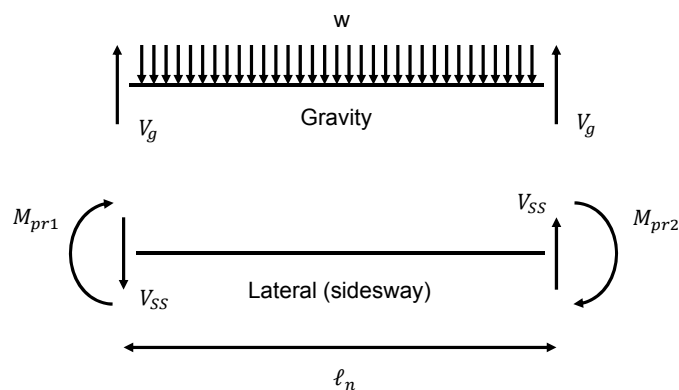


## Special Seismic Frame Philosophy



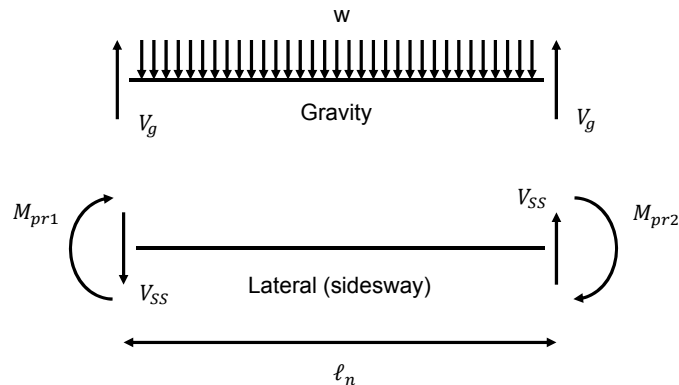
As with IMF, shear in the beam comes from two places: the gravity loads and the lateral load moment (sideways).

## Special Seismic Frame Philosophy



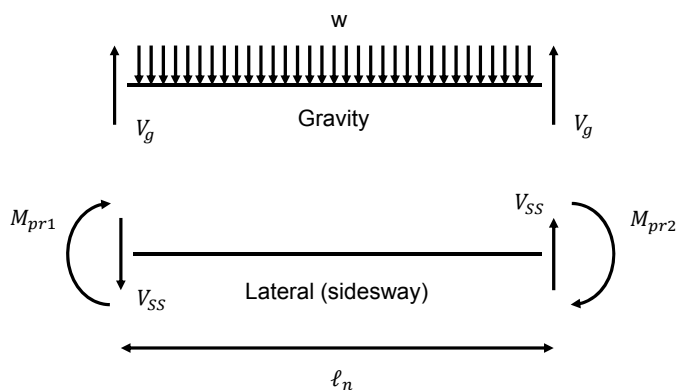
However, there is a difference in how the shear is found. For IMF we used the nominal moment capacity,  $M_n$ , which assumes that  $f_y$  is exactly as specified (e.g. exactly 60 ksi). But specified yield is a **minimum**. Real steel is stronger!

## Special Seismic Frame Philosophy



To prevent a shear failure before yielding the flexural steel, the code requires that the **minimum** design shear forces due to lateral loads in SMFs be based on the “probable” flexural strength of the joints. (18.6.5.1)

## Special Seismic Frame Philosophy

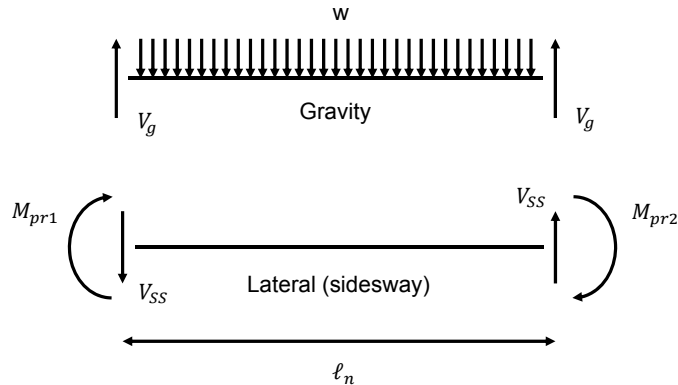


This is why ACI limits the yield strength of steel in seismic frames. A706 specifies a limited  $f_y$ . If A615 is used, the test yield strength is limited to  $1.25f_y$ .

$$M_{pr} = M_n \text{ with } f_s = 1.25f_y \quad (M_{pr} \neq 1.25M_n)$$

That is: the probable moment is calculated using 125% of the specified yield strength! Because “a” changes, it’s not 1.25  $M_n$ . Also,  $\Phi = 1.0$ .

## Special Seismic Frame Philosophy

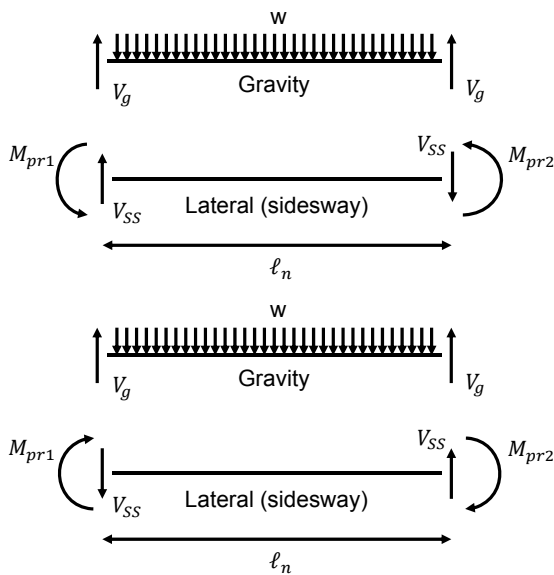


$$V_e = V_g + V_{SS} = \frac{w_u \ell_n}{2} + \frac{M_{pr1} + M_{pr2}}{\ell_n}$$

$\ell_n$  is the clear span (face/face support) and  $w_u$  is the **factored** gravity loads.

$w = 1.2D + 1.0L + 0.2S$  (note, this load combination in 5.3 includes E, but that is calculated from  $M_{pr}$ )

### Note!



You **must** consider sideways in both directions and design for the highest shear!

Remember, the longitudinal reinforcement at the left end could be different from the right end!

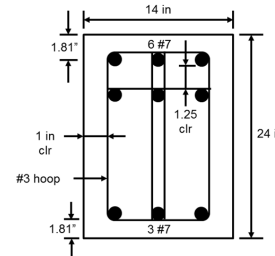
## Negative Probable Moment

The probable moment is found by assuming the steel strength is  $1.25f_y$  and taking  $\phi = 1$ . Since this a probable moment and phi is assigned 1, we do not need to check tension control.

$$A_s = 3.60 \text{ in}^2$$

$$d = 21.12 \text{ in}$$

$$a = \frac{A_s(1.25f_y)}{0.85f'_c b} = \frac{3.60 \text{ in}^2(1.25)(60 \text{ ksi})}{0.85(6 \text{ ksi})(14 \text{ in})} = 3.78 \text{ in}$$



$$M_{pr} = 3.60 \text{ in}^2(1.25)(60 \text{ ksi}) \left( 21.12 \text{ in} - \frac{3.78 \text{ in}}{2} \right) = 5,192 \text{ k} - \text{in}$$

$$M_{pr} = 432.6 \text{ k} - \text{ft}$$

Note: You can't just multiply  $M_n$  by 1.25 because "a" changes, so the moment arm changes.

## Negative Probable Moment

Remember, at the joints, the slab steel goes into tension when there is negative moment. The ACI code does **not** say how to handle this steel in seismic applications!

In this case, we will **not** consider the slab steel in finding the negative  $M_{pr}$  for beam shear. This is consistent with several design examples in text books. This is not a universally applied concept.

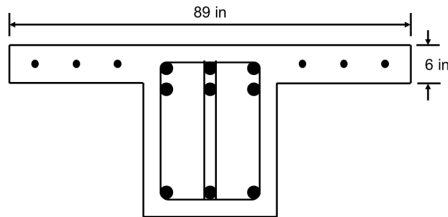
There are places where we will be **required** to consider the slab steel.

## Positive Probable Moment

$$a = \frac{3(0.6 \text{ in}^2)(1.25)60 \text{ ksi}}{0.85(6 \text{ ksi})89 \text{ in}} = 0.30 \text{ in}$$

$$\phi M_n = (1.8 \text{ in}^2)(1.25)(60 \text{ ksi}) \left( 22.2 \text{ in} - \frac{0.30 \text{ in}}{2} \right)$$

$$\phi M_n = 2,976 \text{ in} - \text{k} = 248 \text{ k} - \text{ft}$$



We do need to consider the slab width for positive bending.

## Beam Shear

The controlling load case is:

$$1.2D + 0.5L + 1.0 E$$

We can use 0.5L because 5.3.3 allows it if this is not an area of public assembly, a garage or  $L > 100$  psf.

For E, we calculate the shear from the probable moments.

## Beam Shear

The controlling load case is:

Uniform Gravity Load

$$1.2D + 0.5L = 1.2(1.3) + 0.5(0.812) = 1.97 \text{ k/ft}$$

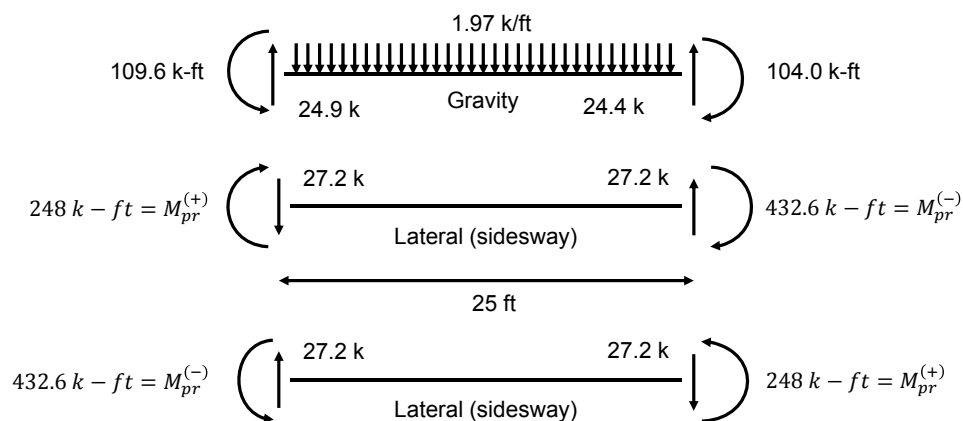
Left

$$1.2M_D + 0.5M_L = 1.2(75) + 0.5(39.1) = 109.6 \text{ k-ft}$$

Right

$$1.2M_D + 0.5M_L = 1.2(68.8) + 0.5(42.9) = 104 \text{ k-ft}$$

## Beam Shear



$$V_e = (432.6 \text{ k-ft} + 248 \text{ k-ft}) / 25 \text{ ft} = 27.2 \text{ k}$$

## Beam Shear – Basics



$$\phi V_u \leq \phi(V_c + V_s)$$

$$V_c = 2\sqrt{f'_c} b_w d$$

If minimum shear steel not provided:

$$\sqrt{f'_c} \leq 100 \text{ psi}$$

$$V_s = \frac{A_v f_y d}{s}$$

$$V_{s,required} \leq 8\sqrt{f'_c} b_w d$$

$V_u$  = Factored Shear  
 $V_c$  = Concrete Shear Strength  
 $V_s$  = Stirrup Strength  
 $b_w$  = Web Width  
 $d$  = Effective Depth  
 $A_v$  = Area of Stirrup Crossing Shear Plane  
 $f_y$  = Stirrup Yield Strength  
 $s$  = Stirrup Spacing

If not true, resize the section! 22.5.1.2.

For gravity loads,  $V_u$  can be taken at “d” from the face of the support if the support reaction, in the direction of the applied shear, induces compression in the end regions; loads are applied at or near the top of the member; there is no point load between the critical section and the support. 9.4.3.2 (beams) 7.4.3.2 (slabs)

## Beam Shear

$$V_u = 24.9 \text{ k} + 27.2 \text{ k} = 52.1 \text{ k}$$

$$V_e = 27.2 > \frac{1}{2} V_u = 26.1 \text{ k}$$

$$\phi V_u \leq \phi(V_c + V_s)$$

$$V_{s,req} = \frac{V_u - V_c}{\phi} = \frac{52.1 \text{ k} - 0}{0.75} = 69.5 \text{ k}$$

Check:

$$8\sqrt{6,000 \text{ psi}}(14 \text{ in})(21.12 \text{ in}) = 183,000 \text{ lbs}$$

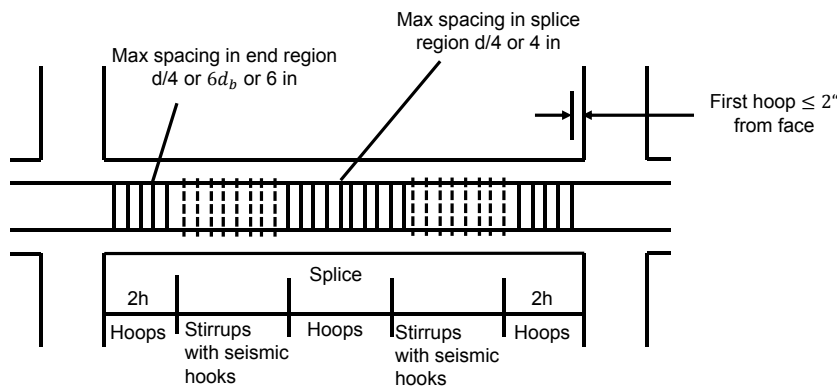
$$183 \text{ k} > 69.5 \text{ k} \text{ OK}$$

If not true, resize the section! 22.5.1.2

18.6.5.1 this check is at the **face** of the support (not d from face).

**If** the shear due to earthquake is greater than  $\frac{1}{2}$  the total shear and  $P_u < A_g f'_c / 20$ , we must assume the concrete contribution = 0 (18.6.5.2).

## Beam Shear



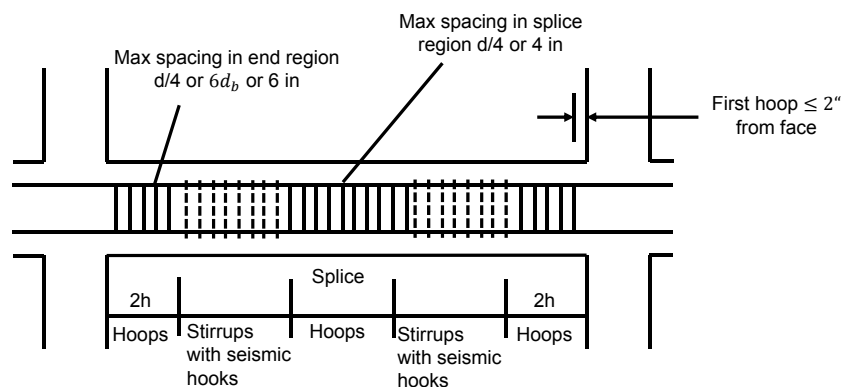
Note: ACI 318 says hoops over a distance of twice the member depth. Some references use  $2d$ , some  $2h$ !

Adapted from **NIST GRC 8-917-1**. Updated to ACI 318-14.

Requirements for transverse reinforcement in beams.

Stirrups have seismic hooks and follow regular spacing rules. Hoops confine end and splice regions.

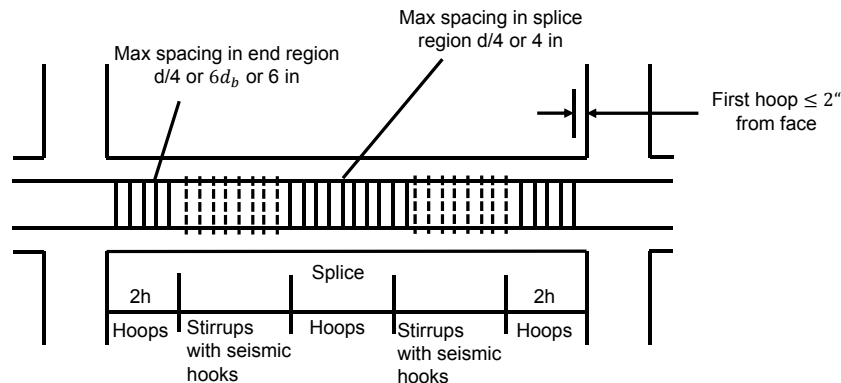
## Special Moment Frames – Flexural Members



18.6.4 Spacing requirements for distances within  $2h$  of the support **or** over a distance  $2h$  on either side of a place where flexural yielding is expected to occur due to lateral displacements beyond the elastic range:  $d/4$ ;  $6d_b$  or 6 in. For  $d_b$  use the smallest flexural bar, but exclude skin reinforcing (used for crack control).



## Special Moment Frames – Flexural Members



18.6.3.3 Spacing requirements for splices:  $d/4$ ; 4 in. Lap splices cannot be used within joints, within  $2h$  of the support or over a distance  $2h$  on either side of a place where flexural yielding is expected to occur due to lateral displacements beyond the elastic range.

## Beam Shear 21.5.3

Maximum spacing of hoops within  $2h$  of the face.

$$s_{max} = d/4 = 21.12/4 = 5.3 \text{ in}$$

$$= 6d_b = 8(7/8) = 5.3 \text{ in}$$

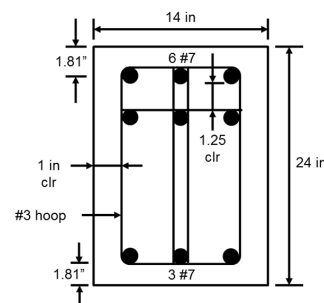
$$= 6 \text{ in}$$

#3 hoop has 4 bars across the shear plane,

$$\text{so } A_v = 4(0.11 \text{ in}^2) = 0.44 \text{ in}^2.$$

Try #3 hoops at 5 inches c/c (Eq'n 22.5.10.5.3):

$$V_s = \frac{A_v f_y t d}{s} = \frac{0.44 \text{ in}^2 (60 \text{ ksi}) 21.1 \text{ in}}{5 \text{ in}} = 112 \text{ k} > 69.5 \text{ k}$$



## Beam Shear



$A_{v,min}$  here also applies to gravity loads

Minimum shear steel (9.6.3.3):

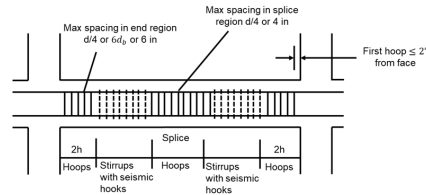
$$A_{v,min} = 0.75 \sqrt{f'_c} \frac{b_w s}{f_{yh}} = 0.75 \sqrt{6,000} \frac{(14 \text{ in})(5 \text{ in})}{60,000 \text{ psi}} = 0.067 \text{ in}^2 \text{ Controls}$$

$$A_{v,min} = \frac{50 b_w s}{f_{yh}} = \frac{50(14 \text{ in})(5 \text{ in})}{60,000 \text{ psi}} = 0.058 \text{ in}^2$$

$$A_v = 0.44 \text{ in}^2 > 0.067 \text{ in}^2 \text{ OK}$$

So #3 at 5 in over the first 2h = 48 in.

Start first hoop s/2, from face. Use 2" from face (18.6.4.4) and 11 hoops. This takes the stirrups 52" from the face on each side (11 hoops create 10 spaces at 5 in each).



## Beam Shear



At 52 inches from the face ( $w = 1.97 \frac{\text{k}}{\text{ft}} = \text{change in } V$ ):

$$V_u = 52.1 \text{ k} - \frac{1.97 \text{ k}}{\text{ft}} \frac{52 \text{ in}}{12} = 43.6 \text{ k}$$

$$V_c = 2 \sqrt{f'_c} b_w d = \frac{2 \sqrt{6,000 \text{ psi}} (14 \text{ in}) (21.1 \text{ in})}{1,000} = 45.8 \text{ k}$$

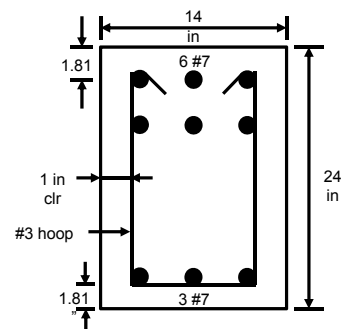
$$V_{s,req} = \frac{43.6 \text{ k} - (0.75) 45.8 \text{ k}}{0.75} = 12.3 \text{ k} < 4 \sqrt{f'_c} b_w d$$

$$s_{max} = \frac{d}{2} \approx 10 \text{ in} < 24 \text{ in } 18.6.4.6$$

$$V_s = \frac{0.22 \text{ in}^2 (60 \text{ ksi}) (21.1 \text{ in})}{10 \text{ in}} = 27.9 \text{ k} > 12.3 \text{ k}$$

Outside of 2h from the face, we can use  $V_c$  (18.6.5.2).

Use #3 seismic stirrups with 10 inch spacing.

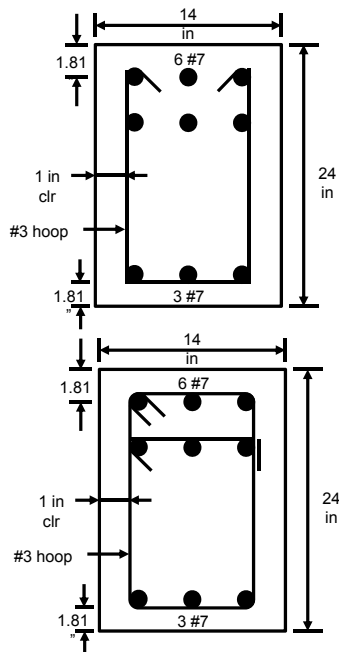


If  $V_s$  required is between

$4 \sqrt{f'_c} b_w d$  and

$8 \sqrt{f'_c} b_w d$ ;  $s_{max}$  is  $d/4 < 12 \text{ in}$ .

## Beam Shear



Outside of  $2h^* = 48$  inches, use of stirrups with seismic hooks is permitted.

Using the closed hoops and a hairpin, as shown, supports the primary reinforcement on both tension and compression faces and is a better detail.

*18.6.4.2 requires primary flexural reinforcing bars closest to the tension and compression faces to be supported according to 25.7.2.3 and 4 where hoops are required (within the  $2h$  length at both ends). Spacing of transversely supported bar  $< 14$  in.*

Skin reinforcement does not need lateral support.

\* Some design examples use  $2d$ .

## Beam Splice

Beam splices are either Class A or B (25.5.2.1).

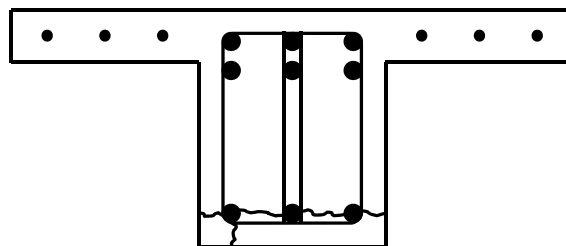
Class A – Splice length = development length  $\ell_d$

Class B – Splice length =  $1.3\ell_d$

To find  $\ell_d$  25.4.2.3:

$$K_{tr} = \frac{40A_{tr}}{sn}$$

$$\ell_d = \frac{3}{40} \frac{f_y}{\lambda \sqrt{f'_c}} \frac{\Psi_t \Psi_e \Psi_s}{\left(\frac{c_b + K_{tr}}{d_b}\right)} d_b$$



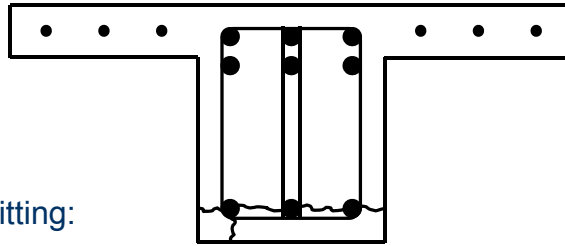
This is also how to find development length for gravity loads.

## Beam Splice

$$K_{tr} = \frac{40A_{tr}}{sn}$$

$$\ell_d = \frac{3}{40} \frac{f_y}{\lambda \sqrt{f'_c}} \frac{\Psi_t \Psi_e \Psi_s}{\left(\frac{c_b + K_{tr}}{d_b}\right)} d_b$$

To find  $K_{tr}$  consider a plane of splitting:



$A_{sh}$  = area of stirrup crossing the plane of splitting

$F_{sh}$  = stirrup yield

$s$  = stirrup spacing

$n$  = # of bars being developed

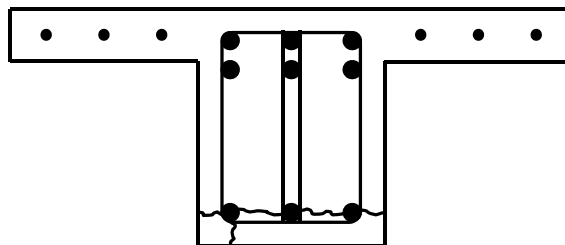
Check  $K_{tr}$  for each plane of splitting.

## Beam Splice

$$K_{tr} = \frac{40A_{tr}}{sn}$$

$$\ell_d = \frac{3}{40} \frac{f_y}{\lambda \sqrt{f'_c}} \frac{\Psi_t \Psi_e \Psi_s}{\left(\frac{c_b + K_{tr}}{d_b}\right)} d_b$$

$$\frac{c_b + K_{tr}}{d_b} \leq 2.5$$



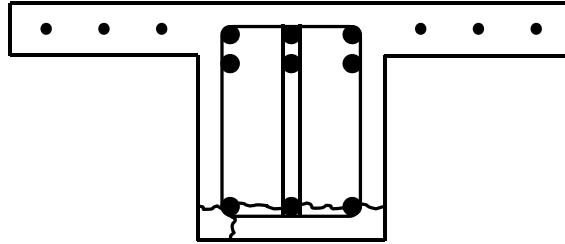
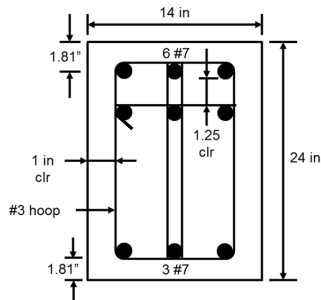
The term  $c_b$  is the smaller of the distance from the center of a bar to the nearest surface or  $\frac{1}{2}$  the c/c distance between bars.

$\Psi_e$  is the epoxy bar factor,  $\Psi_t$  is the top bar factor and  $\Psi_s$  is the size factor.  $\lambda$  is the lightweight factor. (25.4.2.4)

The term  $f_y$  is the longitudinal bar yield and  $f'_c$  is the concrete strength.

Finally,  $d_b$  is the bar diameter.

## Beam Splice



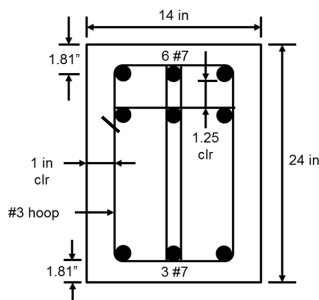
$$c_b = 1 + 0.375 + \frac{1}{2} \left( \frac{7}{8} \right) = 1.81 \text{ in} \leftarrow \text{controls}$$

$$c_b = \frac{1}{2} \frac{[14 - 2(1 + 0.375) - 2(\frac{1}{2})(\frac{7}{8})]}{2 \text{ spaces}} = 2.59 \text{ in}$$

For the horizontal splitting plane,  $n = 3$ ,  $A_{sh} = 4(0.11 \text{ in}^2) = 0.44 \text{ in}^2$ .

For the vertical splitting plane,  $n = 1$ ,  $A_{sh} = 0.11 \text{ in}^2$ ;  $f_{yh} = 60 \text{ ksi}$ ;  $s = 4$  inches for both planes.

## Beam Splice



The splice must be Class B (25.5.2.1) as  $A_{s,prov} < 2A_{s,req}$ ; cannot be within  $2h$  of the face (18.6.3.3) and must have hoops as shown over splice at  $s = d/4 < 4$  in.

$s = 4$  inches controls.

$$K_{tr} = \frac{40(0.44 \text{ in}^2)}{4 \text{ in}(3 \text{ bars})} = 1.47 \text{ or } K_{tr} = \frac{40(0.11 \text{ in}^2)}{4 \text{ in}(1 \text{ bar})} = 1.1$$

$$\frac{c_b + K_{tr}}{d_b} = \frac{1.81 + 1.1}{0.875} = 3.32 > 2.5$$

$$\ell_d = \frac{3}{40} \frac{60,000(1.3)}{\sqrt{6,000}(2.5)} (0.875) = 26.4 \text{ in}$$

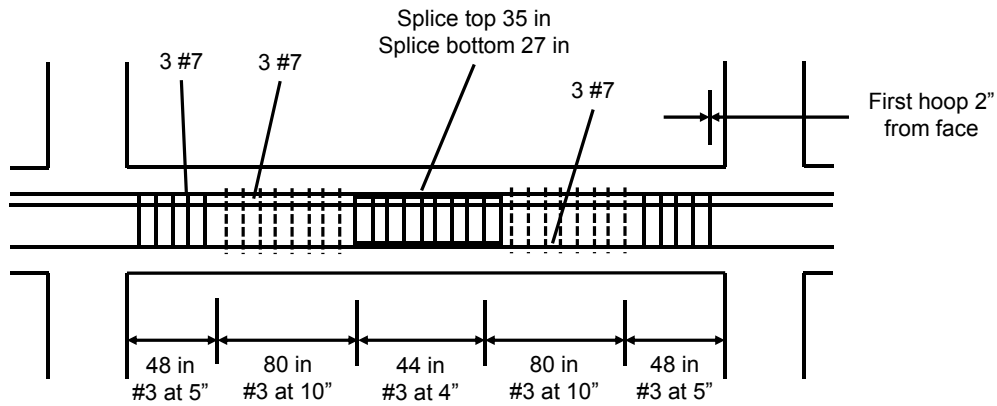
$1.3\ell_d = 1.3(26.4) \approx 35$  in Class B splice

The only  $\Psi$  for the top #7 bars is the top bar factor = 1.3. All other  $\Psi$  values are 1 as is  $\lambda$ .

For the bottom #7, take out the top bar factor.

$$\ell_d = \frac{35}{1.3} \approx 27 \text{ in}$$

## Final Beam Design



## Column

The columns are 10 feet long (clear span).

From analysis, the column loads are as shown. The moments have been magnified for slenderness effects (Ch 6 covers slenderness).

	P kips	M k-ft
D	88	8.1
L	36	-10.1
L <sub>r</sub>	13	-1.5
W	3.6	103
E	50	340

## Column

The applicable load combinations are the same as for the beam. The controlling combinations are:

$$P = 1.2D + 0.5L + E = 174 \text{ k}$$

$$P = 0.9D - E = 29.2 \text{ k}$$

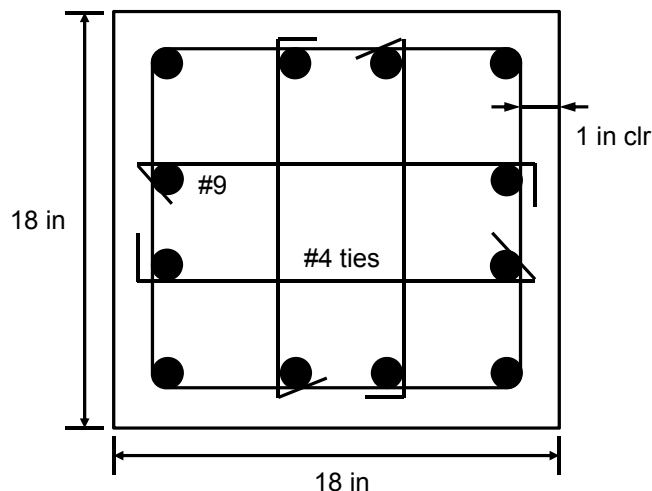
$$M = 1.2D + 0.5L + E = 345 \text{ k-ft}$$

$$M = 0.9D - E = 333 \text{ k-ft}$$

Note: Simple consideration of maximum and minimum  $P$  with associated  $M$  or maximum and minimum  $M$  with associated  $P$  may be inadequate. All combinations of  $P$  and  $M$  must be checked. In this problem, the controlling cases were clear from inspection.



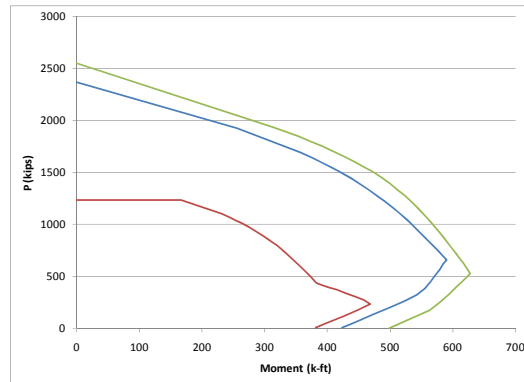
## Column



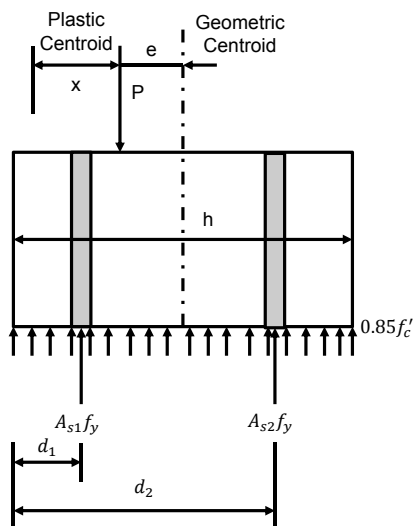
Use an 18 x 18 column with 12 #9 bars. The ties are #4 bars. Check 18.7.4.1:  $\rho_g = 12(1)/18^2 = 0.037$ ; this is between 0.01 and 0.06 as required. (For gravity the limits are 0.01 and 0.08).

## Column

Now we have to construct 3 separate interactions diagrams. First, we must construct the nominal interaction diagram with  $f_y = 60$  ksi. Then, we reduce that by phi to get the design interaction diagram. Finally, we recalculate the nominal diagram with  $1.25f_y = 75$  ksi to get the probable interaction diagram.



## Column



First, find the plastic centroid. This is where the load “P” must be placed such that there is no moment.

The entire cross section is stressed to  $0.85f'_c$  and the steel is assumed to have a stress of  $f_y$ . Find P (next slide). Next, sum the moments. For a rectangular column:

$$Px = 0.85f'_c(A_c) \left(\frac{h}{2}\right) + \sum A_s f_y d$$

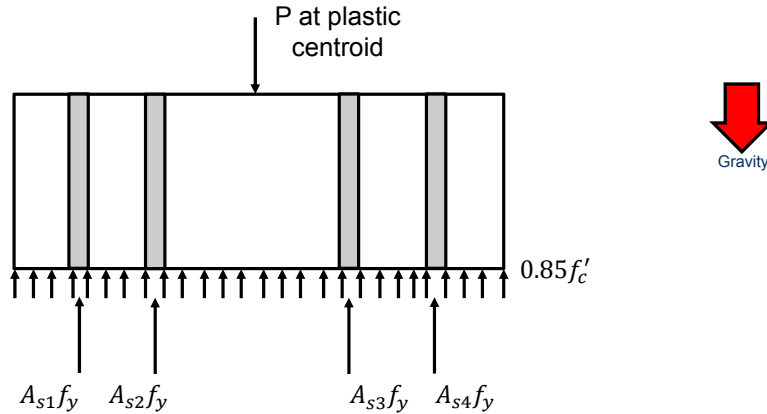
If the column is symmetrical, the plastic centroid is at the geometric centroid.





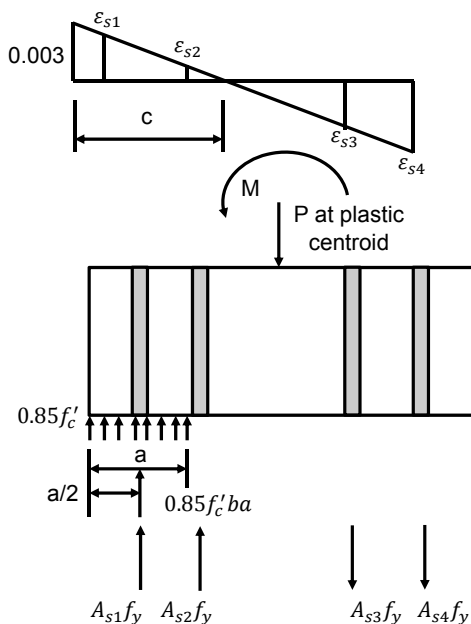
## Column

Now, find  $P_n$ . Assume the entire cross section is stressed to  $0.85f'_c$  and the steel is assumed to have a stress of  $f_y$ .



$$P = 0.85(6 \text{ ksi})(324 \text{ in}^2 - 12 \text{ in}^2) + 12 \text{ in}^2(60 \text{ ksi}) = 2,311 \text{ k}$$

## Column



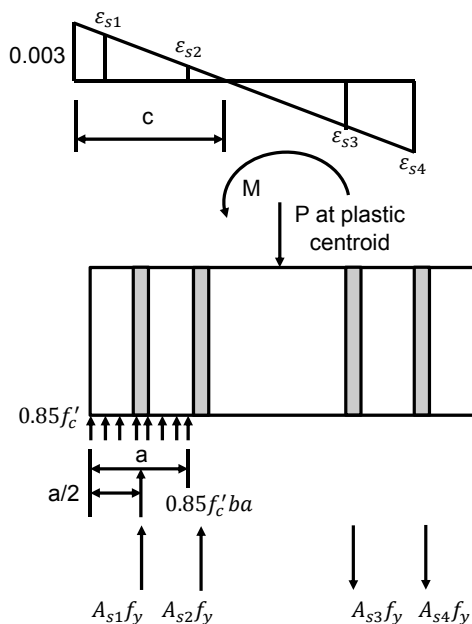
For the rest of the diagram,

- 1) Set the extreme compressive strain = 0.003
- 2) Assume a value of "c".
- 3)  $a = \beta_1 c \leq h$
- 4) Using similar triangles, find the strain in each layer of steel.
- 5) Steel stress,  $f_s = E_s \varepsilon_s \leq f_y$
- 6) Sum the forces to get P
- 7) Sum the moments about the plastic centroid to get M.
- 8) Repeat

## Column

c (in)	$\epsilon_{s4} = \epsilon_t$	P kips	M k-ft	Comment
18	-0.0003	1,690	357	c = h
16	0	1,495	423	Zero tension in extreme tensile steel
12	+0.001	1,040	528	Tens Steel $\approx$ 30ksi
9.4	+0.0021	660	590	Balanced ( $\epsilon_t = \epsilon_y$ )
6	+0.005	261	522	Tens Control ( $\epsilon_t = 0.005$ )
4.2	+0.008	0	423	Pure Bending (P = 0)

## Column



### Sample Calculation



Use  $c = 10$

$$a = \beta_1 c = 0.75(10) = 7.5 \text{ in} < h$$

$$F_c = 0.85(6 \text{ ksi})(7.5 \text{ in})(18 \text{ in}) = 689 \text{ k}$$

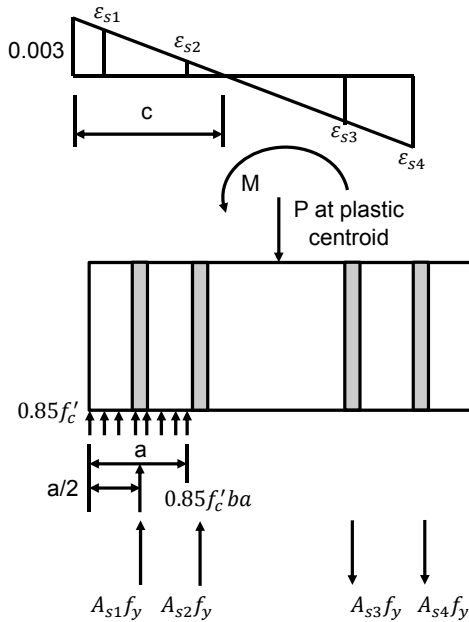
$$\epsilon_{s4} = 0.003 \left( \frac{16}{10} - 1 \right) = 0.0018$$

$$f_{s4} = 29,000 \text{ ksi}(0.0018) = 52.2 \text{ ksi}$$

$$\epsilon_{s3} = 0.003 \left( \frac{11.3}{10} - 1 \right) = 0.00039$$

$$f_{s3} = 29,000 \text{ ksi}(0.00039) = 11.3 \text{ ksi}$$

## Column



### Sample Calculation



Use  $c = 10$

$$\epsilon_{s2} = 0.003 \left( \frac{6.7}{10} - 1 \right) = -0.001$$

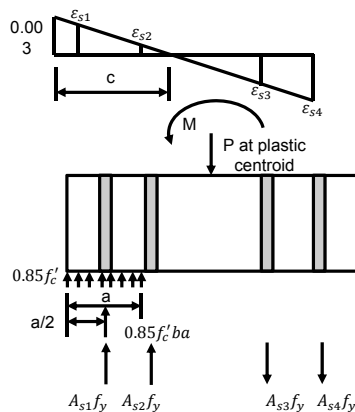
$$f_{s2} = 29,000 \text{ ksi}(-0.001) = -29 \text{ ksi}$$

$$\epsilon_{s1} = 0.003 \left( \frac{2.0}{10} - 1 \right) = 0.0024$$

$$\epsilon_{s1} > \epsilon_y = 0.0021$$

$$f_{s1} = -60 \text{ ksi}$$

## Column



### Sample Calculation



Use  $c = 10$  (Moments are summed about the plastic centroid or you must include  $P$  in the calculation.)

(Note: technically, you should subtract out the steel from the concrete area, but it only makes about 2% difference!)

$$P = 689 \text{ k} + 4(60) + 2(29) - 2(11.3) - 4(52.2) = 756 \text{ k}$$

$$M = -689 \left( \frac{7.5}{2} - 9 \right) - 4(60)(2.0 - 9) - 2(29)(6.7 - 9) \\ + 2(11.3)(11.3 - 9) + 4(52.2)(16 - 9)$$

$$M = 6,944 \text{ k-in} = 578 \text{ k-ft}$$

## Column

Now reduce by the phi factor:

$$P_{max} = 0.8\phi P_n = 0.52P_n \text{ for tied columns.}$$

$$P_{max} = 0.52(2,311 \text{ k}) = 1,295 \text{ k}$$

For values of extreme tensile steel  $< \epsilon_y$   $\phi = 0.65$

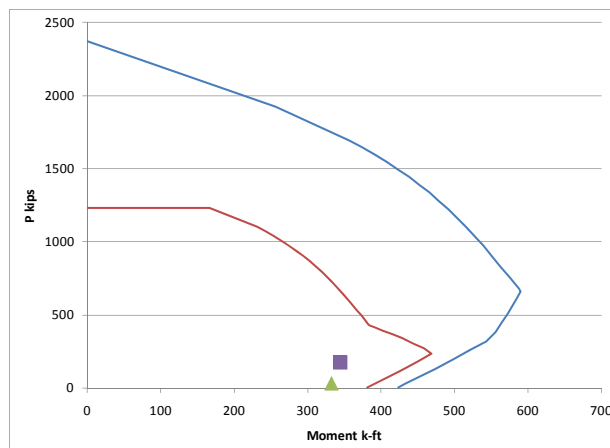
For values of extreme tensile steel  $> 0.005$   $\phi = 0.9$

Interpolate in between



Gravity

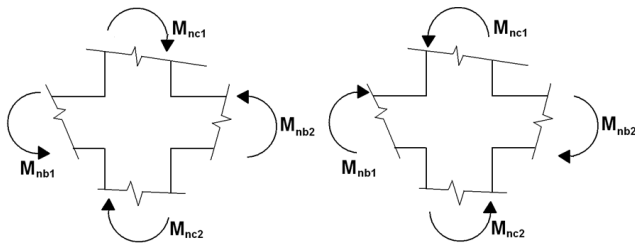
## Column



Gravity

Here are the nominal interaction diagrams. The points represent maximum and minimum P with associated moments; 174 k, 345 k-ft and 30 k, 333 k-ft. Both are within the reduced curve, so the column is adequate.

## Special Seismic Frame Philosophy

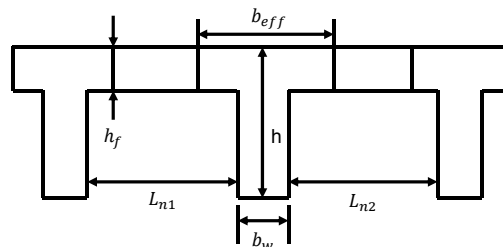
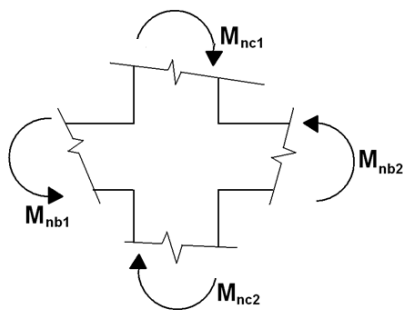


We want the hinges to form by yielding the **beams**, so ACI 18.7.3 requires:

$$\sum M_{nc} \geq 1.2 \sum M_{nb}$$

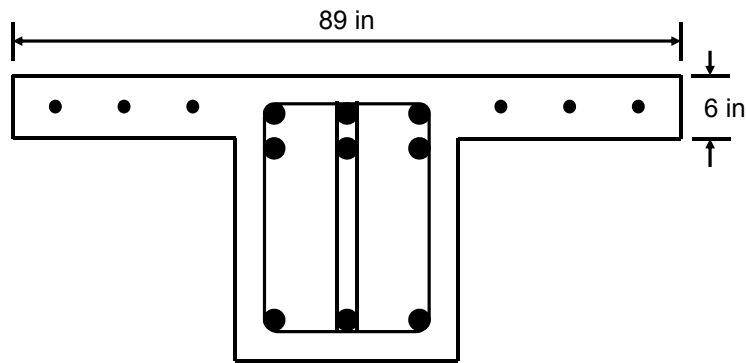
Note that these are the **nominal** moment strengths of the beams and columns. Note that  $M_{nb}$  must consider “T” beam flanges (18.7.3.2).

## Special Moment Frames Columns 18.7.3.2



$M_{nb}$  **must** include any slab reinforcing in the effective flange width! Effective flange width in tension is defined as the same as a flange width in compression (6.3.2.1).

## Special Moment Frames Columns 18.7.3.2



$\phi M_{nb}$  for this section, both positive and negative, was found previously.

## Special Moment Frames Columns 18.7.3.2

So the nominal strength of the beams is:

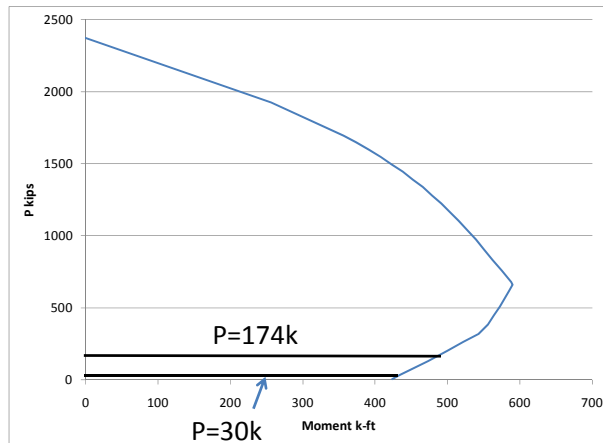
$$\phi M_{nb}^{(+)} = 179 k - ft$$

$$\phi M_{nb}^{(-)} = 370 k - ft$$

$$\phi M_{nb}^{(+)} + \phi M_{nb}^{(-)} = (179 k - ft + 370 k - ft)/0.9 = 610 k - ft$$

The  $\phi$  must be divided out since the equation requires  $M_{nb}$  not  $\phi M_{nb}$ .

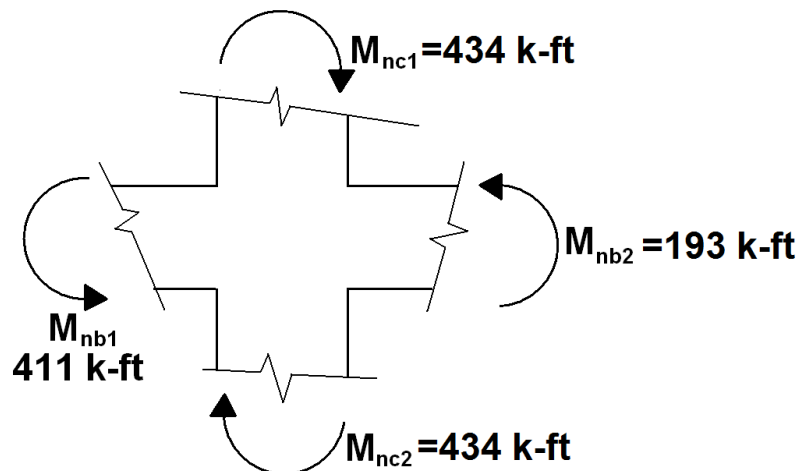
## Special Moment Frames Columns 18.7.3.2



Find  $M_n$  for the column. That depends on  $P_u$ . Using the **nominal** interaction diagram, find  $M$  for the maximum  $P$  (174 k) and the minimum  $P$  (30 k).

Use the smallest moment (434 k ft @ 30 k).

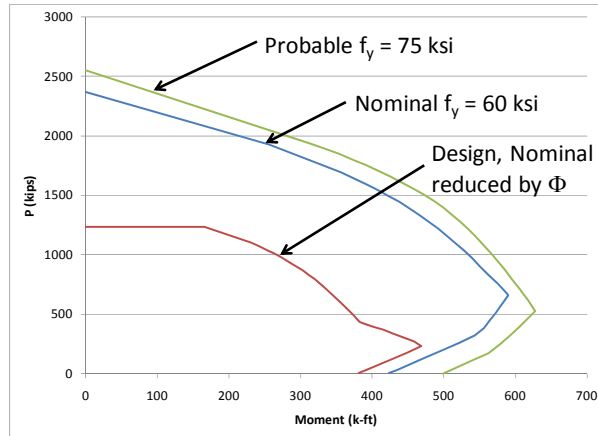
## Special Moment Frames Columns 18.7.3.2



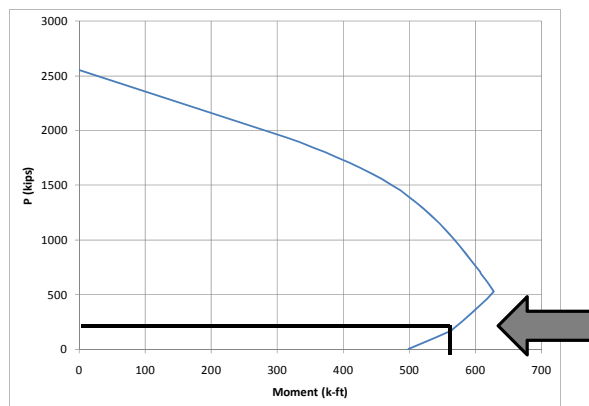
$$1.2 \sum M_{nb} = 732 \text{ k-ft} < \sum M_{nc} = 868 \text{ k-ft} \text{ OK}$$

## Special Moment Frames Columns 18.7.3.2

Now for shear: We must construct the **probable** interaction diagram for the column. We assume  $f_y = 1.25(60) = 75$  ksi. Note that we cannot just multiply the nominal by 1.25; the steel strength increases, not the concrete.



## Special Moment Frames Columns 18.7.3.2

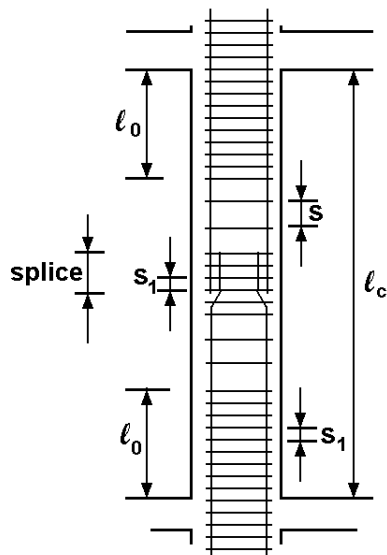


The probable interaction diagram is constructed using the same method as the nominal, but uses  $1.25f_y$ .

The maximum possible probable moment is 627 k-ft, but 18.7.6.1.1 says “over the range of  $P_u$ ”. The largest moment is for  $P_u = 174$  k,  $M_{pr}$  is approximately 565 k-ft.



## Special Moment Frames Columns



Column transverse steel requirements.

18.7.5.1 First hoop  $s_1/2$  from face of joint.

$l_o$  is the greatest of: 18 in;  $c_1$  or  $l_c/6$

$s_1$  is the least of  $6d_b$ ,  $c_1/4$ ,  $c_2/4$  or

$$4" \leq s_o = 4 + \left( \frac{14 - h_x}{3} \right) \leq 6"$$

The term  $h_x$  is the maximum c/c spacing of the longitudinal bars laterally supported by hoop corners or cross ties around column perimeter.

$s \leq$  lesser of  $6d_b$  or 6 inches

Or as required to enclose a mechanical or welded splice or as req'd for shear strength.

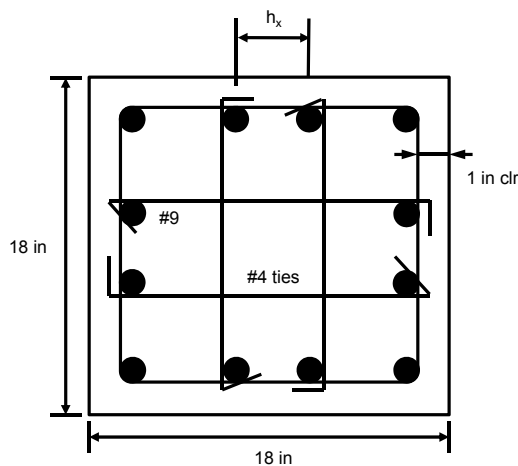
## Column Transverse Reinforcement 18.7.5.2

- Must be single or overlapping spiral, circular hoops or rectilinear ties or cross ties.
- Bends of rectilinear hoops must engage peripheral longitudinal bars.
- Cross ties of the same or smaller bar are permitted subject to limitations of 25.7.2.2. Cross tie ends must alternate end for end along the longitudinal reinforcement and around the perimeter of the column.

## Column Transverse Reinforcement 18.7.5.2

- Rectilinear hoops or cross ties must provide lateral support to longitudinal bars according to 25.7.2.2 and 3.
- The term  $h_x \leq 14$  inches.
- If  $P_u > 0.3f'_c A_g$  or  $f'_c > 10,000$  psi, in columns with rectilinear hoops, every longitudinal bar must have lateral support and  $h_x \leq 8$  in.  $P_u$  is largest value of  $P_u$  for any factored load combination containing E.

## Column Cross Ties



Term  $h_x$ : Column width, minus cover and ties, minus one  $d_b$  divided by spaces.

The term  $h_x$  is the c/c distance between longitudinally supported bars.

$$h_x = \frac{18 - 2(2) - 2(0.5) - 1.125}{3 \text{ spaces}} = 4.6 \text{ in}$$

This column has every bar supported so it meets 18.7.5.2 regardless of the value of  $P_u$ .

From the earthquake load combination  $P_u = 174$  kips.

$$0.3(6 \text{ ksi})(18 \text{ in})(18 \text{ in}) = 583 \text{ k} > 174 \text{ k}$$

And  $f'_c = 6,000$  psi  $< 10,000$  psi.

## Column Cross Ties

This column has every bar supported so it meets 18.7.5.2 regardless of the value of  $P_u$ :

$$s_0 = 4 + \left(\frac{14-h_x}{3}\right) = 4 + \left(\frac{14-4.6}{3}\right) = 7.1 > 6$$

Maximum spacing:

$$s_0 = 6 \text{ in}$$

$$\text{or } c_1/4 \text{ or } c_2/4 = 18/4 = 4.5 \text{ in} \quad \leftarrow \text{Controls for } s_0$$

$$\text{or } 6d_b = 6(1.125) = 6.75$$

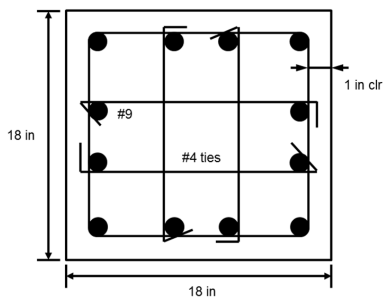
$$\ell_o = \text{clear span}/6 = 120 \text{ in}/6 = 20 \text{ in}$$

$$\text{or } c_1 = 18 \text{ in or } 18 \text{ in min}$$

20 in controls (use max).

Round down  $s_0$  to 4 inch spacing over at least  $\ell_o = 20$  in and at splice.

## Column Cross Ties



Minimum tie area (18.7.5.4) for rectilinear ties.  $A_{ch}$  is the core area out-to-out of ties.

$$A_{ch} = (18 - 2)(18 - 2) = 256 \text{ in}^2$$

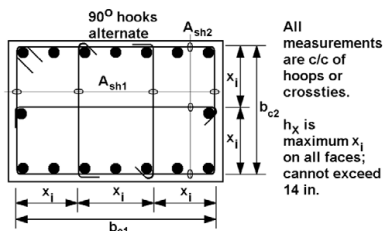
$$A_g = 18^2 = 324 \text{ in}^2$$

$$b_{c1} = b_{c2} = 18 - 2 - 0.5 = 15.5 \text{ in}$$

$$A_{shmin} = 0.3sb_c \frac{f'_c}{f_{yt}} \left(\frac{A_g}{A_{ch}} - 1\right)$$

$$A_{shmin} = 0.3(4)(15.5) \frac{6}{60} \left(\frac{324}{256} - 1\right) = 0.50 \text{ in}^2$$

Definitions:



$$A_{shmin} = 0.09sb_c \frac{f'_c}{f_{yt}} = 0.09(4)(15.5) \frac{6}{60} = 0.56 \text{ in}^2$$

$$A_{sh,provided} = 0.80 \text{ in}^2 \text{ OK}$$

## Column Cross Ties

If  $P_u \geq 0.3A_gf'_c$  or  $f'_c \geq 10,000$  psi, a third equation must be checked:

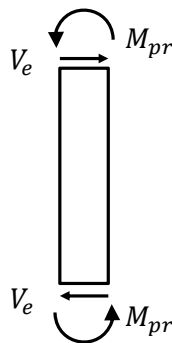
$$A_{sh} \geq 0.2k_fk_n \frac{P_u}{f_{yt}A_{ch}} sb_c$$

$$k_f = \frac{f'_c}{25000} + 0.6 \leq 1.0$$

$$k_n = \frac{n_i}{n_i - 2}$$

The term  $n_i$  is the number of longitudinal bars around the perimeter with rectilinear hoops that are laterally supported by corners or seismic hoops. This is new in ACI 318-14.

## Column



18.7.6.2.1 requires  $V_c$  taken = 0 within  $\ell_o$  when  $V_e > 0.5V_u$  within  $\ell_o$  and  $P_u < A_gf'_c/20$ .

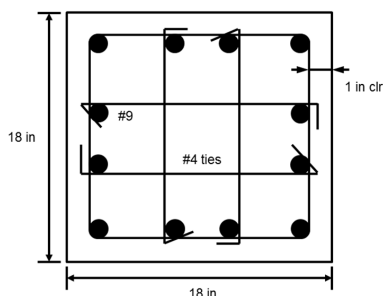
$$V_e = \frac{2(565 \text{ k-ft})}{10 \text{ ft}} = 113 \text{ k}$$

$$P_{min} = 30 \text{ k} < 0.05A_gf'_c = 97 \text{ k}$$

$$V_c = 0$$

Stirrups = #4 at 4

$M_{pr}$  max. corresponding to range of  $P_u$  previously found as 565 k-ft.



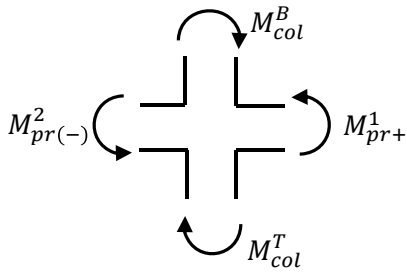
$$\phi V_s = (0.75) \frac{0.8 \text{ in}^2 (60 \text{ ksi}) (15.9 \text{ in})}{4 \text{ in}} = 143 \text{ k}$$

$$\phi(V_c + V_s) = 143 \text{ k} > V_e = 113 \text{ k}$$

$V_e$  must be  $>$  factored  $V_{analysis}$

$V_e$  constant, so #4 at 4 throughout column.

## Column



$$M_{top} = \frac{\left(\frac{EI}{\ell_c}\right)_{top}}{\left(\frac{EI}{\ell_c}\right)_{top} + \left(\frac{EI}{\ell_c}\right)_{bot}} (M_{pr+}^1 + M_{pr(-)}^2)$$

$$M_{bot} = \frac{\left(\frac{EI}{\ell_c}\right)_{bot}}{\left(\frac{EI}{\ell_c}\right)_{top} + \left(\frac{EI}{\ell_c}\right)_{bot}} (M_{pr+}^1 + M_{pr(-)}^2)$$

There is an alternative way to find  $V_e$ :

18.7.6.1.1 says the shear at the end of the column does not need to exceed that calculated from resistance the beams can provide.

Recall that the sum of the beam probable moments was

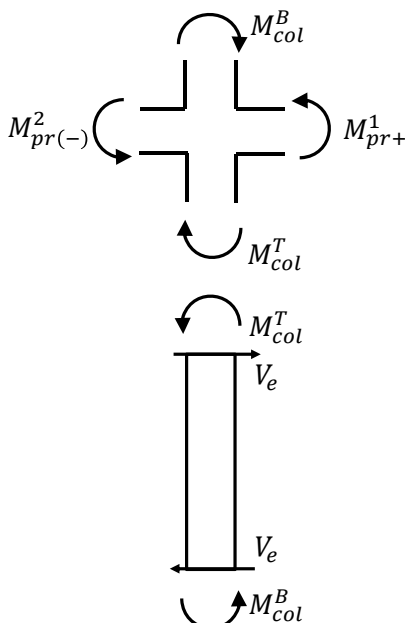
$$199 + 411 = 610 \text{ k-ft}$$

These moments can be distributed to the columns above and below the beam according to the relative stiffness of the columns, as shown in the formula to the left.

If the columns above and below the beam have the same stiffness:

$$M_{col}^T = M_{col}^B = 610/2 = 305 \text{ k-ft}$$

## Column



Next, you would have to repeat this calculation at the joint above (for the top column) and below (for the bottom column).

For the sake of illustration, assume the moment at the bottom of the lower column is 330 k-ft.

$$\text{So, } V_e = (305 + 330)/10 = 63.5 \text{ k}$$

The stirrup calculation is done the same as before, but the smaller  $V$  allows a larger stirrup spacing outside of  $\ell_o$ .

## Column Splice

### Column Splice Length

18.7.4.3 requires:

Mechanical splices conform to 18.2.7 and welded splices conform to 18.2.8.

Lap splices are permitted only within the center half of the column, must be tension splices and must be enclosed within transverse reinforcement according to 18.7.5.2 and 3 (see previous calculations for  $\ell_o$  ties).

## Column Splice

$s = 4$  inches controls.

$$K_{tr} = \frac{40(0.8 \text{ in}^2)}{4 \text{ in}(4 \text{ bars})} = 2$$

$$c_b = 2.1 \text{ inches}$$

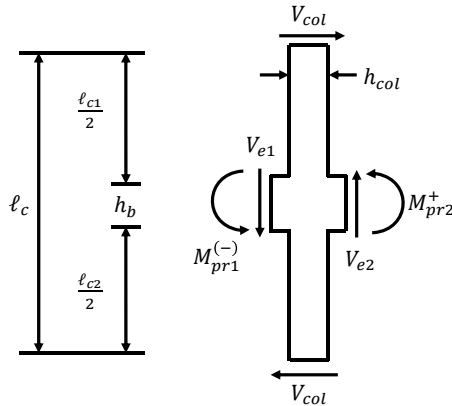
All values of  $\Psi$  and  $\lambda = 1$ .

$$\frac{c_b + K_{tr}}{d_b} = \frac{2.10 + 2}{1.125} = 3.6 > 2.5$$

$$\ell_d = \frac{3}{40} \frac{60000}{\sqrt{6000}(2.5)} (1.125) = 26.0 \text{ in}$$

$$1.3\ell_d = 1.3(26.0) \approx 34 \text{ in Class B splice}$$

## Special Moment Frames Joints



To determine joint shear, we use the probable moments including the slab. The beam shears are from beam design. The sum of the probable beam moments is 681 k-ft and the beam shear was 27.2 k.

$$V_{col} = \left[ \left( M_{pr}^{(-)} + M_{pr}^{(+)} \right) + (V_{e1} + V_{e2}) \frac{c_1}{2} \right] \frac{1}{\ell_c}$$

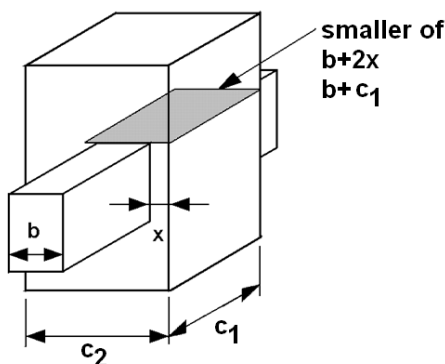
$$\ell_c = 2 \frac{10}{2} + 2 = 12 \text{ ft}$$

$$V_{col} = \left[ 681 \text{ k-ft} + 2(27.2 \text{ k}) \frac{1.5 \text{ ft}}{2} \right] \frac{1}{12 \text{ ft}} = 60 \text{ k}$$

## Special Moment Frames Joints

18.8.4.3 defines the shear area of the joint,  $A_j$ .

If the beam width is not smaller than the column:  $A_j = c_1 c_2$

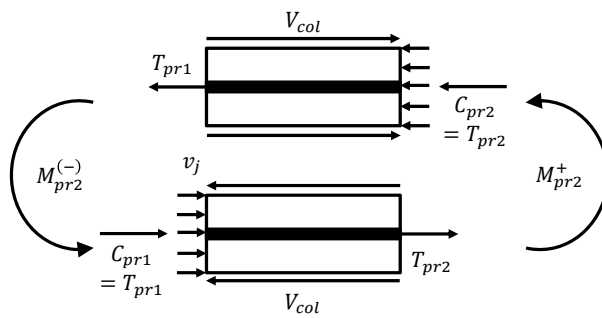


If the beam is smaller than the column, the depth of the joint is still  $c_1$ . The width is the smaller of

$$c_1 + b_{beam} \leq b_{beam} + 2x \leq c_2$$

where  $x$  is the smallest distance from the face of the beam to the face of the column.

## Special Moment Frames Joints



$$V_j = T_{pr2} + C_{pr1} - V_{col}$$

$$V_j = C_{pr2} + T_{pr1} - V_{col}$$

$$T_{pr1} = 3.6 \text{ in}^2 (75 \text{ ksi}) = 270 \text{ k}$$

$$T_{pr2} = 1.8 \text{ in}^2 (75 \text{ ksi}) = 135 \text{ k}$$

$$V_j = 270 + 135 - 60 = 345 \text{ k}$$

18.8.4.3: The joint is  $c_1 = 18$  in long. The width is:

Smallest of  $b + c_1 = 14 + 18 = 32 \text{ in}$  ( $b$  is beam width)

$$b + 2x = 14 + 2 + 2 = 18 \text{ in} \leq c_2$$

( $x$  is the shortest distance from the edge of the beam to the column face.)

ACI 318 does not require considering the slab steel, but some designers do.

## Special Moment Frames Joints

18.8.4.1:

If the joint is confined on all four faces:

$$V_n = 20\sqrt{f'_c} A_j$$

If the joint is confined on 3 faces or 2 opposite faces:

$$V_n = 15\sqrt{f'_c} A_j$$

All other cases:

$$V_n = 12\sqrt{f'_c} A_j$$

For lightweight concrete, multiply the limits above by 0.75.

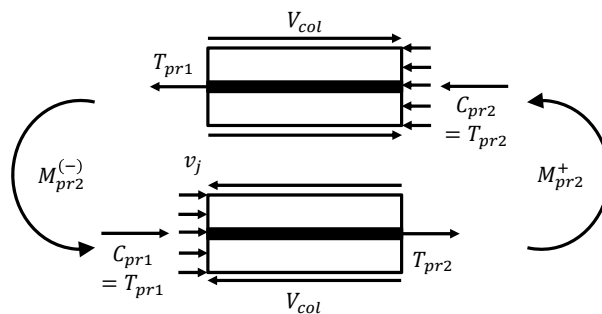


## Special Moment Frames Joints

### 18.8.4.2:

- Members that frame into a joint provide confinement **if** the framing member covers at least  $\frac{3}{4}$  of the face of the joint.
- Extensions of beams at least overall beam depth  $h$  beyond the joint face may be considered as confining members if the extension meets:
  - $b_w > 0.3 h > 10$  in (18.6.2.1b)
  - Have minimum flexural reinforcing (18.6.3.1)
  - Required hoops (18.6.4.2, 3 and 4)

## Special Moment Frames Joints



Joint is confined by beams on all 4 faces.

$$V_j = 345 \text{ k}$$

$$A_j = 18 \text{ in}(18 \text{ in}) = 324 \text{ in}^2$$

$$V_n = 20\sqrt{6,000 \text{ psi}(324 \text{ in}^2)}$$

$$= 502,000 \text{ pounds}$$

$$\phi V_n = 0.75(502 \text{ k}) = 377 \text{ k} > 345 \text{ k}$$

## Special Moment Frames Joints

### 18.8.3.1:

- Transverse Reinforcement
  - Provide transverse hoop reinforcement, the same as in the  $\ell_o$  region (18.7.5.2, 3, 4 and 7) in the joints unless the joint is confined by structural members (see next slide).

## Special Moment Frames Joints

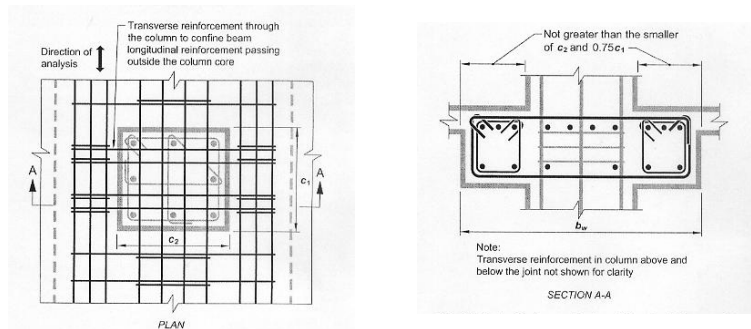
### 18.8.3.2:

- Transverse Reinforcement
  - If the joint is confined by structural members on all 4 sides and the member width is at least  $\frac{3}{4}$  of the column width, the amount of hoop reinforcing may be reduced by  $\frac{1}{2}$  and the spacing may be increased to 6 inches. This may be done within  $h$  of the shallowest beam.

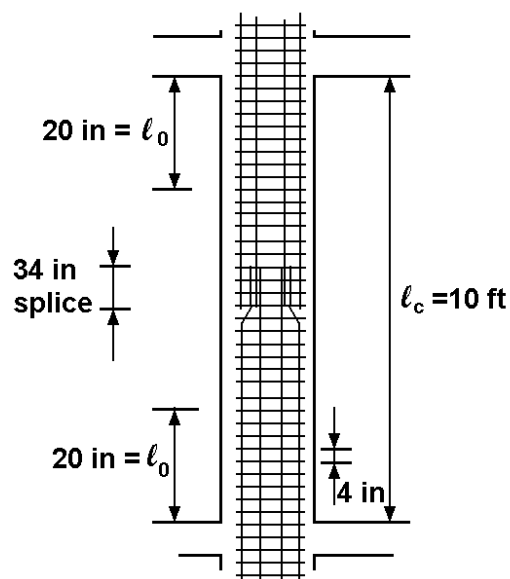
## Special Moment Frames Joints

### 18.8.3.3:

- Transverse Reinforcement
  - Longitudinal beam reinforcement outside the column core shall be confined by transverse steel passing through the column that satisfies spacing requirements of 18.6.4.4, and requirements of 21.6.4.2 and 3.

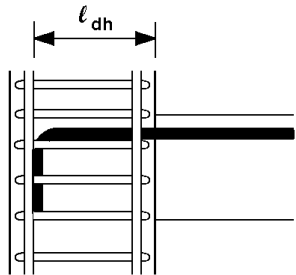


## Final Column Design



## Development Length Within a Joint

18.8.5.1 For #3 - #11 bar, the development length for a standard, 90° hook in tension shall not be less than the largest of:



$$\ell_{dh} = \begin{cases} 6 \text{ in} \\ 8d_b \\ \frac{f_y d_b}{65\sqrt{f'_c}} \end{cases}$$

Hook must be confined within the confined column core! It is good detailing to make the hook go all the way through the column.

## Development Length Within a Joint

18.8.5.1 For #3 - #11 bar, the development length for a standard, 90° hook in tension **in lightweight concrete** shall not be less than the largest of:

$$\ell_{dh} = \begin{cases} 7.5 \text{ in} \\ 10d_b \\ \frac{f_y d_b}{65\lambda\sqrt{f'_c}} \end{cases}$$

Take  $\lambda = 0.75$  for lightweight concrete.

## Development Length Within a Joint

- 18.8.5.3: The development length,  $\ell_d$ , for straight bar, #3 - #11:
  - If the depth of the concrete poured in a single lift below the bar is 12 inches or less,  $2.5\ell_{dh}$  from the previous two slides.
  - If the depth of the concrete poured in a single lift below the bar is greater than 12 inches,  $3.25\ell_{dh}$  from the previous two slides.

## Development Length Within a Joint

- 18.8.5.4: If a straight bar is terminated at a joint
  - It shall pass through the confined core of the column or boundary element
  - Any part of  $\ell_d$  outside of the confined core shall be increased by 1.6.
- Epoxy coated bars or hooks shall be multiplied by the epoxy bar factors in 25.4.2.4 (straight bar) or 25.4.3.2 (hooks).

## Development Length Within a Joint

- Epoxy bar factor 25.4.2.4 (straight bar)
  - 1.2
  - 1.5 if the cover is less than  $3d_b$  or the clear spacing is less than  $6d_b$
- Epoxy bar factor 25.4.3.2 (hooks)
  - 1.2

## Development Length Within a Joint

$$\ell_{dh} = \frac{60,000(0.875)}{65\sqrt{6,000}} = 10.5 \text{ in} > 8d_b = 7 > 6 \text{ in}$$

$$\ell_d = 2.5(10.5) = 26 \text{ in}$$

$$\ell_{d,topbar} = 3.25(10.5) = 33.9 \text{ in}$$

So at the end of the building, the hooks must be embedded 10.5 inches into the columns.

The bars going through the interior columns must have the development lengths shown; 26 inches bottom bars, 34 inches top bar.

Questions

**Thank you!**

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